

PHYSICOCHEMICAL ANALYSIS
OF INORGANIC SYSTEMS

Phase Diagrams of Sections in the EuS–Cu₂S–Nd₂S₃ System

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Received July 7, 2010

Abstract—Phase equilibria in the EuS–Cu₂S–Nd₂S₃ system were studied in an isothermal (970 K) section and NdCuS₂–EuS and Cu₂S–EuNdCuS₃ polythermal sections. The complex sulfide EuNdCuS₃ has an orthorhombic crystal lattice (space group *Pnma*; *a* = 1.10438(2) nm, *b* = 0.40660(1) nm, *c* = 1.14149(4) nm), is isostructural to BaLaCuS₃, and melts incongruently at 1470 K: EuNdCuS₃ (0.50 EuS; 0.50 NdCuS₂) ⇌ 0.18 EuS ss (0.88 EuS; 0.12 NdCuS₂) + 0.82 L (0.415 EuS; 0.585 NdCuS₂); Δ*H* = 17.8 kJ/mol. Within the range 0.5 mol % EuS, EuNdCuS₃-based solid solutions were not found. At 970 K, the tie lines pass from the compound EuNdCuS₃ to Cu₂S, EuS, NdCuS₂, and EuNd₂S₄ phases and lie between the NdCuS₂ phase and solid solutions (ss) of γ-Nd₂S₃ with EuNd₂S₄. Eutectics are formed between the compounds NdCuS₂ and EuNdCuS₃ at 32.0 mol % EuS *T* = 1318 K and between the compounds Cu₂S and EuNdCuS₃ at 20.5 mol % EuNdCuS₃ and *T* = 1142 K. Five main subordinate triangles were identified in the system.

DOI: 10.1134/S0036023611040024

We failed to find any data on phase equilibria in the EuS–Cu₂S–Nd₂S₃ ternary system. The Cu₂S–Nd₂S₃ system forms a complex sulfide NdCuS₂, which melts incongruently at 1465 K [1]. A eutectic between Cu₂S and NdCuS₂ phases is formed at 17 mol % Nd₂S₃ and *T* = 1267 K. The Nd₂S₃–EuS system forms a complex compound EuNd₂S₄ [2, 3], which melts incongruently at 2430 K [4]. A continuous solid solution having a Th₃P₄ type structure is formed between γ-Nd₂S₃ and EuNd₂S₄. A eutectic between the phases EuNd₂S₄ and EuS is formed at 66.5 mol % EuS and *T* = 2290 K. No new compounds were found in the Cu₂S–EuS system. The composition of a eutectic is 24.5 mol % EuS and *T* = 1069 K [5].

A study of phase equilibria in the EuS–Cu₂S–Nd₂S₃ system is topical because a combination of sulfides of *d* and *4f* elements gives new compounds and the information contained in the phase diagrams serves as the basis for determining their synthesis conditions.

The purpose of this work was to investigate phase equilibria in the EuS–Cu₂S–Nd₂S₃ system in an isothermal (970 K) section and polythermal sections and determine the composition and structural characteristics of a new complex sulfide.

EXPERIMENTAL

The compound Cu₂S was produced from the constituent elements (copper of 11-4 high-purity grade and sulfur of 15-3 high-purity grade) in sealed evacuated double-walled quartz ampoules. The sulfides EuS and Nd₂S₃ were synthesized from oxides of the grades

“EvO-Zh” and “NO-Zh”, respectively, in a flow of H₂S and CS₂ at 1300 K [6].

In the EuS–Cu₂S–Nd₂S₃ system, 70 samples the compositions of which fell inside the composition triangle were synthesized from the initial sulfides Cu₂S, EuS, and Nd₂S₃. Mixtures of oxides were alloyed according to published procedures [6]. The samples were annealed at 970 K for 3000 h in sealed evacuated quartz ampoules. Then, the samples were kept for 0.5 h at 1770 K in an open reactor while inductively heating a graphite crucible and, after that, annealed for 3 h at 1450 K in evacuated double-walled quartz ampoules in an electrically heated furnace. The results of microstructural analysis, X-ray powder diffraction, and differential scanning calorimetry of the samples during annealing suggest that they have reached equilibrium.

