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# Self-Assembly of Supramolecular Fractals from Generation 1 to 5

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## **Supporting Information**

ABSTRACT: In the seeking of molecular expression of fractal geometry, chemists have endeavored in the construction of molecules and supramolecules during the past few years, while only a few examples were reported, especially for the discrete architectures. We herein designed and constructed five generations of supramolecular fractals (G1-G5) based on the coordination-driven self-assembly of terpyridine ligands. All the ligands were synthesized from triphenylamine motif, which played a central role in geometry control. Different approaches based on direct Sonogashira coupling and/or (tpy-Ru(II)tpy) connectivity were employed to prepare complex Ru(II)-organic building blocks. Fractals G1-G5 were obtained in high yields by precise coordination of organic or Ru(II)-organic building blocks with Zn(II) ions. Characterization of those architectures were accomplished by 1D and 2D NMR spectroscopy, electrospray ionization



mass spectrometry (ESI-MS), traveling-wave ion mobility mass spectrometry (TWIM-MS), and transmission electron microscopy (TEM). Furthermore, the two largest fractals also hierarchically self-assemble into ordered supramolecular nanostructures either at solid/liquid interface or in solution on the basis of their well-defined scaffolds.

#### INTRODUCTION

The concept of "fractal geometry" is coined by Mandelbrot to describe the natural geometries, which cannot be described precisely using ideal constructions of Euclidean geometry, such as lines, triangles, squares, circles, spheres, etc.<sup>1</sup> As an important characteristic, fractal geometry displays selfsimilarity at different levels of magnification. Inspired by nature and mathematics, the fractal geometry was introduced into several different scientific fields from physics to geomorphology, from chemistry to materials science, and from economics to biology.<sup>2</sup> In particular, the fractal geometry has been behind an enormous change in the way chemists perceive, and subsequently rebuild, the chemistry field in which we explore.<sup>3,4</sup> For instance, dendrimers have been extensively demonstrated to be iconic molecular fractals in conventional synthetic chemistry.<sup>5–10</sup>

In the seeking of alternatives to avoid multistep synthesis, surface self-assembly recently was employed to construct a

well-known fractal geometry, viz., Sierpiński triangle,<sup>11</sup> through theoretical prediction,<sup>12</sup> halogen bonding,<sup>13</sup> hydrogen bond-ing<sup>14</sup> and coordination<sup>15–17</sup> in ultrahigh vacuum. However, different generations of fractals were assembled as a mixture on the surface. With the goal of exerting more elegant manipulation over structural features of fractals, coordination-driven supramolecular chemistry has stepped into the construction of discrete metallo-supramolecular Sierpiński triangles<sup>18,19</sup> and gaskets<sup>20</sup> through the self-assembly in solution with high yields. Although metallo-supramolecular chemistry has witnessed a spectacular explosion in constructing a great variety of polygons and polyhedrons in the field of Euclidean geometry,  $2^{1-37}$  it still remains a formidable challenge to assemble nontrivial architectures, particularly high generation of fractals. Up to date, most of these metallo-

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supramolecular fractals are limited to low generation of ( $\leq$ 3) Sierpiński geometry (Figure 1a) due to the challenge of design,



Figure 1. (a) Sierpiński triangle fractals and (b) supramolecular fractals designed in this study.

synthesis and separation. An important question was raised: can one assemble other high generations of supramolecular fractals rather than Sierpiński fractals?

In this study, we used well-documented 2,2':6',2"terpyridine (tpy)-based coordination chemistry38-48 to construct discrete supramolecular fractals ranging from generation 1 (G1) to 5 (G5) in high yields. Except for G1 and G4, all other fractals were assembled using two combinations of connectivity, i.e., (tpy-Ru(II)-tpy) and (tpy-Zn(II)-tpy). Briefly, a series of Ru(II)-organic building blocks (ROBBs) was synthesized on the basis of the strong binding ability between tpy and Ru(II).<sup>49-51</sup> In the following self-assembly, such ROBBs can assemble with weak coordination metal, i.e., Zn(II) to construct G2, G3 and G5 fractals with increasing size and complexity. More importantly, these architectures exhibit fractal characteristics through repeating the basic shape unit (G1) to form branched frameworks. It is worth noting that supramolecular fractals we reported here display only statistical self-similarity, which are not identical at all levels of magnification (Figure 1b). By contrast, computer generated (i.e., mathematical) fractals can repeat their self-similarity at all scales.

