# Synthesis of new aryl and hetaryl dibromides and diiodides, the monomers for preparation of polyarylene ethynylenes 

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#### Abstract

Dibromides and diiodides with quinoxaline, phenylimidazole, and hexa- or pentaphenylarylene fragments were synthesized from dihalotolans obtained from chloral. Oligoarylene ethynylenes were synthesized by the reaction of the monomers with equimolar amounts of diethynyl aromatic compounds in the presence of the $\mathrm{Pd}^{\prime \prime}$ complex. Oligomers with imidazole and hexa(penta)arylbenzene cycles are soluble in amide organic solvents and their reduced viscosities do not exceed $0.09 \mathrm{dL} \mathrm{g}^{-1}$.


Key words: chloral; dihalotolans; dihalobenzils; quinoxaline; substituted phenylimidazoles; dibromocyclopentadienone; dibromohexaphenylbenzene; dibromopentaphenylbenzene; oligoarylene etynylenes.

Cross-coupling catalyzed by transition metal complexes ( Pd and Ni$)^{1}$ is one of the new methods for the synthesis of polyheteroarylenes and polyarylene ethynylenes, polymers with a polyconjugated structure.

Synthesis of polymers is usually based either on reactions of aromatic dibromides (diiodides) with bis-acetylenes, ${ }^{2,3}$ diboric acids ${ }^{4}$ or their esters, ${ }^{5}$ and bis(trialkylstannyl) compounds ${ }^{6}$ (the reactions mentioned are catalyzed by Pd complexes), or on homocondensations of aromatic or heterocyclic dichlorides (dibromides) in the presence of Ni complexes. ${ }^{7}$

The polycondensation cross-coupling allows one to synthesize a large number of different polymers with bulk groups in the main or side chain. The presence of such groups determines the solubility of polymers, which is important not only for their further conversion but mainly for the removal of the restriction for the growth of a macromolecular chain.

This work is devoted to the synthesis of heterocyclic and branched aromatic dibromides or diiodides. In most cases, the synthesis of monomers is based on the usage of chloral or dichloroacetal in initial steps of the synthesis.

The main intermediate products for the synthesis of the monomers mentioned are $4,4^{\prime}$-dihalotolans ( $1 \mathbf{a}, \mathrm{~b}$ ) and 4,4'-dihalobenzils (2a,b), where $X=\mathrm{Br}(\mathbf{a})$ or $\mathrm{I}(\mathbf{b})$.



1a,b

2a,b

Earlier ${ }^{8}$ compounds $\mathbf{1 a}, \mathbf{b}$ were synthesized according to Scheme 1. The yields of $4,4^{\prime}$-dibromotolan $1 \mathbf{1 a}$ and 4,4'-diiodotolan $\mathbf{l b}$ obtained from the corresponding diaryldichloroethane 3 were $\sim 75 \%$ and $35 \%$, respectively.

## Scheme 1





$X=\operatorname{Br}(a), I(b)$

Oxidation of dihalotolans $\mathbf{1 a}, \mathbf{b}$ readily affords dihalobenzils 2a,b (Scheme 2). ${ }^{9}$

## Scheme 2


$1 \mathrm{a}, \mathrm{b}$


We have developed a simpler scheme for the synthesis of compounds 1 and 2 (Scheme 3). Bromo(or iodo)benzene was treated with chloral, the product was reduced with zinc, and bromostilbene obtained was converted to 1,2-bis(4-bromophenyl)-1,2-dibromoethane (4a) with bromine or to the corresponding diiodo derivative $\mathbf{4 b}$ with iodine. Compound 4 a can also be readily obtained by the direct bromination of dibenzyl. Bis(bromophenyl)dihaloethane 4 a was converted to dibromotolan 1a or dibromobenzil $2 a$ by dehydrobromination with alcoholic alkali or by oxidation, respectively. The yield of 1 a at the final step of the synthesis was $84 \%$.

Using chloral, 4-bromobenzophenone (5) can be synthesized. The treatment of the latter with $\mathrm{TiCl}_{4}$ affords an interesting monomer, 1,2-bis(4-bromophenyl)-1,2diphenylethylene (6) (Scheme 4). Although compound 5 is obtained in four steps, all the reactions proceed in good yields (up to $90 \%$ ).