Thermal analysis was performed on a Setsys Evolution 1750 (TGA-DSC 1600) thermal analysis setup according to previously developed procedures using the SETSOFT 2000 program package [7]. Overlapping peaks were resolved using the Thermogram Analyzer program. Visual polythermal analysis was carried out with accuracy precision of 1%. Microstructural analysis was made with a METAM RV-22 microscope. The hardness was measured with a PMT-3M meter by the Vickers method with a precision of 5–7%. The graphical representation was made using the Edstate 2D and Edstate 3D software. X-ray powder diffraction data were obtained on a Dron-7 diffractometer and a PANalytical X'Pert PRO diffractometer equipped with a PIXcel detector (CoK_α radiation, 10° ≤ 2θ ≤ 120°). The EuNdCuS₃ lattice parameters were

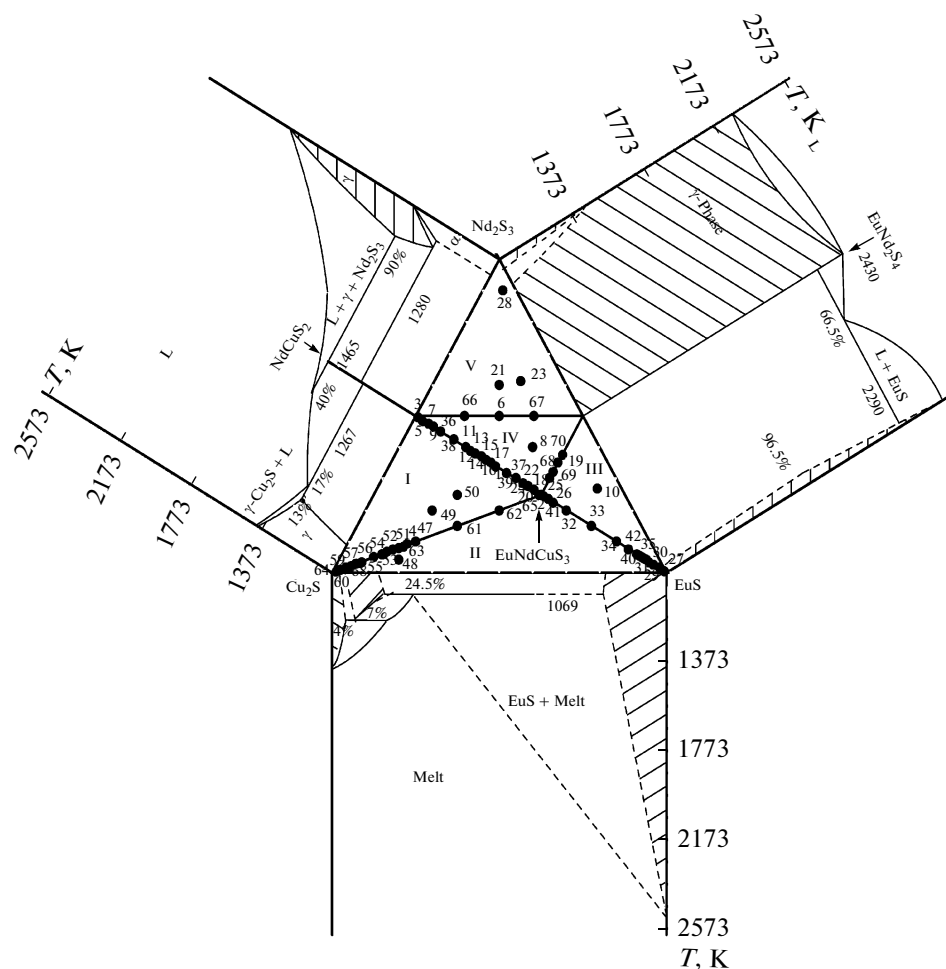


Fig. 1. Positions of tie lines in the $\text{EuS}-\text{Cu}_2\text{S}-\text{Nd}_2\text{S}_3$ system at 970 K. Dots represent studied samples; the Roman numerals, main subordinate triangles.