#### RESULTS AND DISCUSSION

In an effort to elaborate the concept of fractal by coordinationdriven self-assembly, a series of ligands was designed with the goal of assembling a set of discrete structures with Zn(II) ions rather than infinite framework. Those structures possess the same repeating shape unit, namely G1, but display at different scales, leading to different molecular geometry and symmetry. G2 contains three repeating units with a triangle geometry, while G3 is comprised of five repeating units with a dumbbellshaped geometry. The higher generations G4 and G5 consist of 6 and 12 repeating units, respectively. Moreover, all the geometry of G1 to G4 can be found as a proportion in G5, which exhibits the extended supramolecular fractal with high complexity. According to molecular modeling, the size is enlarged more than four times from the smallest supramolecule G1 (~2.5 nm) to the largest one G5 (~11 nm) (Figure 2).

In our synthetic design, triphenylamine motifs played a central role in controlling the geometry of assemblies due to their specific internal bond angles with appropriate molecular rigidity.<sup>52</sup> Tpy units, which were widely used in coordination-driven self-assembly,<sup>43–52</sup> were introduced to provide coordination sites for metal ions. Considering the accessibility, three approaches were utilized to construct building blocks. Approach 1 was using Sonogashira coupling reaction to connect the triphenylamine motifs and tpy directly, for instance, organic ligands LA and LD (Scheme 1). Approach 2 was bridging two organic tpy ligands using Ru(II) chemistry to form ROBB, such as LE with increasing complexity and avoiding multiple self-assembly products.<sup>49a,50</sup> Approach 3 was a combination of the first two methods through performing Sonogashira coupling on the Ru(II)-tpy complexes to precisely control the structures of ligands and the self-assembly supramolecules as well as increasing the diversity and complexity, such as LB and LC. Note that the (tpy-Ru(II)-tpy) connectivity was able to sustain the basic condition and high temperature in the cross-coupling reaction due to its high stability.49a

**Synthesis of Ligands and Fractals.** We initiated the ligand synthesis from organic ligands L and LA, which were obtained easily by approach 1 through connecting different triphenylamine motifs and tpy units using Sonogashira



Figure 2. Energy-minimized structures of fractal complexes  $G1[Zn_2LA_2]$ ,  $G2[Zn_3LB]$ ,  $G3[Zn_6LC_2]$ ,  $G4[Zn_{12}LD_6]$ ,  $G5[Zn_{12}LE_6]$  from molecular modeling (the alkyl chains are omitted for clarity).

Scheme 1. Different Approaches to Prepare the Ligands and Fractal Structures



Figure 3. (a) ESI-MS and (b) TWIM-MS plot (m/z vs drift time) of fractal G2.

coupling (Schemes S2 and S5). L was designed to provide scaffolds of the higher generations of fractals, while LA was able to end-cap the outer binding sites to prevent the

fractal G3.

formation of infinite structure. LA itself could self-assemble into complex  $[Zn_2LA_2]$  in a stoichiometric ratio (1:1) with  $Zn(NO_3)_2$ ·6H<sub>2</sub>O, resulting in the formation of the smallest



Figure 5. (a) ESI-MS spectra and (b) TWIM-MS plot (m/z vs drift time) of fractal G4.



Figure 6. <sup>1</sup>H NMR spectra (500 MHz, 300 K) of LD in  $CDCl_3$  and G4 in  $CD_3CN$ .

structure G1, which represented the basic repeating shape unit in the complex fractal set. Electrospray ionization-mass spectrometry (ESI-MS) and traveling wave ion mobility mass spectrometry (TWIM-MS)<sup>53-56</sup> provided strong evidence for the formation of G1 with a molecular weight of 2722 Da (Figure S8). <sup>1</sup>H NMR, 2D COSY (correlation spectroscopy), and 2D NOESY (nuclear Overhauser effect spectroscopy) spectra supported the formation of the symmetrical structure (Figures S76-S81).



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<sup>*a*</sup>(i) Pd(PPh<sub>3</sub>)<sub>2</sub>Cl<sub>2</sub>, CuI, THF/Et<sub>3</sub>N, 60 °C. (ii) Pd(PPh<sub>3</sub>)<sub>4</sub>, CuI, TBAF, THF/Et<sub>3</sub>N, 70 °C. (iii) Ru(DMSO)<sub>2</sub>Cl<sub>2</sub>, 1,2-dichloroethane, 80 °C. (iv) 1,2-dichloroethane/EtOH, 80 °C.

