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## Electronic transport in MgB<sub>2</sub>, AlB<sub>2</sub> and ZrB<sub>2</sub>—a comparative study

B. Fisher <sup>\*</sup>, K.B. Chashka, L. Patlagan, G.M. Reisner

*Physics Department and Crown Center for Superconductivity, Technion, Haifa 32000, Israel*

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### Abstract

We report on the temperature dependence of the resistivity ( $\rho$ ) and the absolute thermopower ( $S$ ) of the polycrystalline title materials and of AlB<sub>2</sub> single crystals. For all samples  $\rho(T)$  exhibits a Bloch–Grüneisen-like temperature dependence, with large characteristic temperatures  $\theta_R$  ( $\approx \theta_D$ —the Debye temperature). At high temperatures the thermopower  $S(T)$  for ZrB<sub>2</sub> (n-type) is almost the mirror image of  $S(T)$  for MgB<sub>2</sub> (p-type) while  $S(\text{AlB}_2)$  is very small for all temperatures. The density of states distribution  $N(E)$  around  $E_F$  seems to play a dominant role in determining  $S(T)$  of these materials.  $\ln(T)$  terms in the low-temperature  $\rho(T)$  and  $S(T)$  of ZrB<sub>2</sub> samples bear evidence for weak localization in 2D.

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### 1. Introduction

Since the discovery of superconductivity in MgB<sub>2</sub> [1], many studies of its normal state transport properties have been carried out. Experimental results [2–7] show that its resistivity  $\rho(T)$  exhibits a Bloch–Grüneisen-like (BG) temperature dependence typical for phonon scattering in a simple metal with a high Debye temperature, superimposed on a constant (residual) resistivity  $\rho_0$ . The textbook BG formula is [8,9]:

$$\Delta\rho(T) = \rho - \rho_0 = A \left( \frac{T}{\theta_R} \right)^5 J_5(\theta_R/T) \quad (1)$$

where  $\rho_0$  is the residual resistivity,  $A$  is a constant and  $\theta_R$  is a characteristic temperature, usually close to  $\theta_D$ —the Debye temperature deduced from specific heat;  $J_5 = \int_0^x z^5 dz / [(e^z - 1)(1 - e^{-z})]$  where  $x = T/\theta_R$ . In a generalized BG formula (BG( $n$ )) the power 5 and  $J_5$  are replaced by  $n$  and  $J_n$ . At low temperatures  $\Delta\rho(T) \propto T^n$ . For high quality MgB<sub>2</sub> samples (with low  $\rho_0$ )  $n$  is closer to 3 [3–7]. Therefore, in Refs. [3–5] the BG(3) formula was fitted to the experimental  $\rho(T)$ .  $\Delta\rho(T)$  expressed by the BG(3) formula may be associated with interband electron–phonon scattering [10]. The fitted  $\theta_R$  values for BG(3) are higher than those for BG(5) and also larger than most  $\theta_D$  values obtained from heat capacity measurements.

<sup>\*</sup> Corresponding author. Tel.: +972-4-8293652; fax: +972-4-8221514.

E-mail address: [phr06bf@physics.technion.ac.il](mailto:phr06bf@physics.technion.ac.il) (B. Fisher).

A number of studies were devoted to the thermopower of  $\text{MgB}_2$  [4,11–15]. The absolute thermopower ( $S$ ) of  $\text{MgB}_2$  is positive for all temperatures above  $T_c$  and increases quasilinearly with  $T$  in the range  $40 \leq T \leq 150$  K; the extrapolated value of  $S$  at  $T = 0$  has a small but finite negative value and above  $\sim 150$  K  $S$  becomes nonlinear and exhibits a tendency towards saturation. The quasilinear  $S(T)$  was analyzed in terms of diffusion thermopower ( $S_D$ ) dominated by holes; the negative intercept of  $S$  at  $T = 0$  was attributed to phonon drag [11,15] and the deviation from linearity at high temperature to electron-like states adding a negative contribution at high temperatures. In the earlier publications the linear portion of  $S(T)$  was interpreted in terms of Mott's formula for diffusion thermopower of a degenerate electron gas [8,9]:

$$S_D = -\frac{\pi^2 k_B^2 T}{3|e|} \left[ \frac{\partial \ln \sigma(E)}{\partial E} \right]_{E=E_F} = -\frac{\pi^2}{3} \frac{k_B^2 T}{|e|E_F} \xi \quad (2)$$

where  $\sigma(E)$ , would be the conductivity measured for  $E_F$  at  $E$ ,  $\xi = [\partial \ln(\sigma(E))/\partial \ln E]_{E_F}$  and  $E_F$  is measured from the band edge. For spherical Fermi surfaces  $\xi = 1$  for scattering by impurities (constant mean-free-path) and  $=3$  for quasi-elastic phonon scattering [8,9]. For holes, the corresponding values of  $\xi$  are negative. In metals with more complicated Fermi surfaces  $\xi$  deviates strongly from these ideal values and its sign may be unrelated to the type of the carriers.<sup>1</sup> The Fermi energy of carriers in  $\text{MgB}_2$ , estimated [11] by fitting Mott's formula with  $\xi = -1$  to the linear portion of  $S(T)$  was found in fair agreement with that obtained from band structure calculations. Good agreement between the fitted  $E_F$  and band calculation is claimed also in Ref. [15], although different parameters were employed in the latter interpretation.  $\text{MgB}_2$  is a multi-band system [16–19] with complicated Fermi surfaces. In Ref. [4] the Seebeck tensor  $S_D$  was calculated using the two pairs of bands ( $\sigma$  and  $\pi$ ) that contribute to the conductivity of  $\text{MgB}_2$ . The general expressions for