determined using the ITO program [8]. The EuNdCuS_3 crystal structure was refined by the derivative difference minimization method [9] with the confidence factors $R\text{-DDM} = 8.49\%$ and $R_B = 4.6\%$. Data on the isostructural compound BaLaCuS_3 were used as the initial model [10, 11].

RESULTS AND DISCUSSION

In the $\text{EuS}-\text{Cu}_2\text{S}-\text{Nd}_2\text{S}_3$ system at the EuS to Cu_2S to Nd_2S_3 ratio of 2 : 1 : 1, a complex sulfide EuNdCuS_3 forms. The compound is isostructural to BaLaCuS_3 and has an orthorhombic crystal lattice (space group $Pnma$) with the unit cell parameters $a = 1.10438(2)$ nm, $b = 0.40660(1)$ nm, and $c = 1.14149(4)$ nm. Multi-structural analysis and X-ray powder diffraction showed that EuNdCuS_3 is in equilibrium with Cu_2S , EuS , NdCuS_2 , and EuNd_2S_4 , which allows one to determine the positions of tie lines at 970 K (Fig. 1). There is also equilibrium between the NdCuS_2 phase and solid solutions of $\gamma\text{-Nd}_2\text{S}_3$ with EuNd_2S_4 having a Th_3P_4 type structure. Five main subordinate triangles

were identified in the system (Fig. 1): $\text{NdCuS}_2-\text{EuNdCuS}_3-\text{Cu}_2\text{S}$ (I), $\text{Cu}_2\text{S}-\text{EuNdCuS}_3-\text{EuS}$ (II), $\text{EuS}-\text{EuNdCuS}_3-\text{EuNd}_2\text{S}_4$ (III), $\text{NdCuS}_2-\text{EuNdCuS}_3-\text{EuNd}_2\text{S}_4$ (IV), and $\text{NdCuS}_2-\text{Nd}_2\text{S}_3-\text{EuNd}_2\text{S}_4$ (V).

The compound EuNdCuS_3 is in equilibrium with NdCuS_2 and EuS phases. The phase diagram of the $\text{NdCuS}_2-\text{EuS}$ system has been constructed for the first time (Fig. 2a).

Crystals of the complex sulfide EuNdCuS_3 ($1\text{NdCuS}_2 : 1\text{EuS}$) in the microstructural analysis are gray-brown, and $H = 2320$ MPa ($P = 0.02$ kg). The compound melts incongruently. The average onset temperature of the phase-transformation peak is 1470 K. The heat of melting of the compound is 17.8 kJ/mol. The incongruent melting tie line touches the EuS -based solid solution and the liquid, which enables one to write a thermochemical equation of phase transformation (table).

No homogeneity regions based on the compounds NdCuS_2 and EuNdCuS_3 were found. According to X-ray powder diffraction and microstructural analysis,

