



High-pressure responses of alkali metal hydrogen carbonates, RbHCO₃ and CsHCO₃: Findings of new phases and unique compressional behavior



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ABSTRACT

High-pressure responses of RbHCO₃ and CsHCO₃ were characterized by *in situ* Raman spectroscopy and X-ray and neutron diffraction observations. RbHCO₃ exhibited a monoclinic (phase IV) and a triclinic (phase V) high-pressure phase at ~0.5 GPa and room temperature. Increasing compression induced unique behavior in a specific cell parameter (*a* in phase IV or *c* in phase V), which first increased, and then decreased at ~1 GPa, likely owing to the rearrangement of Rb⁺ and reconfiguration of the ordered (HCO₃⁻)₂ dimers. Deuterium positions in phase IV of RbDCO₃ were determined. The hydrogen bonding remained moderately strong, and possibly did not affect the phase transition despite the accompanying disordering and ordering of the dimers. CsHCO₃ showed no structural change up to 5 GPa, suggesting that its ambient phase (isostructural to phase IV of KHCO₃) was already stable at high pressure. The structural stability appeared to be systematically related to the cation size.

1. Introduction

Behaviors of some carbonates and hydrous minerals at high pressure are fundamentally important to geochemical systems and processes, such as the global carbon cycle, the evolution of the atmosphere, and water storage in the deep Earth. Carbonates and bicarbonates (hydrogen carbonates) act as sinks for carbon dioxide. There is increasing interest in these materials for use in the sequestration of CO₂ produced by the combustion of fossil fuels, and their locality and thermodynamic behaviors have been studied. Hydrogen carbonates are minor minerals, but they show interesting characteristic of hydrogen bonding that affects their phase stability. Therefore, the pressure responses of these materials have attracted much attention, not only in geoscience and biomineralogy, but also in physical chemistry.

Alkali metal hydrogen carbonates (MHCO₃, M = Na, K, Rb, and Cs) are a series of inorganic substances that contain HCO₃⁻ anions and alkali metal (elemental) cations. NaHCO₃ (nahcolite) has a structure consisting of infinite chains of HCO₃⁻ [1,2]. The other three hydrogen carbonates have HCO₃⁻ ions that form dimers connected by two hydrogen bonds. These dimers align parallel with each other to create the crystal structure, and the cations occupy the spaces between them. The ambient phase of KHCO₃ (phase II, monoclinic, *P*₂₁/*a*) undergoes several transitions at high pressure or temperature. A temperature-induced phase transition at *T*_C = 318 K (351 K for KDCO₃) takes the ambient phase II to

high-temperature (high-T) phase I (monoclinic, *C*₂/*m*) [3]. At room temperature, KHCO₃ transforms at ~3 GPa [4–6], and there are two stable two high-pressure (high-P) phases, which are monoclinic phase IV (*P*₂₁/*b*, non-standard setting of *P*₂₁/*c*) reported by Komatsu et al. [7] and triclinic phase V (*P*⁻) reported by Allan et al. [8]. These two high-P phases have been observed, either singly or together, under various experimental conditions using single-crystal X-ray diffraction (XRD) [7], single-crystal XRD, and powder neutron diffraction [8], and their abundance ratio varied with each experimental run. Takasaka et al. [9] reported another high-P phase (phase III, triclinic *C*₁ or *C*⁻) under high shear stress. The (HCO₃⁻)₂ dimers were disordered only in the high-T phase I, and they were ordered in all other KHCO₃ polymorphs. Table 1 summarizes the structural information for the KHCO₃ polymorphs, RbHCO₃, and CsHCO₃. The Roman numeral phase identifiers for RbHCO₃ and CsHCO₃ are first given in this study. Although phase III of RbHCO₃ has not yet been reported, the numeral is reserved in case of its discovery, which is considered highly likely. In contrast, the phases of CsHCO₃ are renumbered from I, because there is no guarantee of finding phases corresponding to phases I to III of KHCO₃ or RbHCO₃.

Under ambient conditions, RbHCO₃ and CsHCO₃ have (HCO₃⁻)₂ dimer configurations, but take slightly different structures to KHCO₃ depending on pressure and temperature. The ambient phase of RbHCO₃ (phase I) is isostructural with KHCO₃ (phase I, *C*₂/*m*), and has disordered hydrogen atoms. Larvor and Stöger [10] reported it transforms into an

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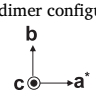
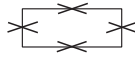
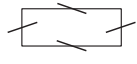
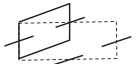

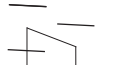
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Table 1
Summary of phases and corresponding structures of KHCO_3 , RbHCO_3 , and CsHCO_3 .

crystal system	monoclinic	monoclinic	triclinic	monoclinic	triclinic
dimer configuration 					
KHCO_3	disordered I	ordered (anti-phase) II	ordered (in-phase) III	ordered (anti-phase) IV	ordered (in-phase) V
RbHCO_3^a	high-T > 318K Ref. [3] I	low-T (ambient) Ref. [3] II	shear-stress-induced Ref. [9] III	high-P > 2.8 GPa Refs. [4–7] IV	high-P > 3.2 GPa Ref. [8] V
CsHCO_3^a	high-T (ambient) Ref. [10]	low-T < 245K Ref. [10]	Undiscovered	high-P > ~0.5 GPa This study I ambient Ref. [11]	high-P > ~0.5 GPa This study

^a Phase numbers for RbHCO_3 and CsHCO_3 are first given in this study. See details in text.

ordered phase (C1) at low temperature (below 245 K). The structure of CsHCO_3 [11] (designated here as CsHCO_3 phase I, Table 1) is equivalent to the high-P phase IV of KHCO_3 , although the positions of the hydrogen atoms remain unclear [7]. Therefore, systematic changes in the phase relations may be possible in MHCO_3 hydrogen carbonates, where $M = \text{K}$, Rb , and Cs . Pressure-induced phase transitions generally follow patterns in isostructural compounds depending on the cation size (e.g., alkali metal chlorides MCl , $M = \text{Na}$, K , Rb , and Cs). However, no high-P behavior has been reported for the hydrogen carbonates RbHCO_3 and CsHCO_3 . Any trends in the series should be clarified to improve understanding of the behavior of hydrogen bonding in these crystal structures under high pressure.

In the present study, the high-P behaviors of RbHCO_3 and CsHCO_3 were investigated via *in situ* studies using Raman spectroscopy, powder XRD, and neutron diffraction. The phase relations, hydrogen bonding configuration, and its stability in the structures are discussed.

2. Experimental methods

2.1. Sample syntheses

CsHCO_3 was obtained commercially from Wako Pure Chemical Industries, Ltd. (purity 99%). RbHCO_3 and RbDCO_3 were synthesized from Rb_2CO_3 (purity 99% (2 N), Kojundo Chemical Laboratory Co., Ltd.) in our laboratory. All synthesized samples were identified as well-crystallized powders from powder XRD patterns (MiniFlex II, Rigaku; 30 kV, 15 mA, $\text{CuK}\alpha$) and Raman spectra (see later in Section 2.3).

2.1.1. RbHCO_3

Powdered RbHCO_3 was synthesized by the reaction $\text{Rb}_2\text{CO}_3 + \text{H}_2\text{O} + \text{CO}_2 \rightarrow 2\text{RbHCO}_3$. Using the difference in aqueous solubility between Rb_2CO_3 (223 g/100 g water at 20 °C) and RbHCO_3 (116 g/100 g water at 20 °C) [12], RbHCO_3 crystals were precipitated from a water–ethanol solution. Rb_2CO_3 (2 g) was placed in a beaker to which was added ethanol (100 mL). Pure water (milli-Q; Nihon Millipore Ltd.) was injected dropwise with a syringe until the Rb_2CO_3 crystals dissolved completely. The mixed solution was filtered through a funnel to remove undissolved reagents. CO_2 was bubbled into the mixed solution for several hours until

the amount of crystals did not obviously increase. The solution was vacuum filtered, and the crystalline powder was dried and kept in a vacuum desiccator to avoid absorbing atmospheric moisture.