## Scheme 3



Scheme 4


Benzene was treated with a large ( $5-10$-fold) excess of chloral, the resulting product was introduced into the reaction with bromobenzene ( 1 mmol ), the intermediate was subjected to dehydrochlorination, and the product that formed was oxidized. The yield of olefin 6 after the treatment of bromobenzophenone 5 with $\mathrm{TiCl}_{4}$ was $84 \%$. This reaction was carried out by the procedure previously described for benzophenone. ${ }^{10}$

## Scheme 5




7a,b

Table 1. Characteristics of the synthesized monomers

| Compound | Yield <br> (\%) | $\begin{aligned} & \text { M.p. } \\ & /^{\circ} \mathrm{C} \end{aligned}$ | IR, $\mathrm{v} / \mathrm{cm}^{-1}$ | $\frac{\text { Found }}{\text { Calculated }} \text { (\%) }$ |  |  |  | Molecular formula |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | C | H | Br (I) | N |  |
| 12 | 84 | 182-183 |  | 49.83 | 2.22 | 47.94 |  | $\mathrm{C}_{14} \mathrm{H}_{8} \mathrm{Br}_{2}$ |
|  |  |  |  | 50.00 38.80 | 2.08 <br> 2.09 <br> 1.87 | 47.92 59.07 |  |  |
| .1b | 80 | 241-243* |  | 39.07 | 1.87 | 59.02 |  |  |
| 2a | 93 | 224-226 | 1680 | 46.25 | 2.22 | 44.17 |  | $\mathrm{C}_{14} \mathrm{H}_{8} \mathrm{O}_{2} \mathrm{Br}_{2}$ |
|  |  |  |  | 46.40 | 2.22 | 44.14 |  |  |
| 2b | 78 | 255-256 | 1680 | 36.52 | 1.85 | 54.66 |  | $\mathrm{C}_{14} \mathrm{H}_{8} \mathrm{O}_{2} \mathrm{I}_{2}$ |
|  |  |  |  | 36.39 | 1.74 | 54.93 |  |  |
| 6 | 84 | 198-199 |  | 63.50 | 3.77 | 32.39 |  | $\mathrm{C}_{26} \mathrm{H}_{18} \mathrm{Br}_{2}$ |
|  |  |  |  | 63.69 | 3.70 | 32.60 |  |  |
| 7 a | 85 | 345-347 |  | 72.77 | 4.00 | 23.16 |  | $\mathrm{C}_{42} \mathrm{H}_{28} \mathrm{Br}_{2}$ |
|  |  |  |  | 72.84 | 4.08 | 23.08 |  |  |
| 7b | 88 | >350 |  | 64.04 | 4.02 | 31.92 |  | $\mathrm{C}_{42} \mathrm{H}_{28} \mathrm{I}_{2}$ |
|  |  |  |  | 64.14 | 3.59 | 32.27 |  |  |
| $8 \mathbf{}$ | 92 | 197-199 | $1620-$ | 55,02 | 2.87 | 36.36 | 5.86 | $\mathrm{C}_{20} \mathrm{H}_{12} \mathrm{~N}_{2} \mathrm{Br}_{2}$ |
|  |  |  | 1640 | 54.58 | 2.74 | 36.32 | 6.36 |  |
| 8b | 85 | 187-188 | $1620-$ | 45,11 | 2.17 | 47.64 | 5.04 | $\mathrm{C}_{20} \mathrm{H}_{12} \mathrm{~N}_{2} \mathrm{I}_{2}$ |
|  |  |  | 1640 | 44.97 | 2.26 | 47.52 | 5.25 |  |
| 9 | 92 | 240-242 | 1670 | 64.08 | 3,39 | 29.61 |  | $\mathrm{C}_{29} \mathrm{H}_{18} \mathrm{OBr}_{2}$ |
|  |  |  |  | 64.23 | 3.34 | 29.47 |  |  |
| 10 | 81 | 245-247 |  | 70.56 | 3.51 | 25.80 |  | $\mathrm{C}_{36} \mathrm{H}_{23} \mathrm{Br}_{2}$ |
|  |  |  |  | 70.26 | 3.77 | 25.97 |  |  |
| 11 | 84 | 312-314 | 3300 | 55.62 | 3.20 | 35.24 | 6.12 | $\mathrm{C}_{21} \mathrm{H}_{14} \mathrm{~N}_{2} \mathrm{Br}_{2}$ |
|  |  |  |  | 55.50 | 3.08 | 35.06 | 6.17 |  |
| 12 | 87 | 342-344 | 3300, | 50.82 | 2.73 | 32.06 | 8.21 | $\mathrm{C}_{21} \mathrm{H}_{13} \mathrm{~N}_{3} \mathrm{O}_{2} \mathrm{Br}_{2}$ |
|  |  |  | 1540 | 50.50 | 2.61 | 31.62 | 8.42 |  |

* Literature data: ${ }^{8}$ m.p. $240-241^{\circ} \mathrm{C}$.