the tensor's components were calculated instead of using Mott's approximation; an isotropic relaxation time, independent on energy, was assumed in that work and a strong phonon drag contribution was included. The calculated  $S(T)$ , representing an average over all directions is in semiquantitative agreement with the experimental  $S(T)$  and reproduces the main features of the dependence on temperature and on Al-doping. This shows that in undoped  $\text{MgB}_2$  the contribution of the  $\sigma$  bands to  $S$  exceeds by far that of the  $\pi$  bands.  $S(T)$  in  $\text{MgB}_2$  may be regarded as fairly simple in spite of the material's complex electronic structure and complications mentioned below:

- The scattering mechanisms dominating transport in each of the bands of  $\text{MgB}_2$  are presently under debate [18,20–22]. The role of the electron–phonon interaction in the thermopower of metals at  $T < \theta_D$ , is not trivial and has been the subject of many studies that did not yet lead to a consensus [23,24].  $\text{MgB}_2$  (and many other diborides) have very high Debye temperatures, typically between 500 and 1000 K [25], thus the interesting regime for their thermopower is  $T < \theta_D$  where the phonon scattering is inelastic.
- All measurements reported so far have been carried out on polycrystalline samples. In such samples it is difficult to distinguish between the contributions of impurity scattering in the bulk and grain-boundary resistance to the residual resistivity (thermopower is insensitive to grain-boundaries). Moreover, a material formed of anisotropic, randomly oriented crystallites appears as if it is multiphase. The thermopower of such a system may be affected by the anisotropy of  $\rho$ , of the heat conductivity and of  $S$  [26].

The solution of the theoretical problems as well as the growth of  $\text{MgB}_2$  single crystals (SCs) (with controlled impurity content) may take some time. At this stage, it was interesting to find out if the relative simplicity of  $S(T)$  for  $\text{MgB}_2$  is accidental or if it is common among the diborides. In particular we looked for a correlation between the density of states (DOS) distribution function  $N(E)$  which is known for many diborides and  $S(T)$ . For spherical equi-energy surfaces and elastic scatter-

<sup>1</sup> Even the sign of  $S$  for Cu, Ag and Au (which are simpler than  $\text{MgB}_2$  in all respects) was not understood for many decades.

ing this correlation is straightforward, but for real metals, even elemental and monovalent, it is not.

Except for  $\text{MgB}_2$ , all known diborides of hexagonal structure are either non-superconducting or low- $T_c$  superconductors [27]. Although many have been investigated in the past, we found in the literature detailed results of  $S(T)$  only for  $\text{TiB}_2$  [28]. It is more complicated than  $S(T)$  for  $\text{MgB}_2$ , exhibiting a sign change from p-type at low- $T$ , to n-type at high- $T$ , and rather poor reproducibility from sample to sample.  $E_F$  of  $\text{TiB}_2$  lies at a minimum of the DOS, in a “pseudogap” [25,29]. Our choices of diborides for electronic transport measurements were  $\text{AlB}_2$  and  $\text{ZrB}_2$ . Following Mg which is divalent, Al is trivalent and Zr—tetravalent. As summarized below, these materials are interesting for additional reasons.

Thirty years ago it has been pointed out that although  $\text{AlB}_2$  is the prototype structure for many diborides, nothing has been reported on its electrical properties [30]. Room temperature (RT) resistivity and Hall effect measurements were reported in that work; the RT Hall constants of several samples were p-type and consistent with  $p \leq 1$  hole/unit cell. It seems that since then not much has been published on this topic. X-ray spectroscopy results published before [31] and after [32,33] the discovery of superconductivity in  $\text{MgB}_2$  show that as in the case of  $\text{TiB}_2$ ,  $E_F$  of  $\text{AlB}_2$  lies in a pseudogap. This is in contrast with the large DOS at  $E_F$  in  $\text{MgB}_2$ . Polarization-dependent X-ray emission and absorption in SCs of  $\text{AlB}_2$  showed that  $E_F$  lies well above the  $\sigma$  band. Al can substitute Mg to form  $\text{Mg}_{1-x}\text{Al}_x\text{B}_2$  in a wide range of concentrations [34]. This substitution leads first to a decrease in  $T_c$  and then to the disappearance of superconductivity, consistent with expectations from electronic structure calculations [16]. For low values of  $x$  the thermopower increases with  $x$  [11]; this is consistent with the shift of  $E_F$  towards the  $\sigma$  band-edge.

$\text{ZrB}_2$  is remarkable: it is a hard, refractory material, its melting point ( $\sim 3000$  °C) is much higher than that of its constituents, and it is a very good conductor although its electronic structure is not that of a metal [35]. The Hall constants obtained in the sixties were consistent with a very low, temperature independent electron concentra-

tion [36]. Early [35,37] and recent band structure calculations [38–40] show that its  $E_F$  lies in a “pseudogap”; close inspection of the figures of Refs. [35,38–40], reveals that  $E_F$  lies slightly above the dip, that is, where  $dN(E)/dE > 0$ . Superconductivity at 5.5 K was recently reported for a sintered  $\text{ZrB}_2$  sample [41] but it was later attributed to a minority phase [42]. According to Ref. [39], the low value of  $N(E_F)$  and the weak electron–phonon coupling (obtained from specific-heat measurements) seem inconsistent with  $T_c = 5.5$  K. In our investigation we found marks of superconductivity in a porous  $\text{ZrB}_2$  sample sintered at low temperature. The resistivity and thermopower of samples sintered at high temperatures exhibit logarithmic temperature dependencies, typical for weak localization in 2D.