2.1.2. RbDCO_3

Deuterated substitutes are commonly used in neutron diffraction experiments to avoid large incoherent scattering by hydrogen, which causes high background in the diffraction patterns. Powdered RbDCO_3 was synthesized similar to RbHCO_3 , but using D_2O (minimum isotope purity of 99.96 atom %, Aldrich Chemical Co. Inc.) instead of H_2O . The initial Rb_2CO_3 powder was baked in a muffle furnace at 300 °C for 24 h to decompose RbHCO_3 impurities to Rb_2CO_3 ($2\text{RbHCO}_3 \rightarrow \text{Rb}_2\text{CO}_3 + \text{H}_2\text{O} + \text{CO}_2$). The purified Rb_2CO_3 was dissolved in a small amount of D_2O , and this aqueous solution was filtered through a funnel to remove undissolved impurities. The solution was placed in a vacuum desiccator under a CO_2 atmosphere for several days, and RbDCO_3 crystals precipitated from the solution. The presence of CO_3^{2-} ions in the solution was checked using a saturated MgSO_4 aqueous solution, which caused any remaining CO_3^{2-} ions to precipitate as MgCO_3 . When almost all the CO_3^{2-} had been converted into DCO_3^- in the RbDCO_3 precipitate, the solution was desiccated under vacuum until all the water evaporated. Complete evaporation of water left high-purity RbDCO_3 . To avoid hydrogen exchange with atmospheric moisture, RbDCO_3 was stored in a vacuum desiccator.

2.2. High-pressure experiments using diamond anvil cells (DACs)

Samples were loaded in clamped DACs, consisting of type Ia diamond anvils with a culet diameter of 600 μm . Stainless steel (SUS 301) gaskets were pre-indented to a thickness of ca. 120 μm and a 300- μm -diameter hole was drilled in the center of the gaskets. A 4:1 methanol/ethanol mixture was used as a pressure-transmitting medium. To reduce the risk of isotope substitution by the pressure-transmitting medium, a deuterated alcohol mixture of dry CD_3OD (*d*4-MeOD) and $\text{C}_2\text{D}_5\text{OD}$ (*d*6-EtOD) (isotope purity of 99.8 atom %) was used for RbDCO_3 . The hydrogenated and deuterated alcohol mixtures were kept dehydrated using molecular sieves (pellet, Type-3A). The pressure was determined from several small ruby balls (several microns in diameter) using ruby

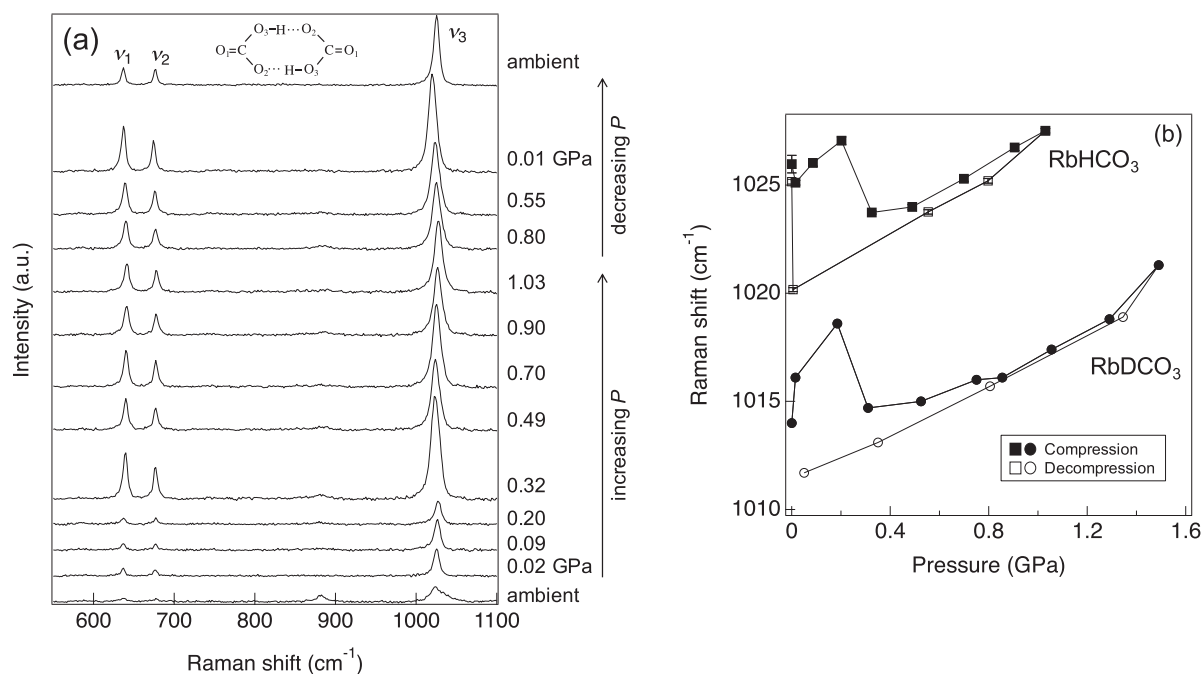


Fig. 1. (a) Raman spectra of RbHCO_3 under increasing pressure. Three bands derived from HCO_3 vibrations in $(\text{HCO}_3)_2$ dimers appeared in the range $600\text{--}1100\text{ cm}^{-1}$: 637 cm^{-1} (δ OCO (ν_1), C–O₂ stretching and in-plane C=O bending), 676 cm^{-1} (δ OCO (ν_2), combined in-plane O₂–C–O₃ bending), and 1037 cm^{-1} (ν_3 , combined C=O₁ stretching and C–O₃ stretching). (b) Raman shift of peak ν_3 for RbHCO_3 and RbDCO_3 vs. pressure.

fluorescence techniques [13].

2.3. Raman spectroscopy

Raman spectra at frequencies corresponding to the samples' vibration modes ($500\text{--}1200\text{ cm}^{-1}$) were measured at room temperature using a micro-Raman spectrometer housed at the Geochemical Research Center (GCRC), the University of Tokyo. The instrument consisted of a 50 cm single polychromator (500is, Chromex; 1200 grooves/mm diffraction grating, wavenumber resolution of $1.5\text{ cm}^{-1}/\text{pixel}$), a 514.5 nm Ar^+ laser (543AP-A01, Melles Griot), and a Si-based charge-coupled device camera (DU-401A-BR-DD, Andor Technology; 1024×128 pixels) electrically cooled to $-65\text{ }^\circ\text{C}$. The laser power was 5 mW for measuring samples and 0.2 mW for ruby fluorescence.

2.4. Synchrotron XRD

Angular-dispersive synchrotron XRD patterns of powder samples were obtained at the BL-18C beamline of the photon factory at the High Energy Accelerator Research Organization (KEK), Tsukuba, Japan. A monochromatized incident X-ray beam with an energy of $\sim 20\text{ keV}$ (ca. 0.6 \AA wavelength) was collimated to a diameter of $100\text{ }\mu\text{m}$. Diffracted X-ray patterns were recorded on an imaging plate (IP) with typical exposure times of 10–20 min. The 2D diffraction image on the IP was converted into an intensity– 2θ diffraction pattern using IPAnalyzer [14]. All the XRD profiles were fitted by Le Bail method using a symmetric pseudo-Voigt function with PDIndexer [14].