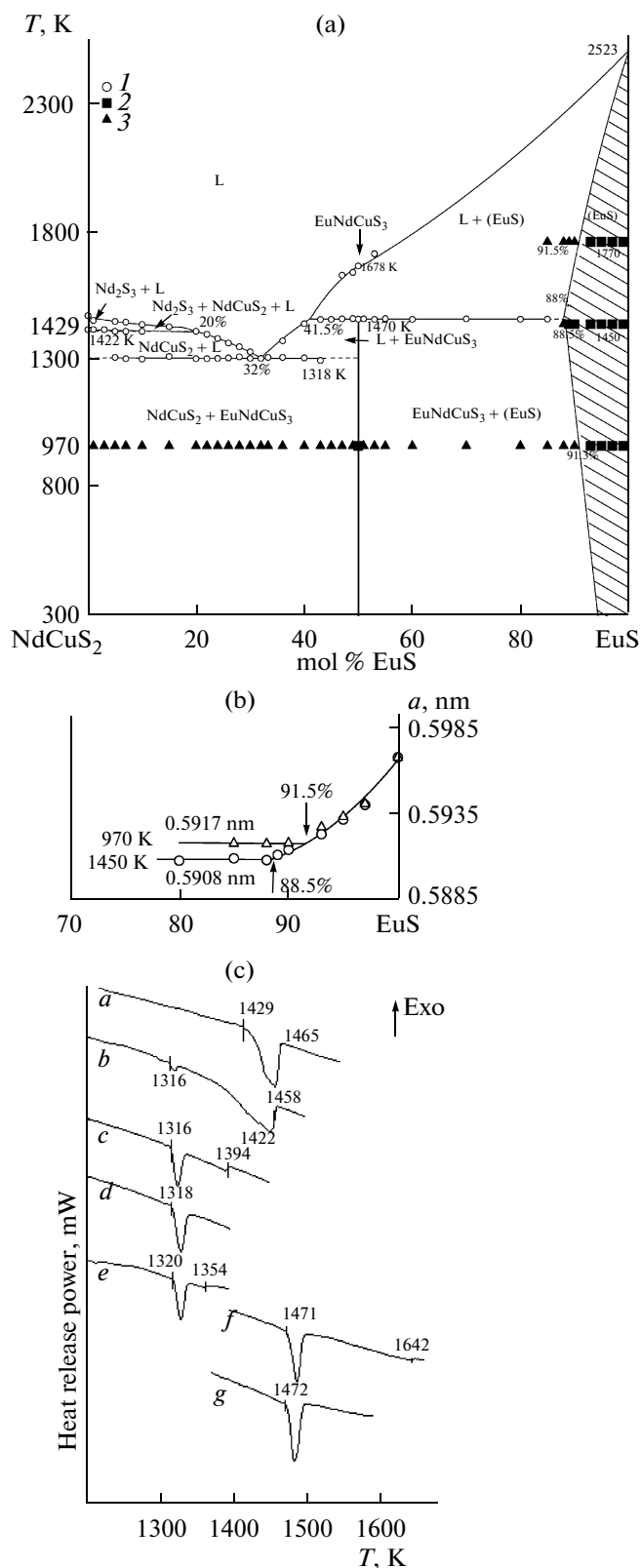


Fig. 2. (a) Phase diagram of the NdCu₂-EuS system: (1) DSC data; the states of samples according to X-ray powder diffraction and microstructural analysis: (2) single-phase and (3) two-phase. (b) Variations in the parameters of the NaCl-type unit cell in the EuS ss region. (c) DTA events for samples containing (a) 1.0, (b) 7.0, (c) 24.0, (d) 26.0, (e) 33.3, (f) 47.0, and (g) 55.0 mol % EuS.

Table

Type of phase transformation	Incongruent melting of compound		Phase transformation equation	ΔH_m , J/g, kJ/mol
	composition	T, K		
Incongruent melting of compound	EuNdCuS ₃ (1NdCuS ₂ : 1EuS)	1470	EuNdCuS ₃ (solid) (0.50 EuS; 0.50 NdCuS ₂) \rightleftharpoons 0.18 ss EuS (0.88 EuS; 0.12 NdCuS ₂) + 0.82 L (0.415 EuS; 0.585 NdCuS ₂)	39 17.8
Melting of eutectic in the NdCuS ₂ –EuS system	32.0 mol % EuS	1318	0.36 NdCuS ₂ (solid) + 0.64 EuNdCuS ₃ (0.50 EuS; 0.50 NdCuS ₂) \rightleftharpoons L (0.32 EuS; 0.68 NdCuS ₂)	22
Incongruent melting of compound	NdCuS ₂ (1Cu ₂ S : 1Nd ₂ S ₃)	1429	NdCuS ₂ (solid) (0.50 Nd ₂ S ₃ ; 0.50 Cu ₂ S) \rightleftharpoons 0.80 L (0.40 Nd ₂ S ₃ ; 0.60 Cu ₂ S) + 0.20 ss γ -Nd ₂ S ₃ (0.90 Nd ₂ S ₃ ; 0.10 Cu ₂ S)	51 13.9
Melting of eutectic in the Cu ₂ S–EuNdCuS ₃ system	20.5 mol % EuNdCuS ₃	1142	0.87 ss Cu ₂ S (0.085 EuNdCuS ₃ ; 0.915 Cu ₂ S) + 0.13 EuNdCuS ₃ (solid) \rightleftharpoons L (0.205 EuNdCuS ₃ ; 0.795 Cu ₂ S)	12