In the assembly of G2, we initially designed LB' through end-capping L with three equivalents of LA (Figure S1). However, no desired product was achieved after vigorous efforts due to the inert coordination of Ru(II). Therefore, we redesigned and synthesized LB using approach 3 to overcome the inertness of coordination with the combination of Sonogashira coupling reaction and Ru(II) chemistry. Ironically, LB with three Ru(II) ions and six free tpy groups is the most challenging one among all the building blocks for the fractals, although G2 is a relatively small structure among those five fractals.

Two steps of Sonogashira coupling were performed on the Ru(II)-tpy complex S-18 to control the structure of the target ligand and assembled supramolecule (Scheme S3). Complex [Zn<sub>3</sub>LB] or fractal G2 with three repeating units was then obtained by assembling LB with Zn(II) in a 1:3 ratio, followed by the counterions exchange from NO<sub>3</sub><sup>-</sup> to PF<sub>6</sub><sup>-</sup> for mass spectrometry characterization. Note that G2 was not accessible through direct mixing L and LA in 1:3 ratio with corresponding Zn(II) because of self-sorting of individual building block.



Figure 7. (a) ESI-MS spectra and (b) TWIM-MS plot (m/z vs drift time) of fractal G5.

In the design of G3, the preparation of LC' was unsuccessful using approach 2 because of the inert coordination of Ru(II) (Figure S1). As such LC was synthesized using the same strategy as LB but underwent only one step of Sonogashira coupling on ROBB as shown in Scheme S4. Briefly, LC was prepared through coupling of organic precursor S-13 and Ru(II)-tpy complex S-21, which was obtained via double endcapping of precursor S-8 with LA and Ru(II). Such combination strategy allowed us to prepare LC in a moderate isolation yield after a column chromatography separation. Complex  $[Zn_6LC_2]$  or fractal G3 was obtained in a yield of 94% by mixing LC and  $Zn(NO_3)_2$ ·6H<sub>2</sub>O in a 1:3 ratio, followed by the same treatment as the other fractals. G3 is comprised of 5 repeating units with 2 organic precursor compound L and 4 LA in each structure; similarly, the direct self-assembly of L and LA in 1:2 ratio with corresponding Zn(II) was unable to form G3-like fractal because of the selfsorting of individual building block.

ESI-MS and TWIM-MS spectra provided structural information on **G2** and **G3** with one set of multiple charged signals observed from 1D ESI-MS and 2D TWIM-MS spectra. Corresponding isotope pattern of each charged state agreed well with theoretical one (Figures 3 and 4). <sup>1</sup>H NMR spectra, 2D COSY and 2D NOESY spectra of ligand **LB** and fractal **G2** showed four types of tpy (Figure S106). <sup>1</sup>H NMR spectra showed four types of tpy for Ligand **LC** but five types of tpy for fractal **G3** (Figure S107). The assigned structures were supported by detailed 2D COSY and 2D NOESY spectra (Figures S82–S93).

Organic ligand LD was obtained in a straightforward manner by approach 1 through direct Sonogashira coupling. The organic ligand could form the complex  $[Zn_{12}LD_6]$ , or G4 in the fractal set, with  $Zn(NO_3)_2$ ·6H<sub>2</sub>O in a 1:2 ratio. ESI-MS and TWIM-MS spectra provided strong evidence for the formation of G4 with molecular weight of 14865 Da. Only one prominent set of signals for multicharged signals (from 10+ to 19+) was observed in ESI-MS spectrum (Figure 5a). Moreover, a narrow distribution of drift time for different charge states in TWIM-MS spectrum (Figure 5b) indicated there were no isomers or structural conformers generated. Furthermore, the isotope pattern of the multicharged ions agreed well to the simulated one, suggesting the proposed structure (Figure S12). <sup>1</sup>H NMR, 2D COSY and 2D NOESY spectra (Figures S96–S99) supported the formation of symmetrical structures. For instance, in the <sup>1</sup>H NMR spectrum of G4, two types of tpy units were observed and the resonance signals had distinguishable shift compared to LD (Figure 6).