We tried to grow crystals of all three materials; so far only some of our  $\text{AlB}_2$  SCs have reasonable dimensions for resistivity and thermopower measurements. It will be shown however that the thermopower of polycrystalline  $\text{AlB}_2$  is close to that of  $\text{AlB}_2$  SCs. The results for our  $\text{MgB}_2$  samples agree with the earlier results and confirm the weak sensitivity of its  $S(T)$  to microstructure. The apparent systematics of  $S(T)$  as function of valence is one of the significant findings of this work: while the  $S(T)$  graphs for  $\text{ZrB}_2$  samples (n-type) are almost mirror images of those for  $\text{MgB}_2$  samples (p-type),  $S(\text{AlB}_2)$  is very low at all temperatures.

## 2. Experimental

### 2.1. Sample preparation and characterization

*MgB<sub>2</sub>*. Polycrystalline  $\text{MgB}_2$  was prepared via various protocols. Here we report on two very different types of  $\text{MgB}_2$ : (a) non-annealed (NA)—formed by RT compression of Alpha-Aesar  $\text{MgB}_2$  powder and (b) hot pressed (HP)—annealed for several hours at 1000 °C under a pressure of 20 MPa.<sup>2</sup>

<sup>2</sup> The hot-pressed annealing of  $\text{MgB}_2$  and sintering of  $\text{ZrB}_2$  at high temperatures has been carried out at the Ceramic and Silicate Institute, Technion City.

$ZrB_2$ . One set of samples was prepared by the standard solid state synthesis from the elements in stoichiometric ratio. The bar-shaped samples were annealed twice at 1500 °C in flowing Ar5%H<sub>2</sub> with intermediate grinding. They were very porous and brittle but on one of them (sample S1) we were able to carry out transport measurements. Rigid samples were obtained by sintering of pressed powder at 1800 °C in Ar atmosphere for 1 h.<sup>2</sup> The raw materials for the high temperature sintering were (a) the powder prepared before from the elements (sample S2) and (b) commercial (Art)  $ZrB_2$  powder with a small boron deficiency (of 0.23% of the total mass) and carbon and oxygen impurities (0.6% and 1.4% of the total mass, respectively). We attempted to grow SCs by slow cooling of molten aluminum solutions of  $ZrB_2$  [43]. The dominant products of two such attempts were mm size rectangular platelets later identified via X-ray diffraction (XRD) as  $Al_3Zr$  SCs. A minority of sub-mm size hexagonal crystallites were later identified as  $ZrB_2$ , however these were too small for transport measurements.

$AlB_2$ . Sub-mm up to mm size,  $\sim 10$   $\mu m$  thick SCs were grown by slow cooling of molten aluminum solutions, following a protocol similar to those of Refs. [30,33]. Slightly larger and thicker (20–40  $\mu m$  thick) crystals were obtained (unintentionally) as a by-product of hexaborides' SC growth [44]. It is easier to grow SCs of  $AlB_2$  from molten aluminum solution than to sinter pellets of high purity powder. This is due to the decomposition of  $AlB_2$  into  $AlB_{12} + Al$  in the absence of excess Al [45]. Here we report on a NA, polycrystalline sample—formed by RT compression of  $AlB_2$  powder (Aldrich 99%); it was relatively rigid and robust.

The XRD patterns for all polycrystalline samples show no foreign phases except for traces of MgO in the HP  $MgB_2$  samples and of  $ZrO_2$  in  $ZrB_2$  S1. The diffraction pattern of the  $ZrB_2$  samples grown at 1800 °C showed no traces of impurities.

## 2.2. Resistivity, thermopower and AC susceptibility measurements

The resistivity of bar-shaped samples was measured by the standard four-probe method in a

closed cycle refrigerator or on a cold finger of a He cryostat. The thermopower measurements on polycrystalline samples were carried out in a He cryostat from 5 K up to RT. In a separate system, that may be adapted to small and fragile samples and can be heated from liquid N<sub>2</sub> temperature up to 400 K, we measured the thermopower of  $AlB_2$  SCs and of the polycrystalline samples (the latter above RT). The thermal emf was measured between the copper wires of two copper-constantan thermocouples with their junctions embedded in the copper heat sinks bridged by the samples;  $S$  was obtained by adding  $S(Cu)$  to the measured thermal emf. For some unknown reason, it was very difficult to obtain good thermal contacts to the  $ZrB_2$  samples in the system for high temperature thermopower measurements. Good thermal contacts were obtained once for sample S2 but above 340 K they were lost and the measurements became irreproducible.

AC susceptibility of  $ZrB_2$  was measured in a home-built susceptometer based on Oxford Teslatron, with a frequency of 1 KHz.

## 3. Experimental results

### 3.1. Temperature dependence of resistivity

For all samples investigated in this work  $\rho(T)$  exhibited a BG-like temperature dependence. We analyzed the experimental traces in terms of the textbook BG formula with  $n = 5$  (see Eq. (1)). The fitting parameters  $\rho_0$ ,  $A$  and  $\theta_R$  for each sample are given in Table 1. We also added the  $\rho(RT)/\rho_0$  data. Values of  $\theta_D$  for  $MgB_2$  and  $ZrB_2$ , from the literature, are shown in the last column of Table 1. (No datum was found for  $AlB_2$ ). The reduced resistivities of all samples  $\Delta\rho(T)/\Delta\rho(\theta_R)$  are plotted as function of the reduced temperature  $T/\theta_R$ , in Fig. 1. All data fall close to the solid line which represents the theoretical BG function. Since for all samples  $\rho_0$  is much larger than  $\Delta\rho(T < 100$  K) the fit is biased by the high temperature data.