samples containing 1.0, 3.0, 47.0, 49.0, 51.0, and 53.0 mol % EuS comprise two phases; the amount of a second phase corresponds to the position of the sample in the diagram. The changes in the unit cell parameters of two-phase samples annealed at 970 K relative to homogeneous samples fall within the measurement errors.

A temperature-dependent region of EuS-based solid solution is formed (Fig. 2b). Within the homogeneity range, the parameter a decreases from 0.5967 to 0.5908 nm at 1450 K and to 0.5917 nm at 970 K, which agrees with the value of the reduced cation radius: $r(\text{Cu}^+, \text{Nd}^{3+}) = (0.0600 + 0.0.1109)/2 = 0.0855$ nm [12]. The negative deviation from Vegard's rule suggests that the interaction between the components of the EuS matrix is weaker than the interaction with the doping components. Using the dependence of the parameter a on the composition and the emergence of a second phase in the samples, we determined the positions of solidus points (1770 K, 91.5 mol % EuS) and solvus points (1450 K, 88.5 mol % EuS and 970 K, 91.5 mol % EuS).

The equation of the reaction of incongruent decomposition of NdCuS₂ was composed based on the phase diagram of the Cu₂S–Nd₂S₃ system [1]. The heat of incongruent melting of NdCuS₂ was found to be 13.9 kJ/mol (table). The heat of melting of Cu₂S is 11.296 ± 0.209 kJ/mol [13]. The enthalpy of melting of NdS_{1.37} is 45.0 kJ/mol [14]. The heat of melting of γ -Nd₂S₃ might be expected to be of the same order. The similarity of the heats of melting of NdCuS₂ and Cu₂S agrees with the formation of 0.20 moles of crystalline solid solution of γ -Nd₂S₃ in the course of the incongruent melting.

Within the range 0–50 mol % EuS, a eutectic between the phases NdCuS₂ and EuNdCuS₃ is formed. The eutectic temperature was found by averaging the temperatures for 15 samples of various compositions and was taken to be 1318 K (Fig. 2c). The composition of the eutectic according to the microstructural analy-

sis data and the data obtained by constructing the Tammann triangle is 32 mol % EuS. According to DSC data, the heat is 22 J/g (table). In the NdCuS₂–eutectic region, the eutectic mixture on polished sections of samples is represented by alternating oval crystals of sulfide phases 10–20 μm in size. In the eutectic–EuNdCuS₃ region, eutectic grains of conjugate phases are also oval, but their colors are similar and interfaces are diffuse even on etching.

The liquidus line in the NdCuS₂–eutectic region consists of two branches which were constructed by fitting the DSC data by second-order polynomials. The branch of the liquidus line that corresponds to the primary crystallization of γ -Nd₂S₃ solid solution grains 3 touches the NdCuS₂ incongruent melting surface. The coordinates of the point of touch are ~20 mol % EuS and $T = 1422$ K.

Between the Nd₂S₃ + liquid and NdCuS₂ + liquid fields, there is the Nd₂S₃ + NdCuS₂ + liquid field (outlined by dashed line). We constructed the side of the Tammann triangle that represents the dependence of the area of the NdCuS₂ incongruent melting peak on the molar composition for samples containing 0.0–0.15 mol % EuS. At 0.0 mol % EuS, the peak area is maximal. The obtained heat value (13.9 kJ/mol) coincides with the heat of incongruent melting of NdCuS₂ (table).