Dibromosubstituted hexaarylbenzene 7 was obtained by Diels-Alder reaction ${ }^{11}$ by refluxing compound 1 in benzophenone with tetraphenylcyclopentadienone (tetracyclone) (Scheme 5) in $85 \%$ yield (Table 1).

The synthesis of monomers from $4,4^{\prime}$-dihalobenzil 2 was carried out by the three methods (Scheme 6).

1. The reactions of dibromide $\mathbf{2 a}$ and diiodide $\mathbf{2 b}$ with o-phenylenediamine ${ }^{12}$ afford 2,3-di(4-bromophenyl)quinoxaline (8a) and 2,3-di(4-iodophenyl)quinoxaline ( 8 b ), respectively, in $>80 \%$ yields.
2. The reaction of compound $2 \mathbf{2 a}$ with dibenzylketone ${ }^{13-15}$ affords dihalosubstituted tetracyclone 9. The reaction of the latter with tolan and phenylacetylene gives hexaarylbenzene 7 and pentaarylbenzene 10 (in $81 \%$ yield), respectively.
3. The treatment of compound 2 a with aldehydes in the presence of ammonium acetate and acetic acid ${ }^{16}$ results in the formation of substituted bromoimidazoles 11 and 12 in $>80 \%$ yield.

Oligoarylene ethynylenes based on synthesized dibromo-containing monomers were obtained by the procedure described earlier ${ }^{2,3}$ using $p$ - and $m$-diethynylbenzene and $4,4^{\circ}$-diethynyldiphenyloxide as co-monomers (Scheme 7). The reactions were carried out in dimethylacetamide (DMAA) at $110^{\circ} \mathrm{C}$ for 6 h , the catalytic system was the following: $\mathrm{PdCl}_{2}\left(\mathrm{Ph}_{3} \mathrm{P}\right)_{2}(1-2 \mathrm{~mol} . \%)+\mathrm{CuI}$ $(3 \mathrm{~mol} . \%)+\mathrm{Ph}_{3} \mathrm{P}(5-6 \mathrm{~mol} . \%)+\mathrm{Et}_{3} \mathrm{~N}(5-6 \mathrm{~mol} . \%)$.

Oligomers 13-18 (Table 2) were precipitated from the reaction solutions and did not further dissolve in any organic solvents. The average polymerization degrees did not exceed 4 judging from the content of bromine. The previously obtained ${ }^{2}$ polymer with a structure very close to that of 13 was insoluble and probably had a low molecular weight.

Introduction of $m$-phenylene and diphenyloxide groups instead of $p$-phenylene ones did not effect the solubility of polymers $16-18$ containing quinoxaline cycles.

We supposed that soluble oligophenylene ethynylene vinylenes may be obtained from monomer 6. However, they also appeared to be insoluble though their molecular weight was somewhat higher than that of the oligomers described previously, judging from the content of bromine.

Oligomers with imidazole and hexa(penta)arylbenzene cycles 19-22 are readily soluble in DMF and other amide solvents. The viscosities of the polymers obtained to date are not very high ( $\eta_{\text {red }}$ up to $0.09 \mathrm{dL} \mathrm{g}^{-1}$, see Table 2), but studies along this line are in progress.

## Experimental

IR spectra were obtained on a UR-20 instrument in KBr pellets. We used 4 -bromobenzophenone (m.p. $80-82^{\circ} \mathrm{C}$ ).

Scheme 6


Scheme 7




1,2-diphenylethane (m.p. $50-53^{\circ} \mathrm{C}$ ), tetraphenyl cyclopentadienone (m.p. 217-220 ${ }^{\circ} \mathrm{C}$ ), o-phenylene diamine (m.p. 103$105^{\circ} \mathrm{C}$ ), dibenzylketone (m.p. $32-34^{\circ} \mathrm{C}$ ), benzaldehyde ( $n_{\mathrm{D}}{ }^{20}$ 1.5450 ), and $p$-nitrobenzaldehyde (m.p. $105-107^{\circ} \mathrm{C}$ ) of "pure" grade. 1,2-Bis(4-bromophenyl)-1,2-dibromoethane (m.p. 245$247{ }^{\circ} \mathrm{C}$ ) was synthesized by the previously described procedure. ${ }^{17}$

4,4-Dibromotolan (1a). A solution of 1,2-di(4-bromo-phenyl)-1,2-dibromoethane (4a) ( $20 \mathrm{~g}, 0.04 \mathrm{~mol}$ ) in abs. ethanol ( 50 mL )'was added to a solution of $\mathrm{NaOH}(19 \mathrm{~g})$ in abs. ethanol $(300 \mathrm{~mL})$. The solution was refluxed for 2 h , cooled, and poured into watef. The precipitate formed was filtered off, washed with ethanol, dried, and crystallized from dioxane to afford 19 in $84 \%$ yield, m.p. $182-183^{\circ} \mathrm{C}$ (cf. Ref. 8: m.p. 182-184 ${ }^{\circ} \mathrm{C}$ ).