Both  $MgB_2$  HP and NA samples were superconducting with  $T_c = 38.3$  and 36 K, respectively in spite of their different resistivities:  $\rho_0(NA)/\rho_0(HP) \sim 140$  (!) and  $A(NA)/A(HP) = 8$ . The

Table 1  
Fitting parameters of the BG formula to  $\rho(T)$  for various samples of  $\text{MgB}_2$ ,  $\text{AlB}_2$  and  $\text{ZrB}_2$

Sample	Type	Relative density	$\rho(\text{RT})/\rho_0$	$\rho_0$ ( $\Omega\text{cm}$ )	$A$ ( $\Omega\text{cm}$ )	$\theta_{\text{R}}$ (K)	$\theta_{\text{D}}$ (K)
$\text{MgB}_2$ HP	Hot pressed	0.8	3.0	$1.12 \times 10^{-5}$	$4.09 \times 10^{-4}$	$862 \pm 18$	750–1050 <sup>a</sup>
$\text{MgB}_2$ NA	NA	0.8	1.2	$1.54 \times 10^{-3}$	$3.16 \times 10^{-3}$	$797 \pm 13$	
$\text{AlB}_2$ SC1	Single crystal <sup>b</sup>		1.4	$1.89 \times 10^{-4}$	$9.63 \times 10^{-4}$	$749 \pm 14$	
$\text{AlB}_2$ SC2	Single crystal <sup>b</sup>		1.4	$1.41 \times 10^{-4}$	$1.11 \times 10^{-3}$	$956 \pm 13$	
$\text{AlB}_2$ SC3	Single crystal <sup>c</sup>		1.4	$1.35 \times 10^{-4}$	$6.20 \times 10^{-4}$	$706 \pm 16$	
$\text{AlB}_2$ NA	NA	0.65	1.1	$2.11 \times 10^{-3}$	$2.17 \times 10^{-3}$	$524 \pm 20$	
$\text{ZrB}_2$ S1	Sintered (1500 °C)	0.55	1.7	$6.20 \times 10^{-4}$	$5.67 \times 10^{-3}$	$712 \pm 16$	585, 630 <sup>d</sup>
$\text{ZrB}_2$ S2	Sintered (1800 °C)	0.65	3.9	$7.71 \times 10^{-6}$	$2.70 \times 10^{-4}$	$666 \pm 4$	
$\text{ZrB}_2$ S3	Sintered (1800 °C)	0.72	2.2	$1.05 \times 10^{-5}$	$1.49 \times 10^{-4}$	$678 \pm 8$	

<sup>a</sup> See Refs. [4,48] and references therein.

<sup>b</sup> Obtained unintentionally during growth of  $\text{CaB}_6$  following the protocol in Ref. [44].

<sup>c</sup> Obtained following the protocol in Ref. [30].

<sup>d</sup> See Tables 3 and 4 in [25] and references therein.

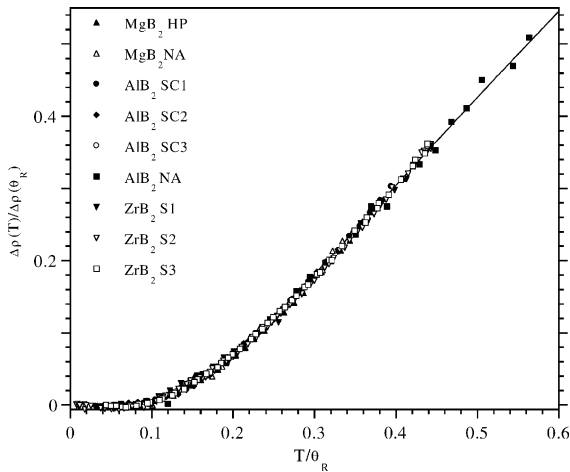


Fig. 1.  $\Delta\rho(T)/\Delta\rho(\theta_{\text{R}})$  versus  $T/\theta_{\text{R}}$  for various  $\text{MgB}_2$ ,  $\text{AlB}_2$  and  $\text{ZrB}_2$  samples. The solid line represents BG function (Eq. (1)). The fitting parameters for each sample are shown in Table 1.

large values of  $\rho_0$  indicate that at least for the NA sample the resistivity is dominated by grain-boundaries. The fairly large ratio of  $A(\text{NA})/A(\text{HP})$  indicates that a large part of the grain boundaries of the NA sample probably blocks the current. The values of  $\theta_{\text{R}}$  for these two samples (and of additional samples investigated by us) are close and fall within the range of  $\theta_{\text{D}}$  values obtained from lattice measurements.

