Pyridine and phosphonate containing ligands for stable lanthanide complexation. An experimental and theoretical study to assess the solution structure[†]

Marta Mato-Iglesias,^a Edina Balogh,^b Carlos Platas-Iglesias,^{*a} Éva Tóth,^{b,c} Andrés de Blas^{*a} and Teresa Rodríguez Blas^a

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We report an experimental and theoretical study of the stability and solution structure of lanthanide complexes with two novel ligands containing pyridine units and phosphonate pendant arms on either ethane-1,2-diamine (L2) or cyclohexane-1,2-diamine (L3) backbones. Potentiometric studies have been carried out to determine the protonation constants of the ligands and the stability constants of the complexes with Gd^{III} and the endogenous metal ions Zn^{II} and Cu^{II}. While the stability constant of the GdL² complex is too high to be determined by direct pH-potentiometric titrations, the cyclohexyl derivative GdL³ has a lower and assessable stability (log $K_{GdL^3} = 17.62$). Due to the presence of the phosphonate groups, various protonated species can be detected up to $pH \approx 8$ for both ligands and all metal ions studied. The molecular clusters $[Ln(L)(H_2O)]^{3-}\cdot 19H_2O$ (Ln = La, Nd, Ho or Lu; L = L² or L^3) were characterized by theoretical calculations at the HF level. Our calculations provide two minimum energy geometries where the ligand adopts different conformations: twist-wrap (tw), in which the ligand wraps around the metal ion by twisting the pyridyl units relative to each other, and twist-fold (tf), where the slight twisting of the pyridyl units is accompanied by an overall folding of the two pyridine units towards one of the phosphonate groups. The relative free energies of the tw and tf conformations of $[Ln(L)(H_2O)]^{3-}$ (L = L², L³) complexes calculated in aqueous solution (C-PCM) by using the B3LYP model indicate that the tw form is the most stable one along the whole lanthanide series for the complexes of L^3 , while for those of L^2 only the Gd^{III} complex is more stable in the *tf* conformation by ca. 0.5 kcal mol⁻¹. ¹H NMR studies of the Eu^{III} complex of L³ show the initial formation of the tf complex in aqueous solution, which slowly converts to the thermodynamically stable tw form. The structures calculated for the Nd^{III} complexes are in reasonably good agreement with the experimental solution structures, as demonstrated by Nd^{III}-induced relaxation rate enhancement effects in the ¹H NMR spectra.

Introduction

Coordination chemistry of lanthanide complexes in aqueous solution has been the subject of intense research efforts over the past ten years.¹ In particular, lanthanide complexes with poly(aminocarboxylate) ligands present considerable interest due to their application as contrast agents for magnetic resonance imaging (MRI),^{2,3} or responsive luminescent lanthanide complexes.⁴ Within the last decade, MRI has become one of the most powerful tools for medical diagnosis. The development of this

^bLaboratoire de Chimie Inorganique et Bioinorganique, Ecole Polytechnique Fédérale de Lausanne, BCH, CH-1015, Lausanne, Switzerland technique is related to the successful use of paramagnetic agents, mainly Gd^{III} complexes, which enhance the intrinsic contrast of the magnetic resonance images by preferentially influencing the relaxation efficiency of the water proton nuclei in the target tissue. These complexes contain at least one Gd^{III}-bound water molecule that rapidly exchanges with the bulk water of the body, which imparts an efficient mechanism for the longitudinal and transverse relaxation (T_1 and T_2) enhancement of water protons. Contrast agents must be stable enough to avoid the *in vivo* release of toxic free Gd^{III}. The ligands used must also show a good selectivity for Gd^{III} over other metal ions present in body fluids such as the most abundant Zn^{II}.

In a recent work,⁵ we reported a new receptor containing pyridine units and carboxylate pendants (H_4L^1 , Scheme 1), which forms relatively stable complexes with Ln^{III} ions in aqueous solution.⁶ In these complexes, the Ln^{III} ion is nine-coordinate, where a water molecule completes the metal ion coordination sphere. This induces a relaxivity in solutions of the complex at the imaging fields comparable to those reported for standard contrast agents such as $[Gd(DOTA)(H_2O)]^-$ (DOTA⁴⁻ = 1,4,7,10-tetraaza-cyclododecane-1,4,7,10-tetraacetate) and $[Gd(DTPA)(H_2O)]^{2-}$

^aDepartamento de Química Fundamental, Universidade da Coruña, Alejandro de la Sota 1, 15008 A, Coruña, Spain. E-mail: cplatas@udc.es

^cCentre de Biophysique Moléculaire, CNRS, rue Charles-Sadron, 45071 Orléans, Cedex 2, France