The synthesis of LE was achieved by approach 2 through end-capping hexatopic tpy ligand L with one LA using Ru(II) chemistry in two steps (Scheme 2). Such end-capping approach left four free tpy moieties for further coordination. Complex  $[Zn_{12}LE_6]$  (i.e., G5), the largest supramolecule in the fractal set was obtained in high yield (96%) by treatment LE with  $Zn(NO_3)_2 \cdot 6H_2O$  in a stoichiometric ratio (1:2) in CHCl<sub>3</sub>/MeOH (v/v 1:3) at 50 °C for 10 h, followed by counterion exchange. ESI-MS and TWIM-MS spectra identified the formation of desired fractal G5 with molecular weight of 28 384 Da. Also, one prominent set of signals was observed for multicharged signals (from 14+ to 28+) in ESI-MS spectrum (Figure 7a) and TWIM-MS spectrum (Figure 7b) as other fractals did. <sup>1</sup>H NMR spectra of LE and G5 were consistent with the assigned structure. Four sets of tpy signals were observed in both ligand and complex, indicating a highly symmetrical structure was formed after complexation (Figure 8). All the protons of 3', 5' positions on the metal-free tpy units of LE, i.e.,  $A^{3',5'}$  and  $B^{3',5'}$  were shifted downfield (~0.4 ppm) due to electron deficiency upon coordination with metal ions, while those protons of 6, 6" positions were significantly shifted upfield (~0.7 ppm) due to electron shielding effects according to the previous reports.<sup>45a,50</sup> In addition, the characteristic protons on alkoxy chain  $(-OCH_2-)$  with a 1:2:1 integration ratio also suggested the formation of discrete structure rather than polymers. All the assignments were confirmed by detailed 2D COSY and 2D NOESY spectra, respectively (Figures S102–S105).

Diffusion-ordered NMR spectroscopy (DOSY) experiments were conducted to provide dimensional information on those supramolecular assemblies.<sup>48,57</sup> All the five spectra showed narrow bands of signal that suggested the self-assemblies formed discrete supramolecular architectures (Figure 9). Moreover, the diffusion coefficient (D, m<sup>2</sup>/s) decreased from 4.99 × 10<sup>-10</sup> to 1.46 × 10<sup>-10</sup> as the size gradually increased from G1 to G5.<sup>57,58</sup> And the experimental hydrodynamic radius ( $r_{\rm H}$ ) of the fractals from the D value agreed well to the molecular modeling. For instance, the obtained radii for G4 and G5 were 4.2 and 5.7 nm, respectively, which were comparable to the sizes obtained from the modeling. And the results were summarized in Table S1.

Transmission electron microscopy (TEM) was also utilized to provide further structural information on the shape and size of the complexes, especially the large fractals **G4** and **G5**. The measured dimension of individual supramolecule deposited on the surface of copper grid showed the diameter around 7 and 12 nm (the average distance between the farthest corners) for **G4** and **G5**, respectively from TEM images (Figures 10a–d), which were also consistent with the sizes obtained from



Figure 8. <sup>1</sup>H NMR spectra (500 MHz, 300 K) of LE in DMSO-d<sub>6</sub> and fractal G5 in CD<sub>3</sub>CN.

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-8.75-					<u> </u>
9	9.18.17.1	9.18.17.1	9.1 8.1 7.1	9.1 8.1 7.1	9.1 8.1 7.1
Chemical shift (ppm)					

Figure 9. 2D DOSY NMR spectra (600 MHz, 300 K) of G1–G5 in CD<sub>3</sub>CN.

molecular dynamic modeling as well as DOSY NMR experiments.

**Physical Properties.** Given that triphenylamine motifs and tpy-metal complexes were extensively studied for optoelectronic application, <sup>52,59</sup> a series of experiments was performed to study photophysical and electrochemical properties of the complexes. Absorption spectra for complexes are shown in Figure S112. All the complexes exhibited the typical  $\pi \rightarrow \pi^*$  bands localized on the tpy-Ph subunits of ligands at around 285 and 325 nm because of intraligand charge transfer (<sup>1</sup>ILCT). The band formed at around 485 nm in G2, G3 and G5 is assigned to the Ru(II)-tpy moiety because of the metal-to-ligand charge transfer (MLCT) transitions.<sup>60</sup> All the five fractals also show a characteristic absorption band centered at 390 nm, which corresponds to the intramolecular charge transfer transition from the triphenylamine motif to the tpy-metal component.<sup>61,62</sup>

Oxidation and reduction properties of all the five fractals were studied using cyclic voltammetry (CV), and the results



Figure 10. TEM images of (a,c) G4 and (b,d) G5.



Figure 11. TEM images of nanostructures formed by (a) G4 and (b) G5 in solution and (c,d) proposed packing models (c for G4, d for G5).

were summarized in Figure S113. Two irreversible couples observed between -1.8 and -0.5 V are ascribed to the tpyligand-centered redox process, while overlapped by the broad peak from reduction process of triphenylamine motifs.<sup>52</sup> The Ru(II)/Ru(III) oxidation process of tpy-based complex occurred at 0.8–1.0 V according to the literature,<sup>63</sup> and the oxidation of the organic amine unit also occurred at around 1.0 and 1.2 V with broad peak corresponding to successive one electron removal.<sup>64,65</sup> That leads to an overlap in G2, G3 and G5 in the positive potential region.