2.5. Powder neutron diffraction

Powder neutron diffraction patterns of RbDCO_3 were obtained at high pressure using a two-column Paris–Edinburgh press (type-VX4, maximum load of 200 t [15]). Single toroidal opposed anvils made of WC (diameter, 6 mm) and Ti–Zr capsulated gaskets were used for the anvil-cell assembly. The sample was loaded with a 4:1 deuterated d_4 -MeOD and d_6 -EtOD mixture as a pressure-transmitting medium. *In*

situ powder neutron diffraction experiments at up to $\sim 5\text{ GPa}$ were performed at beamline BL-11 (PLANET) [16], Material and Life Science Experimental Facility (MLF), Japan Proton Accelerator Research Complex (J-PARC), Tokai, Japan. A focusing mirror for incident neutrons was used and radial collimators were attached in front of the two perpendicular detector banks to reduce background. The diffraction patterns were measured by the time-of-flight method using a pulsed neutron beam. Measurement was typically for $\sim 7\text{ h}$ at an accelerator power of around 400 kW. The obtained d -spacing was doubled in a long-wavelength frame setting ($0.2\text{--}8.4\text{ \AA}$). Pressures were estimated from the volumetric compressibilities of RbHCO_3 and RbDCO_3 obtained from *in situ* XRD experiments at high pressure. Pressure uncertainties were estimated within $\pm 0.1\text{ GPa}$. Sample data were normalized by vanadium data to correct the energy profile of the incident neutron beam, detector sensitivity, and cell attenuation. Empty-cell data were subtracted from the individual data.

The crystal structures and atomic positions including deuterium were refined by the Rietveld technique [17] using the GSAS program [18]. The initial structure models of RbDCO_3 were taken from Larvor and Stöger [10] for the ambient phase ($C2/m$) and Komatsu et al. [7] for the high-P phase ($P12_1/c1$), where the unit cell parameters were slightly changed with reference to the compression data to allow consideration of the difference in pressure. Rietveld analyses were processed with individual constraining isotropic atomic displacement parameters U_{iso} for Ca, O, and D atoms. The d -ranges for the refinements were from ~ 0.6 to $\sim 4.2\text{ \AA}$.

3. Results and discussion

3.1. RbHCO_3

3.1.1. Raman spectra

Fig. 1 shows the Raman spectra for RbHCO_3 during compression and decompression. At ambient pressure, the region of $600\text{--}1100\text{ cm}^{-1}$ contained three characteristic peaks derived from HCO_3 vibration modes in $(\text{HCO}_3)_2$ dimers: 637 cm^{-1} (ν_1) for C–O₂ stretching and in-plane C=O₁ bending, 676 cm^{-1} (ν_2) for combined in-plane O₂–C–O₃

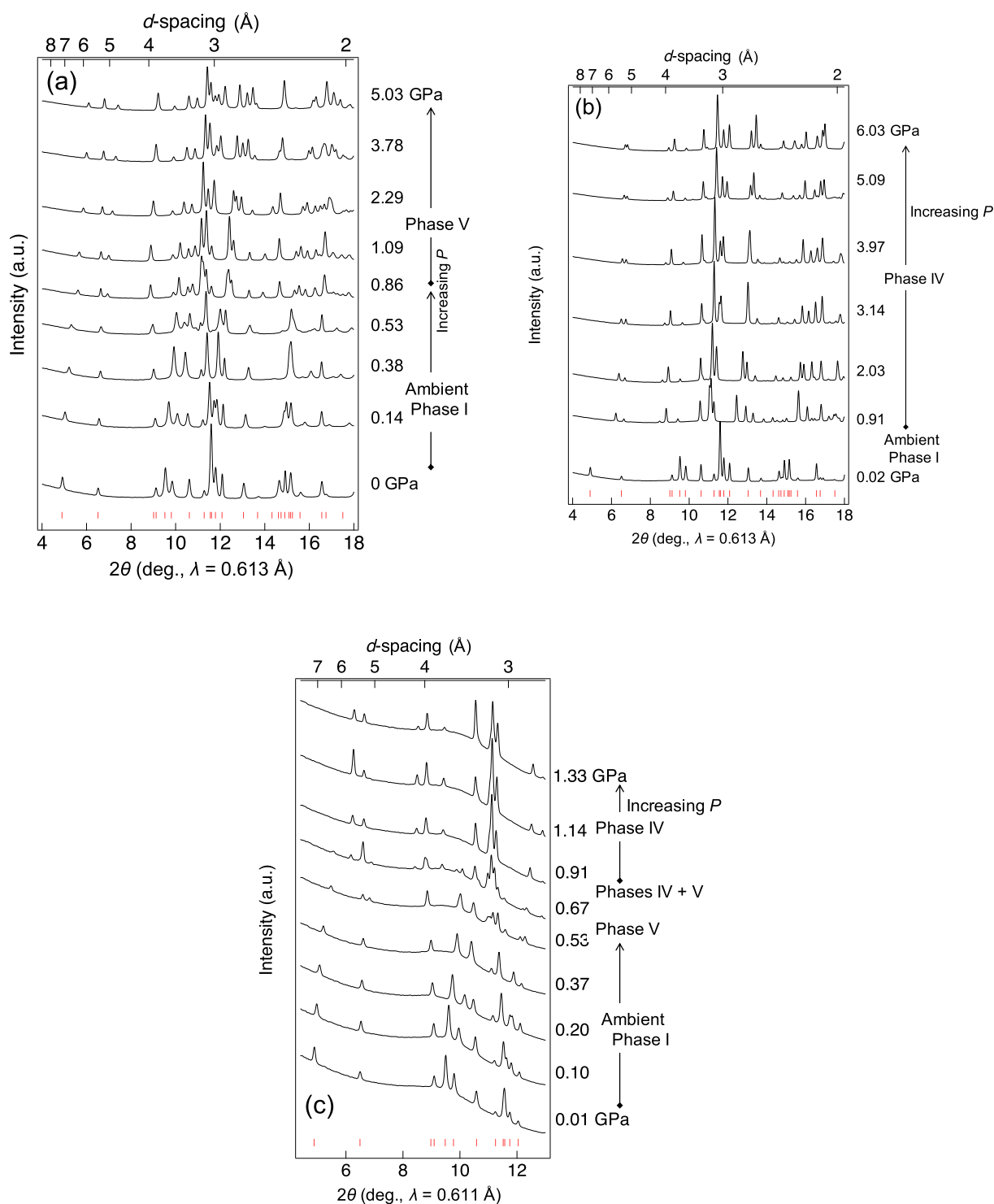


Fig. 2. Representative XRD patterns of RbHCO_3 under high pressure. High-P phases emerge through one of three phase transitions: (a) phase V, (b) phase IV, and (c) coexistence of phases IV and V. Tick marks below the patterns show the peak positions for the ambient phase I at ambient condition. Wavelength of X-ray was $\lambda \sim 0.61 \text{ \AA}$.

bending, and 1037 cm^{-1} (ν_3) for the combination of $\text{C}=\text{O}_1$ stretching and $\text{C}-\text{O}_3$ stretching (Fig. 1a). With increasing pressure, the most intense peak, ν_3 , gradually shifted to higher frequency, but dropped discontinuously from 1027 to 1024 cm^{-1} between 0.2 and 0.32 GPa (Fig. 1b). The other two peaks showed similar pressure responses to ν_3 . The discontinuous drops in the vibrational modes corresponded to changes in the structure and orientation of the dimers, which was also supported by the

XRD results described in Section 3.1.2. Further increases in pressure caused the frequencies of the three Raman peaks to increase monotonically. During decompression, the frequencies decreased continually, and ν_3 became 1020 cm^{-1} near 0 GPa , which was much lower than the initial value of 1026 cm^{-1} . After the DAC was opened and left at ambient conditions for several hours, ν_3 returned to 1026 cm^{-1} , indicating that the back transition occurred with a large pressure hysteresis. RbDCO_3

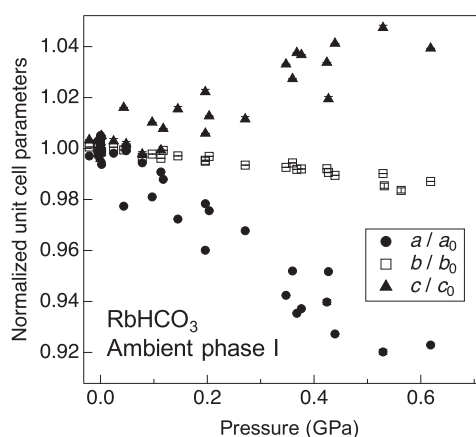


Fig. 3. Pressure dependence of normalized unit cell parameters, the ratios a/a_0 , b/b_0 , and c/c_0 in RbHCO_3 ambient phase I calculated from powder XRD results. The a_0 , b_0 , and c_0 are the cell parameters at ambient condition.

behaved almost identically, suggesting there were no H–D isotope effects on the pressure response (Fig. 1b).