Within the range 50–100 mol % EuS at temperatures below the EuNdCuS₃ incongruent melting temperature, EuNdCuS₃ and a EuS-based solid solution are in equilibrium. The reflections of these phases were only detected in the X-ray diffraction patterns of the samples annealed at 970 K. On polished sections, there are brown oval EuS grains ($H = 1300$ MPa) 5×10 to 50×70 μm in size, located inside the field of the EuNdCuS₃ phase ($H = 2320$ MPa). The microstructure of the samples cooled from melt is formed by primary oval EuS grains located inside the field of the EuNdCuS₃ phase, and some areas include regions of a eutectic between the EuNdCuS₃ and NdCuS₂ phases.

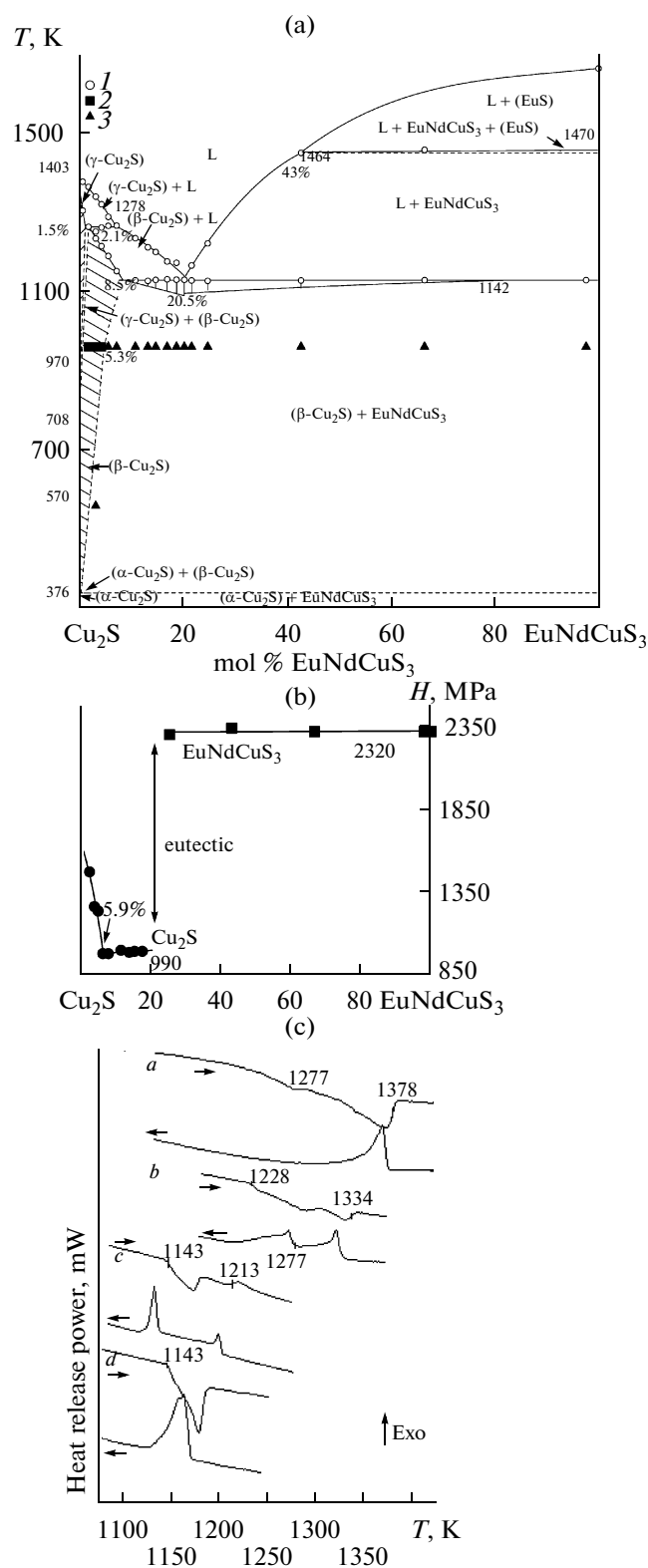


Fig. 3. (a) Phase diagram of the Cu_2S – EuNdCuS_3 system: (1) DSC data; the states of samples according to X-ray powder diffraction and microstructural analysis: (2) single-phase and (3) two-phase. (b) Microhardness versus composition diagram. (c) DTA events for samples containing (a) 2.1, (b) 4.6, (c) 15.0, and (d) 20.5 mol % EuNdCuS_3 .

The microstructural analysis of quenched and annealed samples confirmed the incongruent melting of EuNdCuS_3 .

The thermoanalytical curves of annealed samples containing 43.0–85.0 mol % EuS have a peak of EuNdCuS_3 incongruent melting (Fig. 2c). The average temperature is 1470 ± 2 K, which coincides with the average incongruent melting temperature of EuNdCuS_3 . Differential scanning calorimetry gave the melt-transition temperatures for samples containing up to 55.0 mol % EuS . The thermogravimetric data at $T > 1740$ K show weight loss caused probably by thermal dissociation. The branch of the liquidus line was constructed using the data on the EuS melting point (2523 K [15]).