Hierarchical Self-Assembly Behaviors. We investigated the hierarchical self-assembly behaviors of fractals G4 and G5 under different conditions. TEM imaging showed that G4 could further self-assemble into columnar nanostructures, which were bound together to form twisted fiber-like aggregates (Figure 11a) by diffusing THF into the solution of the complex (5 mg/mL in DMF) slowly. G5 also hierarchically assembled into a well-organized tubular structure under the same condition and the diameter (~12 nm) of nanostructures was close to that of the individual fractal G5 from energy-minimized structure by molecular modeling (Figure 11b). The formation of those ordered nanostructures were probably ascribed to the multiple intermolecular interactions such as  $\pi-\pi$  stacking, CH- $\pi$  hydrophobic/ hydrophilic interactions.<sup>66</sup> The proposed stacking models were displayed in Figures 11c and 11d. We speculated that the diameter and the orientation of the repeating units might result in the different hierarchical self-assembly behaviors of **G4** and **G5** in solution.

The hierarchical self-assembly behaviors of complexes G4 and G5 at liquid/solid interface were further investigated using scanning tunneling microscopy (STM). It is well-known that molecules could self-assemble into ordered 2D materials at liquid/solid interface through noncovalent interactions such as intermolecular, molecule-substrate, molecule-solvent, solvent-substrate interactions.<sup>67,68</sup> However, giant metallo-supramolecules were less explored because of the challenges in construction of large supramolecules with well-defined geometry. Furthermore, many previous studies reported that alkylated compounds tended to form ordered supramolecular assemblies on the highly oriented pyrolytic graphite (HOPG) surface due to their high affinities.<sup>69,70</sup> We herein reasoned that the giant complexes G4 and G5 with many alkyl chains on the rigid architectures could directly self-assemble into ordered 2D nanopattern on HOPG surface. Ambient STM imaging showed the formation of the anticipated honeycomb 2D supramolecular networks for both G4 (Figures 12a, 12b, and 12d) and G5 (Figures 12f, 12g, and 12i) after dropcasting of the fresh prepared solution onto HOPG surface. Obviously, the networks formed by G4 had higher resolution, which might result from its higher rigidity compared to G5.

More interestingly, with short incubation time, 1D supramolecular metal-organic nanoribbons (SMON)<sup>58,71</sup> with single-molecule width were also observed on HOPG surfaces (Figures 12e, 12h, and 12k). The SMON might grow along specific lattice direction of HOPG according to the reported gold(I) cyanide nanowires formed on graphene;<sup>72</sup> however, the current resolution by ambient STM was unable to provide more conclusive evidence. The achievements of those 2D networks and 1D orientated nanostructures on surfaces from giant supramolecular fractals might advance the study of surface chemistry for molecular-scale applications.<sup>73,74</sup>

#### CONCLUSIONS

In summary, five supramolecular architectures using triphenylamine and tpy moieties were successfully designed to demonstrate the concept of "supramolecular fractal". In preparation of the ligands, different approaches were applied to precisely control the geometry as well as increasing the complexity. Particularly, the extensive utilization of Sonogashira coupling reaction on the Ru(II)-tpy complexes was able to significantly increase the complexity of building blocks, and thus substantially increased the diversity and complexity of metallo-supramolecules. With such strategy, we were able to construct nontrivial architectures, particularly high generation of fractals, which were not achievable using conventional direct self-assembly approach. Their photophysical and electrochemical properties were investigated for further application study. Besides the self-assembly of the discrete structures, the hierarchical self-assembly of the largest fractals, G4 and G5 were also studied under different conditions. They were found to form tubular aggregates in solution while 2D networks and 1D orientated SMON on HOPG surface. Those unique



Figure 12. STM images of 2D networks formed by (a, b, d) G4 and (f, g, j) G5; 1D nanoribbons formed by (e) G4 and (h, k) G5 on HOPG (note that d, e, j are 3D STM images); energy-minimized structures for (c) G4 and (i) G5.

hierarchical self-assembly behaviors of the giant supramolecular architectures might broaden the avenue of novel materials such as semiconducting nanowires and 2D supramolecular networks for specific applications at molecular level.

#### ASSOCIATED CONTENT

#### **S** Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/jacs.8b05530.

Synthetic details, ligands and complexes characterization including <sup>1</sup>H NMR, <sup>13</sup>C NMR, 2D COSY, 2D NOESY, ESI-MS, TWIM-MS, UV–vis, CV, TEM and STM images (PDF)

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#### Notes

The authors declare no competing financial interest.

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