3.1.2. XRD

RbHCO_3 transformed into high-P phases above about 0.5 GPa. There were two high-P phases, and the phase transition occurred in the following ways (Fig. 2): (i) a transition to a triclinic phase, (ii) a transition to a monoclinic phase, and (iii) an initial transition to the triclinic phase and a subsequent transition to the monoclinic phase through the coexistence of these two phases. Fig. 2a shows XRD patterns for transition (i). The patterns between 0.1 MPa and 0.53 GPa showed the continuous compression of ambient phase I regardless of apparent changes due to anisotropic compressibility. At 0.86 GPa, several new peaks appeared, and RbHCO_3 underwent a phase transition to a triclinic phase with cell parameters at 0.86 GPa of $a = 6.875(5)$ Å, $b = 5.708(3)$ Å, $c = 4.354(4)$ Å, $\alpha = 93.45(6)^\circ$, $\beta = 101.64(11)^\circ$, and $\gamma = 110.27(4)^\circ$. This structure was isostructural with the high-P phase V of KHCO_3 reported by Allan et al. [8], and was stable up to 5 GPa. In transition (ii), a similar change in the diffraction pattern was observed above about 0.9 GPa, but below 8° only two peaks appeared (Fig. 2b) instead of the three peaks seen in phase V (Fig. 2a). This indicated the formation of a different phase with a diffraction pattern that matched that of the monoclinic high-P phase IV of KHCO_3 reported by Komatsu et al. [7]. The cell parameters at 0.9 GPa after the phase transition were $a = 4.373(3)$ Å, $b = 10.594(1)$ Å, $c = 6.809(5)$ Å, and $\beta = 101.65(5)^\circ$. This high-P phase IV of RbHCO_3 remained stable up to 6 GPa. In transition (iii) (Fig. 2c), RbHCO_3 underwent the first phase transition to phase V at 0.44–0.53 GPa, and then the two high-P phases V and IV coexisted. Above 0.91 GPa, a second transition led to a single phase (phase IV), which remained stable under further compression.

In more than 15 subsequent experiments, we sought to clarify the factors controlling the formation of the different high-P phases; the conditions we varied included the starting material (powder or single crystal), pressure-transmitting material (alcohol mixture, helium gas, or a fluorocarbon fluid), and compression speed. However, no clear dependence on these factors was observed.

Fig. 3 displays the pressure dependence of the cell parameters of ambient phase I of RbHCO_3 . Increasing pressure compressed both the a - and b -axes and elongated the c -axis. This anomalous elongation of the c -axis was not observed in the ambient phase of KHCO_3 (phase II) [4]. The ambient phase I of RbHCO_3 is isostructural to the high-T phase of KHCO_3 (phase I), which has disordered $(\text{HCO}_3)_2$ dimers [10] that may affect the high-P behavior. In the ambient phase I of RbHCO_3 , the stacked layers of disordered dimers along the c -axis may be affected strongly by changes in the dimer orientation and hydrogen bonding geometry. In addition, Rb^+

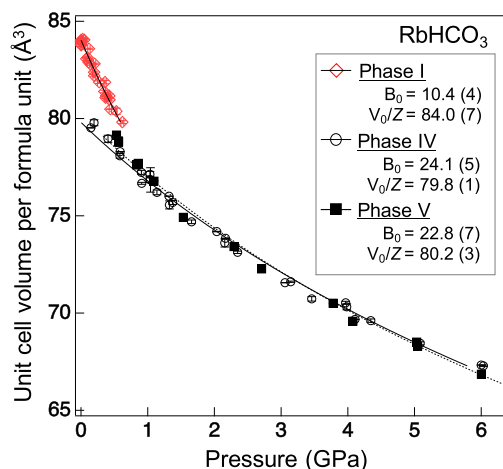


Fig. 4. Unit cell volume versus pressure in ambient phase I and high-P phases IV and V RbHCO_3 obtained by powder XRD. Error bars are smaller than the symbols.

Table 2

Results of Birch–Murnaghan fitting.

Phase	B_0	B'	V_0/Z	Refs.
KHCO_3 Phase II (ambient)	22.7(3)	4	77.78(3)	Nagai et al. [4]
KDCO_3 Phase II (ambient)	22.7(8)	4.1(5)	76.81(6)	Allan et al. [8]
KDCO_3 Phase V (high-P)	26.5(2.8)	5.2(6)	72.5(5)	Allan et al. [8]
RbHCO_3 Phase I (ambient)	10.4(4)	4 (fixed)	84.0(7)	This study
RbHCO_3 Phase IV (high-P)	24.1(5)	4 (fixed)	79.8(1)	This study
RbHCO_3 Phase V (high-P)	22.8(7)	4 (fixed)	80.2(3)	This study
CsHCO_3 Phase I (ambient)	22.5(6)	4 (fixed)	90.0(2)	This study

(larger than K^+) ions are arranged in Rb-O polyhedra by sharing O–O edges along the c -axis, and their mutual repulsion results in the elongation of this axis as shown later in Fig. 6c.

Fig. 4 shows changes of the unit cell volumes of the three RbHCO_3 polymorphs (phases I, IV, and V) with increasing pressure. The bulk modulus B_0 was estimated by fitting to the Birch–Murnaghan equation of state [19]:

$$P(V) = 3B_0/2 [(V_0/V)^{7/3} - (V_0/V)^{5/3}] \{1 + 3/4(B_0' - 4) [(V_0/V)^{2/3} - 1]\}, \quad (1)$$

where P is pressure, V is volume, and V_0 is the volume at ambient conditions. The fitting parameter B_0' was fixed as 4.

The B_0 and V_0 values obtained for RbHCO_3 are listed in Table 2 along with those for KHCO_3 from previous studies. RbHCO_3 ambient phase I has $B_0 = 10.4(4)$ GPa and $V_0 = 84.0(7)$ Å³. Its two high-P phases IV and V showed similar values for B_0 (24.1(5) and 22.8(7) GPa, respectively) and V_0 (79.8(1) and 80.2(3) Å³, respectively). The ambient phase was more compressible than the high-P phases, even though the fitted data points were within a narrow pressure region. Allan et al. [8] reported that phase V of KHCO_3 had $B_0 = 26.5(2.8)$ GPa ($B_0' = 5.2(6)$), which is consistent with the current results for the high-P RbHCO_3 phases; there are no data for high-P phase IV of KHCO_3 .

Fig. 4 shows that the unit cell volumes (per formula unit) of RbHCO_3 phase IV and V remain similar throughout the pressure range considered here. This result suggests that these two phases are energetically very close, which may lead to non-unique phase transitions and their coexistence. Although it was difficult to judge which of the two high-P phases