4,4'-Dibromobenzil (2a). A. A mixture of compound la (2.1 $\mathrm{mmol}), \mathrm{I}_{2}(0.25 \mathrm{~g}, 1 \mathrm{mmol})$, and DMSO ( 5 mL ) was heated at $155^{\circ} \mathrm{C}$ for 6 h with stirring. Then the reaction mixture was cooled and poured into a $1 \%$ solution of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}(20 \mathrm{~mL})$. Yellow crystals that precipitated were filtered off, washed with water, dried, and crystallized from dioxane to give $2 a$ in $93 \%$ yield, m.p. $224-226^{\circ} \mathrm{C}$.

4,4'-Diiodobenzil (2b) was obtained by a similar procedure in $78 \%$ yield, m.p. $255-260^{\circ} \mathrm{C}$ (cf. Ref. 18: m.p. $254-256^{\circ} \mathrm{C}$ ).

4,4'-Dibromobenzil (2a). B. DMSO ( 1500 mL ) and HBr $(150 \mathrm{~mL})$ were added to compound $42(150 \mathrm{~g}, 0.3 \mathrm{~mol})$ and the reaction mixture was slowly heated to $110^{\circ} \mathrm{C}$ with stirring. At this temperature the starting compound was completely dissolved. The reaction was carried out at $110^{\circ} \mathrm{C}$ for 9 h . After 0.5 h , the precipitation of 2 a started. The reaction mixture was then cooled, and the yellow crystals that precipitated were filtered off, dried, and crystallized from dioxane to afford $2 a$ in $80 \%$ yield, m.p. $225-226^{\circ} \mathrm{C}$ (cf. Ref. 19: m.p. 224-226 ${ }^{\circ} \mathrm{C}$ ).

1,2-Di(4-bromophenyl)-1,2-diphenylethylene (6). $\mathrm{TiCl}_{4}$ $(5 \mathrm{~mL})$ was added to a solution of 4 -bromobenzophenone ( 5 ) $(7.80 \mathrm{~g}, 0.03 \mathrm{~mol})$ in THF ( 200 mL ) at $-10^{\circ} \mathrm{C}$. Then a suspension of zinc powder ( $5.9 \mathrm{~g}, 0.09 \mathrm{~mol}$ ) in THF ( 100 mL ) was added dropwise to the reaction mixture at the same temperature. The reaction mixture was heated to boiling, refluxed for 5 h
with stirring, and then cooled. The resulting solution was filtered, and the filtrate was poured into water and extracted with ether. The organic layer was washed with water, dried, and the solvents were distilled off. The product was crystallized from $n$-butanol to afford 6 in $84 \%$ yield, m.p. $198-199^{\circ} \mathrm{C}$ (cf. Ref. 20: m.p. 198-199 ${ }^{\circ} \mathrm{C}$ ).

1,2-Di(4-bromophenyl)-3,4,5,6-tetraphenylbenzene (7). Melted benzophenone ( 5 g ) was mixed with compound 1 ( 1.9 g , 5.65 mmol ) and tetracyclone ( $1 \mathrm{~g}, 2.6 \mathrm{mmol}$ ) at $50^{\circ} \mathrm{C}$. The mixture was heated at vigorous boiling ( $305^{\circ} \mathrm{C}$ ) for 1 h . Diphenyl ether ( 1 g ) was then added to the reddish-brown reaction mixture. The crystals formed were filtered off, washed with benzene to a white color, then with methanol, and dried in vacuo. The product was crystallized from diphenyl ether (the residual solvent was extracted with ethanol) to afford 7 in $85 \%$ yield, m.p. $345-347^{\circ} \mathrm{C}$.

1,2-Di(4-bromophenyl)quinoxaline (8a) was synthesized by the previously described procedure, ${ }^{12}$ m.p. $197-199^{\circ} \mathrm{C}$ (cf. Ref. 12: m.p. 198-199 ${ }^{\circ} \mathrm{C}$ ).