The phase diagram of the Cu_2S – EuNdCuS_3 system is of the eutectic type and is characterized by the presence of an unclosed region of solid solution based on β - Cu_2S and α - Cu_2S and a closed region of solid solution based on γ - Cu_2S (Fig. 3a).

The region of β - Cu_2S based solid solution has a polygonal shape, the solubility in the solid state is temperature dependent, and the solid solution decomposes incongruently. The onset temperatures of heat absorption were determined from the differential thermal analysis curves for samples containing 2.1–7.5 mol % EuNdCuS_3 (Fig. 3c). The solidus temperatures were fitted by a second-order polynomial. At the eutectic temperature 1142 K, the solidus is extrapolated to the composition 8.5 mol % EuNdCuS_3 . The peak temperature of the decomposition peak for the β - Cu_2S -based solid solution was detected to be at 1278 K. The peritectoid-point composition (2.1 mol % EuNdCuS_3) was determined by constructing the Tammann triangle and extrapolating the solidus line. The horizontal line of incongruent decomposition of the β - Cu_2S -based solid solution intersects the liquidus line at 7.5 mol % EuNdCuS_3 . In a sample containing 1 mol % EuNdCuS_3 , the onset temperature of heat absorption is 1318 K and corresponds to the solidus of γ - Cu_2S -based solid solution. The composition at the point of intersection of the horizontal line and the region of γ - Cu_2S -based solid solution was taken to be 1.5 mol % EuNdCuS_3 . We composed the equation of the incongruent decomposition of β - Cu_2S -based solid solution: $\beta\text{-Cu}_2\text{S ss (0.021 EuNdCuS}_3; 0.979 \text{ Cu}_2\text{S)} \rightleftharpoons 0.9 \gamma\text{-Cu}_2\text{S ss (0.015 EuNdCuS}_3; 0.985 \text{ Cu}_2\text{S)} + 0.1 \text{ L (0.075 EuNdCuS}_3; 0.925 \text{ Cu}_2\text{S)}$.