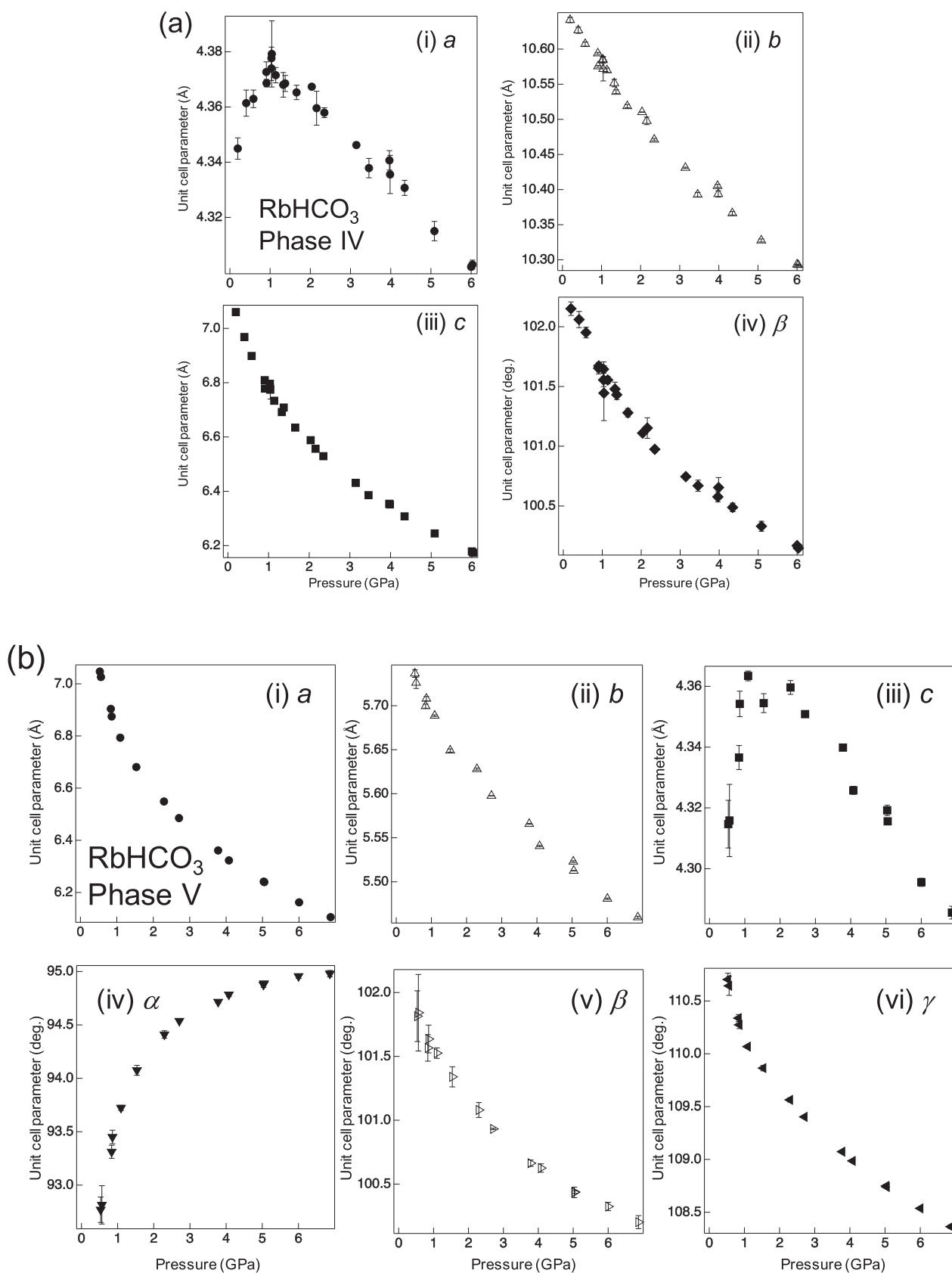


Fig. 5. Pressure dependence of unit cell parameters obtained by powder XRD (a) for high-P phase IV of RbHCO₃ (i) *a*, (ii) *b*, (iii) *c*, and (iv) β and (b) for high-P phase V of RbHCO₃ (i) *a*, (ii) *b*, (iii) *c*, and angles (iv) α , (v) β , and (vi) γ .

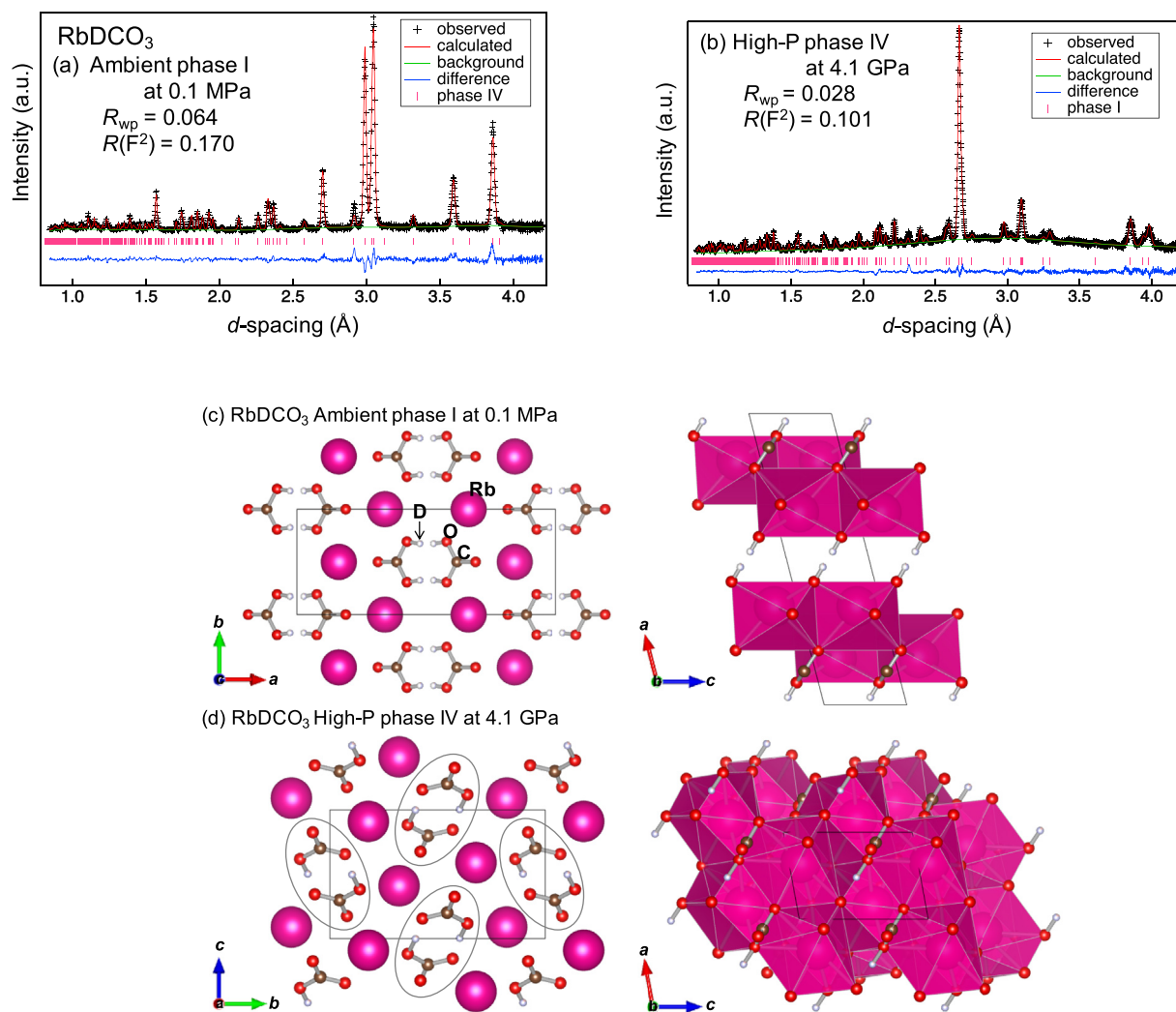


Fig. 6. Neutron diffraction patterns of RbDCO_3 (a) ambient phase I at 0.1 MPa and (b) high-P phase IV refined at 4.1 GPa. “+” denotes the observed data points; the solid line red denotes the calculated profile. The difference between the observed (black +) and the calculated (red) profiles is shown at the bottom of each plot. Tick marks below the pattern show the positions of allowed diffraction peaks for the corresponding phases. Crystal structures of (c) ambient phase I and (d) high-P phase IV drawn using VESTA by Momma and Izumi [21]. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

was thermodynamically more stable, the phase transition from phase V to phase IV was observed frequently (Fig. 2c), whereas no reverse transition was observed. This result suggests that phase IV was more stable than phase V, which is consistent with the fact that CsHCO_3 is isostructural with phase IV even at ambient pressure.