The RT resistivities of our  $\text{AlB}_2$  SCs are larger than those cited in Ref. [30] by factors of 3–9. For all three SCs,  $\rho(\text{RT})/\rho_0 = 1.4$ ; their resistivity seems to be dominated by impurity scattering. For the porous, NA sample this ratio is only 1.1. In this case, a large part of  $\rho_0$  is probably due to grain boundaries. The values of the fitted  $\theta_{\text{R}}$  are spread over a range that is much wider than those for  $\text{MgB}_2$  or  $\text{ZrB}_2$ . This is in spite of the fact that  $\rho(\text{RT})/\rho_0$  for the  $\text{MgB}_2$  NA and  $\text{AlB}_2$  NA samples are comparable and the porosity of the  $\text{ZrB}_2$  S1 sample is larger than that of the  $\text{AlB}_2$  NA sample. We looked therefore for a process that may compete with electron–phonon scattering leading to a BG type  $\rho(T)$ . Such a process is the scattering from vibrating impurities. This mechanism known as “electron–phonon–impurity–interference” was analyzed in detail by Reizer and Sergeev [46]. Its signature is the behavior of  $\rho(T)$  at temperatures far below  $\theta_{\text{D}}$ :  $\Delta\rho_{\text{Int}} = \rho - \rho_0 = \rho_0 B T^2$  where  $B$  is a constant. The reduced resistivities  $\Delta\rho(T)/\Delta\rho(\theta_{\text{R}})$  calculated from the BG formulae BG(5) (Eq. (1)) and BG(3), and the Reizer and Sergeev (RS) formula [46] are plotted as function of the reduced temperature  $T/\theta_{\text{R}}$ , in Fig. 2(a). It can be seen that up to  $T \approx 0.1\theta_{\text{R}}$ ,  $\Delta\rho(T) \propto T^5$  and  $T^3$  according to the BG formulae and  $\propto T^2$  according to the RS formula; with increasing  $T$  the slope drops gradually towards 1 for the first two cases and 0 for the

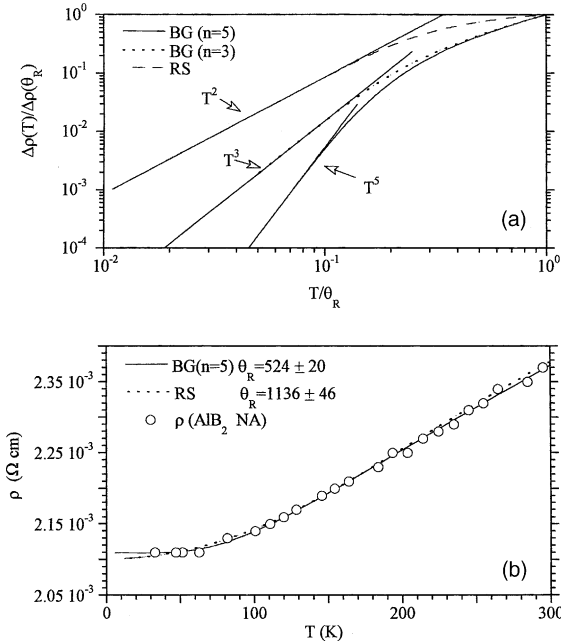


Fig. 2. (a)  $\Delta\rho(T)/\Delta\rho(\theta_R)$  versus  $T/\theta_R$  given by the BG functions with  $n = 5$  and  $3$  and the RS functions, (b)  $\rho$  versus  $T$  for sample  $\text{AlB}_2$  NA, with the BG(5) and RS functions fitted to the plot of the experimental data. Note that the values of  $\theta_R$  for the fitted BG(5) and RS functions differ by more than a factor of two.

third. Around  $T/\theta_D = 1/3$  the BG ( $n = 5$ )  $\Delta\rho(T) \propto T^2$ ; if the temperature dependence of the resistivity is minor due to a large  $\rho_0$ , and  $\theta_D$  is unknown, it is hard to distinguish between the BG and RS temperature dependencies (or their combination). The analysis of  $\rho(T)$  for the  $\text{AlB}_2$  NA sample in terms of the two alternative formulae is a good example for this uncertainty. Fig. 2(b) shows the two lines fitted to the experimental plot. The fitted  $\theta_R$  value for the RS formula is more than twice larger than that for the BG formula.  $\Delta\rho(T < 100 \text{ K})$  for the three SCs was plotted as function of  $T^2$  and as function of  $T^5$  and linear functions were fitted to the plots. The  $R^2$  of the lines fitted to the  $\Delta\rho$  versus  $T^2$  plots were higher but not enough to prove that the low- $T$  resistivity is governed by the RS mechanism. The spread of the  $\theta_R$  values among the SCs indicates that the two mechanisms probably compete at low temperatures; this implies that  $\theta_R(\text{AlB}_2)$  is about 1000 K.

$\text{ZrB}_2$  sintered at  $1500^\circ\text{C}$  was very porous and brittle. However it was possible to carry out both resistivity and thermopower measurements on such a sample. Upon increasing the sintering temperature of  $\text{ZrB}_2$  from  $1500$  to  $1800^\circ\text{C}$ ,  $\rho_0$  dropped by about two orders of magnitude and  $A$ —by more than one. High temperature sintering heals most of the grain boundaries, as hot pressing does in the case of  $\text{MgB}_2$ . The material sintered at the higher temperature is very rigid although its density is much lower than the ideal density (see relative densities of samples S2 and S3 in Table 1).