The β - and γ high-temperature phases of Cu_2S are not fixed by quenching [1]. Within the solid-solution region, the phase-transformation kinetics was observed. For samples annealed and quenched from 970 K, the reflections of the following phases were detected: α - $\text{Cu}_2\text{S ss}$ (1.0 mol % EuNdCuS_3); α - $\text{Cu}_2\text{S ss}$ and β - $\text{Cu}_2\text{S ss}$ (2.1, 3.5, and 4.6 mol %) with continuously increasing β - Cu_2S content; β - $\text{Cu}_2\text{S ss}$ (5.9 mol %); and β - $\text{Cu}_2\text{S ss}$ and EuNdCuS_3 (7.5–97.6 mol %). The

parameters of the hexagonal unit cell of β -Cu₂S are $a = 0.396$ nm, $c = 0.678$ nm [16]. Within the solid-solution region, there is scatter of experimental values for the Cu₂S unit cell parameters as functions of composition. For 5.9 mol % EuNdCuS₃, the unit cell parameters are $a = 0.395$ nm, $c = 0.674$ nm.

According to microstructural analysis, samples containing up to 4.6 mol % EuNdCuS₃ are homogeneous. In samples containing 5.9 and 7.5 mol % EuNdCuS₃, the field of the Cu₂S phase is pierced throughout its volume by needle-shaped intrusions of 10–100- μ m-long, 2–5- μ m-wide gray-brown crystals of the conjugate phase EuNdCuS₃; there is no eutectic. The shape, size, and distribution of grains of the EuNdCuS₃ phase suggest solid-phase decomposition of the primary β -Cu₂S solid solution. In an initially homogeneous sample (5.9 mol % EuNdCuS₃) annealed at 970 K, needle-shaped crystals of the EuNdCuS₃ phase appear, which is indicative of the temperature dependence of solubility in solid β -Cu₂S.

Within the homogeneity region, the Cu₂S microhardness decreases from 1470 to 990 MPa (Fig. 3b), which is indicative of incorporation of ions having a larger radius ($r(\text{Eu}^{2+}(\text{VII})) = 0.12$ nm [12]).

A eutectic is formed between β -Cu₂S ss and EuNdCuS₃ phases. The peak of melting of the eutectic has a pronounced linear portion and is detected at an average temperature of 1142 K. As the eutectic composition is approached, the sizes of Cu₂S primary yellow grains and EuNdCuS₃ gray-brown grains systematically decrease from 200×30 to 60×20 μ m ($H = 990$ MPa) and from 900×50 to 60×20 μ m ($H = 2320$ MPa). Crystals of the phases in the eutectic are 10×20 μ m in size. According to the Tammann triangle construction and microstructural analysis, the eutectic composition was taken to be 20.5 mol % EuNdCuS₃, with the heat of melting being 12 J/g. A phase transformation equation was composed (table).

Between the EuS + L and EuNdCuS₃ + L fields in the system under investigation, there should be a EuS + EuNdCuS₃ + L field (outlined by dashed line). DSC detected a weak decrease in the EuNdCuS₃ melting point from 1470 to 1464 K. The coordinates of the point of intersection of the liquidus line and the line of phase decomposition of the compound EuNdCuS₃ are 43.0 mol % EuNdCuS₃ and $T = 1464$ K.

In the EuNdCuS₃–EuNd₂S₄ system, EuNdCuS₃ and EuNd₂S₄ phases are in equilibrium at the isothermal-section temperature of 970 K. No change was detected in the unit cell parameter within the two-phase region relative to the individual compounds, which is indicative of the absence of reciprocal solid solutions. A eutectic is formed between the phases, and the melting peak was detected at 1467 K and a composition of $\sim(30.0 \pm 3.0)$ mol % EuNd₂S₄.

In the NdCuS₂–EuNd₂S₄ system at the isothermal-section temperature, the NdCuS₂ phase and the γ phase are in equilibrium. X-ray powder diffraction pattern showed no noticeable regions of homogeneity. No changes were detected in the unit cell parameter of the conjugate phases in the two-phase region. On polished sections, there are grains of the NdCuS₂ phase ($H = 3350$ MPa), located inside the fields of γ phase crystals ($H = 5520$ MPa).

ACKNOWLEDGMENTS

This work was supported by the Federal Target Program “Research and Research-Teaching Staff in Innovative Russia” for 2009–2013 (state contract nos. 6K/143-09 (P646) and NK-409/5 (P2263)).

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