The axial compression of the two high-P phases of RbHCO_3 showed unusual behavior. The a -axis of phase IV (Fig. 5a) and the c -axis of phase V (Fig. 5b) expanded with compression at low pressure. With further compression, both axes started to shrink from the maximum, whereas all the other axes showed only continuous monotonic decreases. The unusual behavior was observed in different axes in the two phases because their different space groups use different notation. However, in each structure, these axes were oriented in the same structural direction along the layers of stacked dimers. The a - and c -axes of each high-P phase can be exchanged via a transformation matrix. These unusual axial behaviors may be related to structural changes in Rb–O polyhedra, the ordered dimer configuration, hydrogen bonding geometry, and the repulsion of Rb^+ in each structure, even after completing the phase transition (discussed later in Section 3.1.3).

3.1.3. Hydrogen bonding in high-P phase IV: Powder neutron diffraction measurements

Powder neutron diffraction at ambient conditions confirmed the synthesis of deuterated RbDCO_3 with a D:H occupancy ratio of approximately 4:1. Fig. 6a–b shows representative diffraction patterns of ambient phase I at 0.1 MPa and high-P phase IV at 4.1 GPa, respectively. Their crystal structures including deuterium positions were refined by Rietveld analysis (Fig. 6c–d). Table 3 lists the crystallographic data at each pressure. The neutron experiments consistently found phase IV as a high-P phase even under different conditions, such as using pellet or powdered samples, the amount of pressure medium, compression speed, and heating the sample to 80 °C to anneal the internal stress.

Fig. 7 shows the pressure dependence of the distance between Rb^+ and a neighboring O atom ($d(\text{Rb}-\text{O})$). One Rb^+ was coordinated to eight oxygen atoms from six HCO_3^- anions in ambient phase I, and $d(\text{Rb}-\text{O})$ was 2.873(10)–3.067(3) Å. However, in high-P phase IV of RbDCO_3 , $d(\text{Rb}-\text{O})$ varied widely between 2.872(9) and 3.483(8) Å at 0.2 GPa just after the phase transition, indicating that the Rb–O polyhedra were distorted if Rb^+ coordinated to 10 oxygen atoms. This phase IV at 0.2 GPa has still more stable Rb–O polyhedra with 9 coordinates rather than 10. The

Table 3
Crystallographic data for RbDCO₃ obtained by neutron diffraction.

Pressure (GPa)	0	0.04	0.15	0.58	1.32	2.17	3.06	4.11
Phase	I	I	IV	IV	IV	IV	IV	IV
<i>a</i> (Å)	14.8221(8)	14.4527(7)	4.3653(3)	4.3849(2)	4.3828(2)	4.3710(2)	4.3485(2)	4.32961(19)
<i>b</i> (Å)	5.8289(3)	5.8097(2)	10.6536(5)	10.6330(4)	10.5733(4)	10.5116(4)	10.4337(5)	10.3730(4)
<i>c</i> (Å)	4.0337(2)	4.0796(2)	6.9947(3)	6.8604(3)	6.6922(6)	6.5491(2)	6.4224(2)	6.3106(2)
α (°)	90	90	90	90	90	90	90	90
β (°)	104.384(4)	103.931(3)	102.040(3)	101.730(3)	101.334(3)	100.968(3)	100.690(3)	100.409(3)
γ (°)	90	90	90	90	90	90	90	90
<i>V</i> (Å ³)	337.57(3)	332.47(3)	318.15(3)	313.18(2)	304.07(2)	295.41(2)	286.34(2)	278.75(2)
Rb								
<i>x</i>	0.6637(4)	0.6627(3)	0.1522(12)	0.1491(9)	0.1432(9)	0.1493(9)	0.1517(7)	0.1530(8)
<i>y</i>	0	0	0.6741(5)	0.6727(3)	0.6736(3)	0.6760(3)	0.6764(3)	0.6792(3)
<i>z</i>	0.2945(15)	0.3022(9)	0.5776(7)	0.5796(6)	0.5826(6)	0.5874(6)	0.5888(5)	0.5898(6)
<i>U</i> _{iso} (× 100 Å ²)	2.9(2)	2.45(10)	3.26(11)	1.85(10)	1.51(10)	1.99(8)	1.16(7)	1.25(8)
C								
<i>x</i>	0.6143(5)	0.6145(3)	0.3643(12)	0.3715(9)	0.3770(9)	0.3768(10)	0.3761(7)	0.3802(9)
<i>y</i>	0.5	0.5	0.5272(5)	0.5473(3)	0.5458(3)	0.5455(3)	0.5454(3)	0.5445(3)
<i>z</i>	0.8531(16)	0.8687(10)	0.1885(9)	0.1969(5)	0.1968(6)	0.1975(6)	0.1977(5)	0.2008(5)
<i>U</i> _{iso} (× 100 Å ²)	2.2(2)	2.05(10)	4.24(14)	1.45(10)	1.19(10)	1.78(9)	0.87(8)	0.77(9)
O1								
<i>x</i>	0.6872(5)	0.6819(3)	0.6047(13)	0.6097(10)	0.6152(10)	0.6148(10)	0.6170(9)	0.6144(11)
<i>y</i>	0.5	0.5	0.5788(4)	0.5802(4)	0.5812(4)	0.5810(3)	0.5802(3)	0.5796(4)
<i>z</i>	1.094(2)	1.1033(12)	0.3168(10)	0.3134(8)	0.3224(7)	0.3208(8)	0.3210(6)	0.3254(7)
<i>U</i> _{iso} (× 100 Å ²)	2.94(15)	2.41(6)	2.91(6)	2.05(7)	1.72(6)	1.96(6)	1.02(5)	1.11(5)
O2								
<i>x</i>	0.5810(5)	0.5765(3)	0.2895(14)	0.2861(11)	0.2879(10)	0.2918(10)	0.2994(8)	0.3055(10)
<i>y</i>	0.3080(10)	0.3076(5)	0.4307(5)	0.4307(4)	0.4313(4)	0.4294(4)	0.4305(3)	0.4293(4)
<i>z</i>	0.7441(17)	0.7366(9)	0.1645(9)	0.1667(7)	0.1620(7)	0.1562(8)	0.1586(6)	0.1539(8)
<i>U</i> _{iso} (× 100 Å ²)	2.94(15)	2.41(6)	2.91(6)	2.05(8)	1.72(6)	1.96(6)	1.02(5)	1.11(5)
O3								
<i>x</i>			0.1727(16)	0.1800(12)	0.1824(11)	0.1765(13)	0.1803(10)	0.1771(12)
<i>y</i>			0.6342(4)	0.6346(3)	0.6352(4)	0.6381(4)	0.6364(3)	0.6383(4)
<i>z</i>			0.0871(11)	0.1003(8)	0.1063(8)	0.1050(8)	0.1130(6)	0.1119(7)
<i>U</i> _{iso} (× 100 Å ²)			2.91(6)	2.05(8)	1.72(6)	1.96(6)	1.02(5)	1.11(5)
D								
<i>x</i>	0.5230(12)	0.5133(12)	−0.035(3)	−0.0187(19)	−0.0152(17)	−0.0135(15)	−0.0258(12)	−0.0237(15)
<i>y</i>	0.3234(13)	0.3237(10)	0.5924(9)	0.5926(6)	0.5924(6)	0.5929(6)	0.5958(5)	0.5983(5)
<i>z</i>	0.589(4)	0.585(3)	−0.0223(19)	−0.0112(14)	0.0017(11)	0.0047(10)	0.0043(8)	−0.0003(9)
<i>U</i> _{iso} (× 100 Å ²)	1.7(5)	5.7(3)	4.00(5)	1.8(4)	3.0(4)	3.1(3)	3.3(3)	2.96(19)
<i>F</i> (D)	0.424(8)	0.416(5)	0.664(6)	0.679(9)	0.746(11)	0.755(9)	0.784(7)	0.801(15)
<i>F</i> (H)	0.076(8)	0.084(5)	0.336(6)	0.321(9)	0.254(11)	0.245(9)	0.216(7)	0.199(15)
<i>R</i> _p	0.064	0.030	0.028	0.026	0.026	0.026	0.023	0.028
<i>R</i> _{wp}	0.059	0.030	0.028	0.028	0.029	0.027	0.024	0.027
<i>R</i> (<i>F</i> ²)	0.170	0.175	0.166	0.152	0.149	0.201	0.107	0.101
<i>N</i> _{obs}	358	367	641	590	577	591	552	538
Hydrogen bond								
<i>d</i> (O–D) (Å)	0.934(14)	0.977(14)	1.143(16)	1.128(8)	1.098(7)	1.097(9)	1.112(6)	1.099(7)
<i>d</i> (D···O) (Å)	1.778(19)	1.610(17)	1.355(17)	1.437(8)	1.476(7)	1.473(8)	1.458(6)	1.443(6)
<i>d</i> (O···O) (Å)	2.701(15)	2.561(9)	2.492(14)	2.548(7)	2.552(7)	2.552(9)	2.556(6)	2.531(7)
angle(O–D···O) (°)	166.(4)	163.4(13)	172.1(13)	166.5(7)	164.9(7)	166.4(8)	167.9(5)	169.1(6)
<i>d</i> (Rb–O) (Å)								
Rb1–O1	2.873(10)	2.882(6)	2.872(9)	2.853(6)	2.785(6)	2.811(7)	2.808(5)	2.808(6)
Rb1–O1	3.012(8)	3.0464(16)	2.933(6)	2.928(6)	2.918(5)	2.905(6)	2.881(4)	2.883(5)
Rb1–O1	3.0669(27)	3.0464(16)	3.125(7)	3.101(6)	3.065(6)	3.001(6)	2.963(4)	2.931(5)
Rb1–O1	3.0669(27)	3.093(5)	3.149(7)	3.144(6)	3.111(6)	3.106(7)	3.058(5)	3.008(6)
Rb1–O2	2.881(8)	2.947(5)	2.935(7)	2.936(6)	2.948(6)	2.905(6)	2.852(5)	2.830(6)
Rb1–O2	2.881(8)	2.947(5)	3.109(7)	3.038(5)	2.998(5)	2.968(6)	2.984(5)	2.997(6)
Rb1–O2	3.019(7)	2.993(4)	3.257(7)	3.265(6)	3.224(6)	3.183(7)	3.119(5)	3.038(6)
Rb1–O2	3.019(7)	2.993(4)	4.021(7)	3.962(6)	3.948(6)	3.931(8)	3.909(5)	3.922(5)
Rb1–O2(O3)	3.986(10)	3.971(6)	2.927(7)	2.926(6)	2.885(7)	2.862(8)	2.857(5)	2.820(6)
Rb1–O2(O3)	3.986(10)	3.971(6)	3.050(7)	3.082(6)	3.091(6)	3.044(7)	2.999(5)	2.939(6)
Rb1–O3			3.483(8)	3.343(6)	3.251(7)	3.192(8)	3.109(5)	3.066(6)
Rb1–O3			3.565(9)	3.570(7)	3.499(7)	3.413(8)	3.372(5)	3.305(6)
Average (Å)	2.977(13)	2.993(8)	3.084(7)	3.062(6)	3.028(6)	2.998(7)	2.963(5)	2.932(6)