1,2-Di(4-iodophenyl)quinoxaline (8b) was synthesized by the same procedure, ${ }^{12}$ m.p. $187-188^{\circ} \mathrm{C}$ (cf. Ref. 12: m.p. $188-189^{\circ} \mathrm{C}$ ).

2,3-Di(4-bromophenyl)-1,4-diphenylcyclopentadienone (9) was synthesized by the previously described procedure, ${ }^{15}$ m.p. $240-242^{\circ} \mathrm{C}$ (cf. Ref. 15 : m.p. $240-242^{\circ} \mathrm{C}$ ).

2-Phenyl-4,5-di(4-bromophenyl)imidazole (11). Glacial acetic acid ( 100 mL ) was added to a mixture of compound $2 \mathrm{a}(5 \mathrm{~g}$, 13.6 mmol ) and ammonium acetate ( $10.5 \mathrm{~g}, 135 \mathrm{mmol}$ ) in argon flow. The reaction mixture was heated to $100^{\circ} \mathrm{C}$, then benzaldehyde ( $1.4 \mathrm{~mL}, 13.6 \mathrm{mmol}$ ) was added dropwise, and the solution was refluxed at $118^{\circ} \mathrm{C}$ for 5.5 h . The mixture was cooled and poured into water, and the precipitate formed was filtered off, washed with ethanol, dried, and crystallized from $n$-butanol to afford 11 in $84 \%$ yield, m.p. $312-314^{\circ} \mathrm{C}$.

2-Nitrophenyl-4,5-di(4-bromophenyl)imidazole (12) was synthesized by the similar procedure in $87 \%$ yield, m.p. $342-344^{\circ} \mathrm{C}$.

Table 2. Properties of the obtained polymers

| Com- <br> pound | Main polymer unit | Yield <br> $(\%)$ | Found <br> Calculated <br> (\%), <br> Br |
| :--- | :---: | :---: | :---: |

[^0]Table 2 (continued)

| Com- <br> pound | Main polymer unit | Yield <br> (\%) |
| :--- | :--- | :--- |

16

$72 \quad \frac{11.78}{7.87} \quad$ Insoluble

17


69


The same

18


70
11.63


58
16.99
8.99
0.09

19

16.99
8.99

The same

60
13.21
8.57
0.07

20

$65 \quad \frac{11.21}{5.74}$
0.08

21




68
$\frac{16.09}{6.45}$
0.06

[^1]1,2-Di(4-bromophenyl)-3,4,6-triphenylbenzene (10). Compound $9(2 \mathrm{~g}, 3.69 \mathrm{mmol})$, phenylacetylene ( $0.94 \mathrm{~g}, 9.23 \mathrm{mmol}$ ), and $o$-dichlorobenzene ( 15 mL ) were put into a two-necked flask with stirrer and reflux condenser and the mixture was refluxed for 32 h . The reaction solution was then cooled and poured into ethanol ( 100 mL ), and the precipitate formed was filtered off and crystallized from $n$-butanol to afford 10 in $81 \%$ yield, m.p. $245-247^{\circ} \mathrm{C}$.

Synthesis of oligomers (general procedure). Compound 8a ( $0.4416 \mathrm{~g}, 1 \mathrm{mmol}$ ), $4,4^{\prime}$-diethynylbenzene ( $0.1004 \mathrm{~g}, 1 \mathrm{mmol}$ ), $\mathrm{PdCl}_{2}\left(\mathrm{Ph}_{3} \mathrm{P}_{2}(0.0021 \mathrm{~g}), \mathrm{Ph}_{3} \mathrm{P}(0.0042 \mathrm{~g}), \mathrm{DMAA}(1.5 \mathrm{~mL})\right.$, and $\mathrm{Et}_{3} \mathrm{~N}^{2}(0.5 \mathrm{~mL})$ were put into a flask with stirrer and an inlet and outlet for argon and the mixture was heated to $110^{\circ} \mathrm{C}$. Then CuI $(0.0021 \mathrm{~g})$ was added and the reaction mixture was stirred for 6 h at this temperature. The mixture was cooled and poured into methanol ( 10 mL ), and the precipitate formed was filtered, washed twice with water, 5 M HCl , water, and methanol, and dried.

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[^0]:    13
    

    14
    

    | $\frac{10.65}{11.75}$ | Insoluble |
    | :--- | :--- |
    | $\frac{12.67}{10.33}$ | The same |

    15
    

[^1]:    * Calculated for $n=4$.