The resistivities of  $\text{ZrB}_2$  samples S2 and S3 are larger but of the same order of magnitude as that reported in Ref. [41].  $\rho(T)$  of these samples exhibited a shallow minimum around  $40 \text{ K}$  which is barely resolved from the noise in the case of S2. No drop in  $\rho(T)$ , that could be associated with transition to superconductivity, was detected in this sample down to  $T = 4.75 \text{ K}$ . The clear minimum of  $\rho(T)$  of sample S3 seen in Fig. 3 was obtained under very slow cooling. Attempts were made to fit several functions to the regime where the temperature coefficient of resistivity is negative. The best fit to the experimental data for  $7 \leq T \leq 40 \text{ K}$ , and a very good one ( $R^2 = 0.997$ ), was obtained for the logarithmic function. This behavior is the signature of weak localization in 2D [47]. The coefficient of  $\ln(T)$  seems to support this possibility:  $\Delta\sigma_{\text{square}} = c\Delta\rho/\rho^2 \approx 8 \times 10^{-5} \ln(T) \Omega^{-1}$ , where  $c$  ( $= 3.53 \text{ \AA}$ ) is the lattice parameter

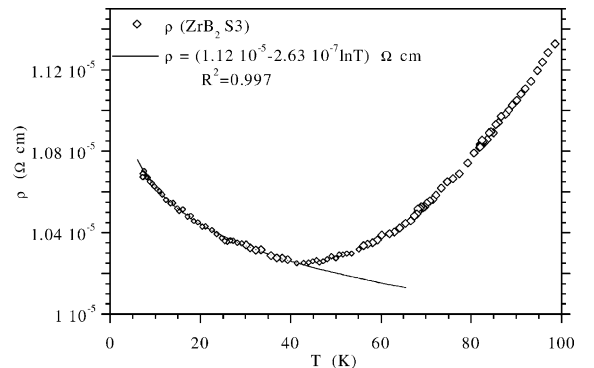


Fig. 3. The shallow minimum in  $\rho$  versus  $T$  for sample  $\text{ZrB}_2$  S3 at low temperatures. The solid line represents the fitted logarithmic function that indicates weak localization (see text).

of  $\text{ZrB}_2$ ; the coefficient of  $\ln(T)$  in  $\Delta\sigma_{\text{square}}$  is very close to the value of  $G_0 = 2e^2/h$  ( $= 7.75 \times 10^{-5} \Omega^{-1}$ ), of the order of the theoretical coefficient. The origin of the weak disorder in S2 and S3 may be carbon impurities from the graphite crucible or deviations from stoichiometry. As shown below, the thermopower of the  $\text{ZrB}_2$  samples S2 and S3 provides further support for weak localization. The shallow minimum discussed above had a negligible effect on the fitting parameters of the BG formula. It can be seen that  $\theta_R$  varies little from sample to sample; it is much larger than that found in Ref. [41] but closer to  $\theta_D$  (see Table 1).

A narrow step was observed around 5.4 K in the AC magnetic susceptibility of sample S1; it was about 0.3% of the step found (around 87 K) for an YBCO sample of comparable volume. A similar step was observed around 3 K for the unprocessed commercial powder. AC susceptibility showed no marks of a transition to superconductivity in S2 and S3 and in the powder synthesized by us.

### 3.2. Temperature dependence of thermopower

Fig. 4 represents  $S(T)$  for  $\text{MgB}_2$ ,  $\text{AlB}_2$  and  $\text{ZrB}_2$  samples on which  $\rho(T)$  was measured. The most prominent feature of this figure is that  $S(T)$  for  $\text{MgB}_2$  and  $\text{ZrB}_2$  lie on both sides of  $S = 0$  almost as *mirror images* of one another with  $S(T)$  of  $\text{AlB}_2$  lying in the middle, with almost zero values for all temperatures.

Looking for systematics in  $S(T)$  for these materials was rewarding. The details, specific for each system, will be discussed prior to drawing conclusions on the systematics.

In general there is good agreement between  $S(T)$  of the  $\text{MgB}_2$  HP sample and most of the earlier results in the overlapping ranges of temperature. The solid line through the low- $T$  data points represents  $S = -1 + 0.034T \mu\text{V/K}$ . In Refs. [4,11,13–15] the RT values of  $S$  range between 7 and 8.7  $\mu\text{V/K}$ , those of  $dS/dT$  in the linear regime range between 0.035 and 0.042  $\mu\text{V/K}^2$ . There is also agreement on the negative extrapolated value of  $S$  at  $T = 0$ . The  $S(T)$  data for the NA  $\text{MgB}_2$  sample are very close to those of the HP sample in the regime where  $S(T)$  is linear; this, in spite of the

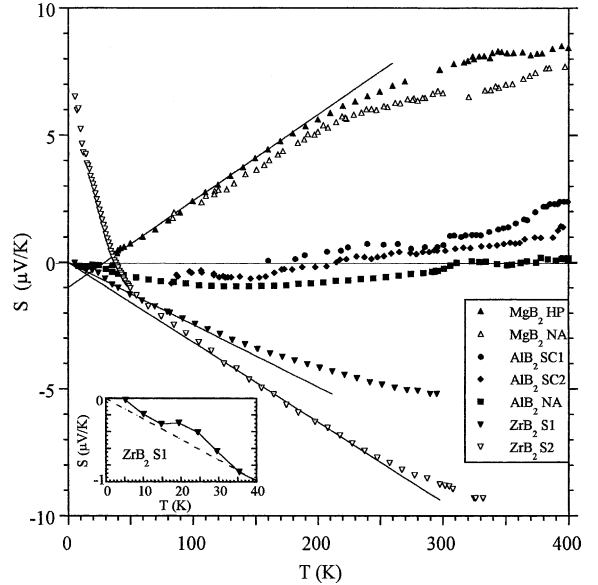


Fig. 4.  $S$  versus  $T$  for samples of  $\text{MgB}_2$ ,  $\text{AlB}_2$  and  $\text{ZrB}_2$  on which resistivity was measured (see Fig. 1 and Table 1). The solid line that passes through data points for the  $\text{MgB}_2$  HP sample represents  $S = -1 + 0.034T \mu\text{V/K}$  and the two solid lines that pass through data points for  $\text{ZrB}_2$  S1 and S2 represent  $S = -0.025T$  and  $S = -0.032T \mu\text{V/K}$ , respectively. Low temperature  $S(T)$  for  $\text{ZrB}_2$  S1 is shown on an expanded scale in the inset. The low temperature range of  $S(T)$  for S2 is replotted in Fig. 5.