Note: Errors in calculated pressures are within ±0.1 GPa. *U*_{iso}, isotropic atomic displacement parameters; *F*, site occupancy; *R*_{wp}, *R*_p and *R*(*F*²), reliability factors; *N*_{obs}, total number of observations. Average Rb–O distances were calculated for eight (ambient phase I) and 10 (high-P phase IV) coordinates.

distance between Rb and the 10th coordinated oxygen (Rb–O3 in Table 3) for phase IV is drastically decreasing compared to other shorter Rb–O distances. Above 0.6 GPa, the coordination number of 10 is getting more stable with less variation in *d*(Rb–O) as the pressure increased. This gradual increase in the coordination from 9 to 10 might be caused by a rearrangement of Rb–O polyhedra to diminish the structural distortion, which also accompanies the unusual increase and decrease in the *a*-axis

of phase IV (and the *c*-axis of phase V) as described above (Section 3.1.2). This suggests that complementary changes in all of the unit cell parameters result in the monotonous compression of volume for the two high-P phases shown in Fig. 4.

At 4.1 GPa, Rb⁺ was more effectively coordinated to 10 oxygen atoms with *d*(Rb–O) ranging from 2.808(6) to 3.066(6) Å. The average *d*(Rb–O) did not change substantially between ambient phase I and high-P phase

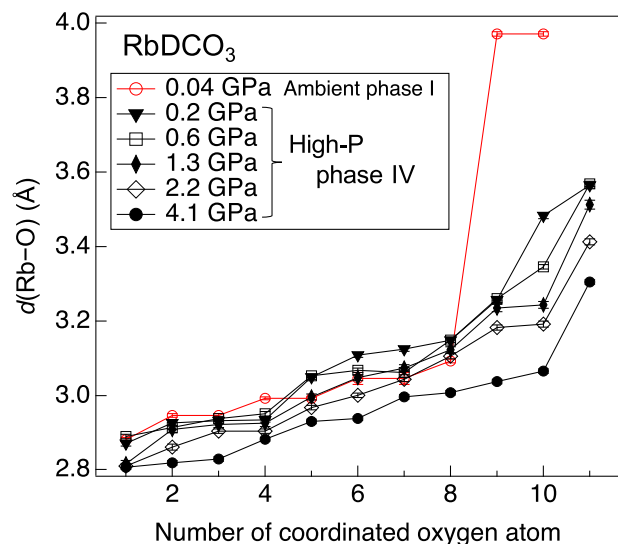


Fig. 7. Change in Rb–O distance of RbDCO₃ under high pressure.

IV at 4.1 GPa, despite the increase in coordination number (Table 3). This result agreed well with the increase in coordination number and the unchanging K–O distance in high-P phase V of KDCO₃ reported previously by Allan et al. [8]. Thus, the local maximum for the *a*-axis at ~1 GPa in Fig. 5a possibly resulted from the change in the configuration of the ordered (HCO₃⁻)₂ dimer and rearrangement of the Rb⁺ cations along this specific axis in high-P phase IV of RbDCO₃.

Fig. 8 depicts the pressure dependence of the O–D, D···O, and O···O distances and the O–D···O angle of hydrogen bonding in high-P phase IV of RbDCO₃. The results under ambient conditions agreed well with those of Larvor and Stöger [10]. There are no comparable data for high-P phase IV of KHCO₃, but data for high-P phase V of KDCO₃ [8] are also plotted in Fig. 8. The O···O distance in high-P phase IV of RbDCO₃ did not decrease, similar to that in high-P phase V of KDCO₃ (Fig. 8a), with no discontinuity around the phase transition at 0.2 GPa. The O–D distance became longer than that of ambient phase I just after the phase transition, and then remained mostly unchanged as the pressure increased further. Conversely, the D···O distance became shorter, and then did not change greatly or decreased slightly above ~1 GPa (Fig. 8b and c). The O–D···O angle of RbDCO₃ also showed no notable change at the phase transition, and then gradually increased after a local minimum at ~1 GPa; however, Allan et al. [8] reported a discontinuity for high-P phase V of KDCO₃ (Fig. 8d).

Jeffery [20] described the strength of hydrogen bonding in terms of bond lengths, angles, and other criteria. Strong hydrogen bonds are generally considered to have an O(H)···O distance of 2.2–2.55 Å and an O–H···O angle of 175–180°; longer distances and angles deviating further from linear (180°) denote weaker hydrogen bonds. KHCO₃ has moderately strong hydrogen bonds with short O–H···O distances of ~2.6 Å even at ambient pressure [5]. The O–D···O angle in RbDCO₃ remained almost constant around 165°–170° after the phase transition (Fig. 8d). High-P phase IV of RbDCO₃ had an ordered configuration of the (DCO₃⁻)₂ dimers, with longer O–D and shorter D···O distances than the ambient phase (Fig. 8b and c), indicating that deuterium atoms gradually moved from the donor O to the acceptor O with increasing pressure. However, the relatively short O···O distances at ~2.55 Å for ambient phase I and high-P phase IV (Fig. 8a) suggested moderately strong hydrogen bonding. Overall, the geometry of hydrogen bonding in the dimer did not change, and thus might not trigger the phase transition, although the originally disordered dimer configuration spontaneously becomes ordered.