fact that the residual resistivities of these two samples are different by more than two orders of magnitude. This emphasizes the weak sensitivity of the thermopower to grain-boundaries and porosity. The difference between  $S(T)$  for the HP and NA samples is larger at high temperatures where  $S(T)$  is non-linear and tends to saturate.

Up to RT,  $S(T)$  for the  $\text{AlB}_2$ , NA and SC samples, lie within  $\pm 1 \mu\text{V/K}$ . Above RT,  $S$  for the polycrystal remains zero and that of the SCs increases up to 1.5 and 2.5  $\mu\text{V/K}$ . As in the case of  $\text{MgB}_2$ , the microstructure (or composition) affects  $S(\text{AlB}_2)$  mainly at high temperatures. It is notable that at high temperature, the sign of  $S$  for the  $\text{AlB}_2$  SC samples (+) is the same as that of the RT Hall constant [30].  $N(E)$  in the pseudogap is probably non-symmetric. With increasing temperature the increasing  $\Delta E$  window around  $E_F$  may contain more hole-like than electron-like states leading to positive  $S$  and  $R_H$ .

$S(T)$  for the  $\text{ZrB}_2$  S1 (sintered at 1500 °C) and S2 (sintered at 1800 °C) are quasilinear over wide ranges of temperature. The straight lines that pass through the data points in this region represent  $S = -0.025T$   $\mu\text{V/K}$  and  $S = -0.032T$   $\mu\text{V/K}$ , for S1 and S2, respectively. The reproducibility of  $S(T)$  for samples prepared differently is poorer than for  $\text{MgB}_2$ . Above  $\sim 150$  K for S1 and  $\sim 250$  K for S2, the corresponding  $S(T)$  become nonlinear exhibiting a tendency towards saturation, very similar to that of  $S(\text{MgB}_2)$ .  $S(T)$  of S1 at low temperatures is shown on an expanded scale in the inset of Fig. 4. A minute but reproducible deviation from the straight line is observed around 20 K; it resembles what one would expect for phonon drag thermopower in a dirty metal. At 5 K  $S \approx -0.01$   $\mu\text{V/K}$ , i.e. zero within the experimental uncertainty as expected for a superconductor. However, a thin, percolating superconducting filament could account for this result.

Below  $\sim 50$  K,  $S(T)$  for  $\text{ZrB}_2$  S2 deviates from the straight line, crosses the  $S = 0$  line at  $T = 38$  K and increases steeply with further decrease of  $T$ . This behavior was exhibited by several samples sintered at 1800 °C and accompanies their  $\rho(T)$  bearing the signature of weak localization. There have been conflicting predictions for the thermopower in the weak-localization regime; recent results suggest a  $\ln(1/T)$  dependence of  $S$  [49].  $S(T)$  for samples S2 and S3 below 40 K is plotted as function of temperature on a linear-log scale in Fig. 5. At least for S3 the logarithmic function fits remarkably well the experimental plot ( $R^2 = 0.998$ ). The inset of Fig. 5 shows  $\rho(T)$  for S3 (shown before in Fig. 3), replotted on a linear-log scale. To our knowledge this is a rare example of evidence for weak localization in 2D, based on both  $\rho(T)$  and  $S(T)$  dependencies.

We now return to the gross features of  $S(T)$  and show that these seem to be correlated with  $dN(E)/dE|_{E_F}$ . Inspection of the available  $N(E)$  graphs shows that  $dN(E)/dE|_{E_F}$  is negative for  $\text{MgB}_2$  [16,32,40,50], positive for  $\text{ZrB}_2$  [35,38–40] and  $\sim 0$  for  $\text{AlB}_2$  [31–33]. For spherical equi-energy surfaces and elastic scattering this correlation is straightforward since  $\sigma(E) \propto v^2(E)\tau(E)N(E)$  where  $v(E)$  is the energy dependent velocity, and the derivative of  $v^2(E)\tau(E)$  has the same sign as that of

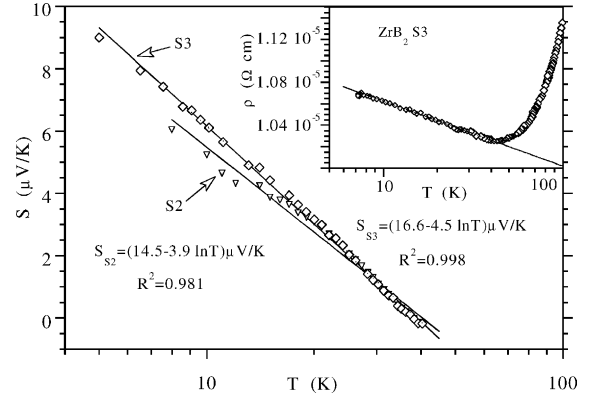


Fig. 5.  $S$  versus  $T$  for the nonsuperconducting  $\text{ZrB}_2$  S2 and S3 samples plotted on a linear-log scale.  $\rho$  versus  $T$  for sample  $\text{ZrB}_2$  S3 plotted on linear-log scale is shown in the inset.

$N(E)$  [9]. Suppose that this relation, with  $N(E)$  and the diffusivity  $D (\propto v^2(E)\tau(E))$  replaced by averages over equi-energy surfaces may be extended to our systems. The question “which of the two terms  $d \ln N(E)/dE|_{E_F}$  and  $d \ln D(E)/dE|_{E_F}$  dominates  $d \ln \sigma(E)/dE|_{E_F}$ ” might be posed. The answer ( $d \ln N(E)/dE|_{E_F}$ ) is simple in the case of  $\text{AlB}_2$  for which  $dN/dE|_{E_F} \approx 0$  and  $S \approx 0$ . The values of  $dS/dT$  for  $\text{MgB}_2$  HP and  $\text{ZrB}_2$  S1 and S2 yield:  $d \ln \sigma(E)/dE|_{E_F} \approx -1.4, +1.0$  and  $+1.3$   $\text{eV}^{-1}$ , respectively. Within the limited resolution of the available  $N(E)$  graphs around  $E_F$  we checked if  $(1/N)dN/dE|_{E_F}$  can reach  $-1.4$  and  $+1.3$   $\text{eV}^{-1}$ , for  $\text{MgB}_2$  and  $\text{ZrB}_2$ , respectively. In Fig. 2 of Ref. [16]  $N(E)$  of  $\text{MgB}_2$  has a steep negative slope around  $E_F$  where  $N(E) \sim 0.7$ ; inspection of that graph shows that  $dN/dE$  could be  $-1$   $\text{eV}^{-2}$ . In Fig. 3 of Ref. [38]  $N(E)$  of  $\text{ZrB}_2$  has a steep positive slope around  $E_F$  where  $N(E) \sim 0.3$ ; according to this figure  $dN/dE|_{E_F}$  could be  $+0.4$   $\text{eV}^{-2}$ ; however,  $dN/dE|_{E_F}$  in Fig. 1 of Ref. [39] seems larger. In spite of this uncertainty it seems that  $(1/N)dN/dE|_{E_F}$  plays an important role in  $S(T)$  of all three materials.

#### 4. Summary and final remarks

Resistivity and thermopower measurements were carried out on polycrystalline samples of the



three title materials and on SCs of  $\text{AlB}_2$ . The polycrystalline samples were either hot-pressed ( $\text{MgB}_2$  HP), sintered at various temperatures ( $\text{ZrB}_2$  S1–S3) or just compacted at RT ( $\text{MgB}_2$  NA and  $\text{AlB}_2$  NA). Single crystal growth was attempted for all three materials but only the  $\text{AlB}_2$  crystals were large enough for both resistivity and thermopower measurements.

For all samples  $\rho(T)$  exhibited BG-like temperature dependencies. Fitting the textbook formula to the  $\rho(T)$  graphs for  $\text{MgB}_2$  and  $\text{ZrB}_2$  gave characteristic temperatures ( $\theta_R$ ) that vary little from sample to sample and fall close to the respective Debye temperatures obtained from thermal measurements. Larger  $\theta_R$  values are obtained from fitting to the experimental plots a generalized BG function (BG(3)). A widespread of  $\theta_R$  values was obtained for the  $\text{AlB}_2$  samples. Using the case of  $\text{AlB}_2$  NA sample having the largest  $\rho_0$  and lowest fitted  $\theta_R$ , it was shown that the widespread of  $\theta_R$  values among the  $\text{AlB}_2$  samples may be due to competition between phonon scattering and scattering from vibrating impurities [46].

$\text{MgB}_2$  samples with resistivities different by more than two orders of magnitude exhibited superconductivity below only slightly different transition temperatures. Marks of low- $T$  superconductivity (at  $\sim 5.5$  K) were obtained in the AC susceptibility and thermopower measurements in a sample of  $\text{ZrB}_2$  processed at low temperatures. These marks may be due to a foreign phase, as proposed for previously published results [42]. No marks of superconductivity were detected in samples of  $\text{ZrB}_2$  processed at higher temperatures, having much lower resistivities. At low temperatures the resistivity and thermopower of these samples exhibit a logarithmic dependence on temperature, typical for weak localization in 2D.

At high temperatures the thermopower  $S(T)$  for  $\text{ZrB}_2$  (n-type) is almost the mirror image of  $S(T)$  for  $\text{MgB}_2$  (p-type) while  $S(\text{AlB}_2)$  is very small at all temperatures. Using available graphs of the DOS distribution  $N(E)$  around  $E_F$ , it is shown that for  $\text{MgB}_2$  and  $\text{ZrB}_2$  the sign of  $S$  is that of  $-\text{d} \ln N(E)/\text{d}E$ . Rough estimates of  $\text{d} \ln N(E)/\text{d}E|_{E_F}$  are consistent with the possibility that this term represents the main contribution to the magnitude of  $S$ . Thus, it may not be accidental

that for  $\text{AlB}_2$   $\text{d}N(E)/\text{d}E|_{E_F} \sim 0$  and  $S(E)$  is very small at all temperatures.

The results of this work suggest that measuring transport properties of additional diborides may be rewarding. The first choices would be materials for which calculated and/or experimental  $N(E)$  around  $E_F$  results are available. It would also be interesting to investigate diborides for which there are conflicting reports about superconductivity.

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