After the phase transition, the parameters (except for the O···O

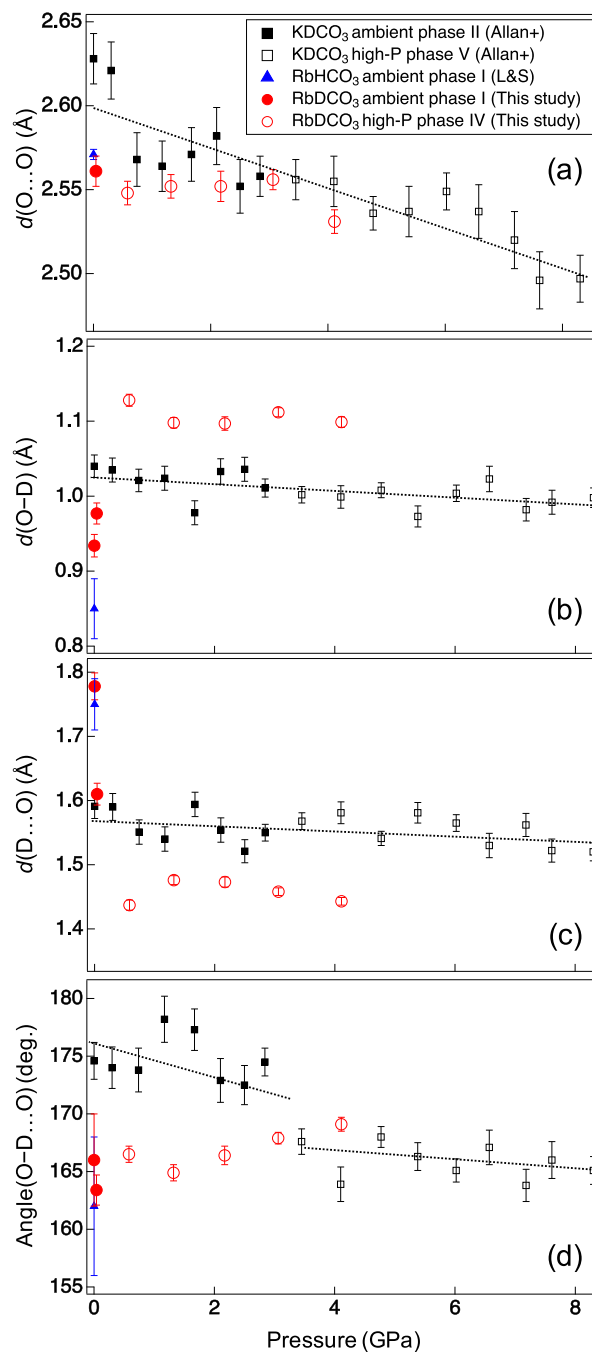


Fig. 8. Parameters of hydrogen bonding in RbDCO₃ vs. pressure: distances (a) O···O, (b) O–D, (c) D···O, and (d) angle O–D···O. Data for high-P phase V KDCO₃ are from Allan et al. [8] and those for ambient phase I of RbHCO₃ are from Larvor and Stöger [10]. The data points for 0.2 GPa just after the phase transition are not plotted because of the coexistence of ambient and high-P phases.

distance) showed anomalous changes with a local maximum (or minimum) at ~1 GPa, which was strongly related to the unique compression behavior of the *a*-axis in phase IV (Fig. 5a). Rb⁺ cations in the crystal structure were rearranged to relax the Rb–Rb repulsion as the coordination number gradually increased. The simultaneous reconfiguration of the dimers and hydrogen bonding may allow the hydrogen atoms to occupy more stable locations in the ordered dimers to enhance the geometrical stability of high-P phase IV.

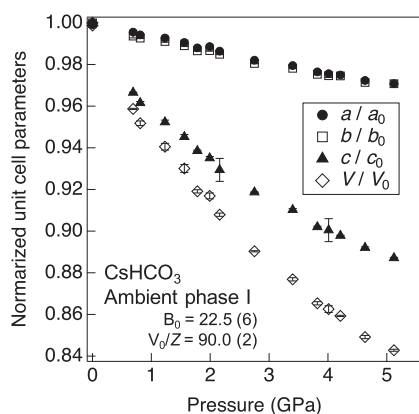


Fig. 9. Compressibility of unit cell parameters of CsHCO₃, ratios a/a_0 , b/b_0 , c/c_0 , and V/V_0 , calculated from powder XRD results. The a_0 , b_0 , c_0 and V_0 are values at ambient condition.

3.2. CsHCO₃

3.2.1. Raman spectra

The Raman spectra of CsHCO₃ (Supplementary Fig. 1a) were similar to those of RbHCO₃, and all the peaks shifted monotonically to higher frequency with increasing pressure (Supplementary Fig. 1b). Unlike RbHCO₃, there was no discontinuity observed up to 5 GPa, suggesting that no phase transition occurred in this pressure region.

3.2.2. XRD

All reflections in the XRD patterns of CsHCO₃ (Supplementary Fig. 2) gradually shifted to higher angles under pressures up to 5 GPa, and they were all well explained by a structure similar to phase IV KHCO₃ or RbHCO₃. Therefore, the ambient phase of CsHCO₃ (designated here as phase I) was stable at least up to 5 GPa. The changes in volume and cell parameters are summarized in Fig. 9 and listed in Supplementary Table 1. The bulk modulus and zero-pressure volume obtained by fitting the equations of state were $B_0 = 22.5(6)$ GPa and $V_0 = 90.0(2)$ Å³ (Table 2).

All the axes of CsHCO₃ were compressed monotonically with no unusual expansions, unlike high-P phase IV of RbHCO₃ (Fig. 5a), despite them both having the same crystal structure. CsHCO₃ phase I which is isostructural to KHCO₃ and RbHCO₃ high-P phase IV, already exists stably at ambient condition.

4. Conclusions

The high-P behaviors of two alkali metal hydrogen carbonates, RbHCO₃ and CsHCO₃, were investigated and compared with previous results for KHCO₃. RbHCO₃ transformed into high-P phases at about 0.5 GPa, whereas no phase transition was found in CsHCO₃ up to 5 GPa. This demonstrated the effect of cation size on these compounds' high-P behaviors. Increasing the cation radius decreased the phase transition pressure, from ~3 GPa for KHCO₃ to ~0.5 GPa for RbHCO₃, with CsHCO₃ assuming a structure similar to the high-P form of KHCO₃ (monoclinic phase IV) even at ambient conditions. At high-P, phase IV (monoclinic) and phase V (triclinic) of RbHCO₃ with crystal structures analogous to high-P phases of KHCO₃ emerged. However, no thermodynamic factor was identified that determined which phase appeared and remained stable above the phase transition pressure. Although the volume and compression behavior of these two phases in RbHCO₃ were similar, a phase transition from phase V to phase IV or their coexistence was observed, but no reverse transition from phase IV to phase V was observed. Therefore, it is likely that phase IV is stable, while phase V is metastable. Deuterium positions in the high-P phase IV of RbDCO₃ were determined for the first time. In many ionic crystals, the relative size of the cation and anion greatly affects the compression behavior and

pressure-induced phase transitions. In this system, however, the disordered/ordered configuration and orientation of (HCO₃)₂ dimers, together with the cation size, are strongly involved in the phase transition. The properties and networks of hydrogen bonding inside the (HCO₃)₂ dimers did not drastically change upon phase transition.

Author contributions section

G.W., R.I.-O. and H.K. performed high-P experiments. R.I.-O., G.W. and K.K. analyzed the obtained data. G.W. prepared the synthesized samples. R.I.-O., T.Y. and H.K. wrote the manuscript.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.jssc.2019.121139>.

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