[†] Electronic supplementary information (ESI) available: Optimized Cartesian coordinates (Å) of the $[Ln(L)(H_2O)]^{3-.19H_2O}$ (Ln = La, Nd, Gd, Ho or Lu; L = L² or L³) and $[Lu(L)]^{3-.20H_2O}$ (L = L² or L³) systems; hydrogen bonding data for $[Gd(L)(H_2O)]^{3-.19H_2O}$ and $[Lu(L)]^{3-.20H_2O}$ (L = L² or L³) systems; Fig. S1: ¹H NMR spectrum of the Eu^{III} complex of L². See DOI: 10.1039/b611544f



Scheme 1

 $(DTPA^{5-} = diethylenetriamine-N, N, N', N'', N'')$ -pentaacetate). In previous papers, we have reported two new ligands (H_6L^2 and H_6L^3 , Scheme 1) designed for stable complexation of lanthanide ions.^{7,8} The corresponding Gd^{III} complexes present an extremely high water exchange rate of the inner sphere water molecule, an important parameter to be optimized for the design of new, more effective, MRI contrast agents. In the present work we report an experimental and theoretical study of the complexation properties of ligands H_6L^2 and H_6L^3 towards lanthanide and some divalent ions. Ligand H_6L^2 maintains the same basic structure as H_4L^1 , but the acetate pendants have been replaced by phosphonic acid pendant arms, while ligand H_6L^3 contains the same structural backbone as H₆L² with the ethyl bridge being substituted by a more rigid cyclohexyl moiety. This structural modification has been shown to have an important effect on the water exchange rate of the inner sphere water molecule.8 In this work, the corresponding lanthanide complexes were characterized by ¹H and ¹³C NMR techniques in D₂O solution. Thermodynamic stability constants of the Gd^{III} complexes of these ligands have been determined by pH potentiometry. Stability studies on the complexes of these ligands with some endogenously available metal ions, such as Cu^{II} and Zn^{II} are also reported. In addition, the complexes were characterized by ab initio calculations carried out at the HF level. These calculations were performed on molecular clusters with formula $[Ln(L)(H_2O)]^{3-} \cdot 19H_2O$ and $[Ln(L)]^{3-} \cdot 20H_2O$ (L = L², L³). Calculations on molecular clusters have the advantage of providing useful direct information about the second sphere solvation shell, which has been shown to enhance the relaxivity of Gd^{III} chelates bearing phosphonate groups.9,10 The structures established by these calculations were compared with the structural information obtained in solution from paramagnetic NMR measurements (Nd^{III}-induced relaxation rate enhancement effects).

Experimental

Ligands H_6L^2 and H_6L^3 were prepared as described previously.⁸ The nitrate salts, $Ln(NO_3)_3 \cdot nH_2O$, were from Alfa Laboratories, and were used without further purification. D₂O for NMR studies was obtained from Merck (99.9% D).

NMR measurements

¹H, ¹³C and ³¹P NMR spectra were run on Bruker AC200 F or Bruker Avance 300 spectrometers. Chemical shifts are reported in δ values. For measurements in D₂O, *tert*-butyl alcohol was used as an internal standard with the methyl signal calibrated at $\delta = 1.2$ (¹H) and 31.2 ppm (¹³C). Spectral assignments were based in part on two-dimensional COSY, HMQC and HMBC experiments. Longitudinal ¹H relaxation times T_1 were measured by the inversion–recovery pulse sequence.¹¹ Samples of the Ln^{III} complexes for NMR measurements were prepared by dissolving equimolar amounts of the ligand and hydrated Ln(NO₃)₃ in D₂O, followed by adjustment of the pD with ND₄OD and DCl (Aldrich) solutions in D₂O. The pH of the solutions was measured at room temperature with a calibrated microcombination probe purchased from Aldrich Chemical Co. The pH values were corrected for the deuterium isotope effect using the relationship pH = pD – 0.4.¹²

Potentiometry

The stock solution of GdCl₃ was made by dissolving Gd₂O₃ in a slight excess of concentrated HCl in double distilled water. The excess of aqueous HCl solution was removed by evaporation. Stock solutions of Zn^{II} and Cu^{II} were prepared from ZnCl₂ and CuSO₄ salts in double distilled water. The concentration of the solutions was determined by complexometric titration with a standardized Na₂H₂EDTA solution (H₄edta = ethylenediaminetetraacetic acid) using xylenol orange as indicator (Zn^{II}, Gd^{III}) or by gravimetry (Cu^{II}). Ligand stock solutions were prepared in double distilled water using KOH to increase the pH up to 4 in order to avoid precipitation. The exact ligand concentrations were determined by adding excess of GdCl₃ to the ligand solution and titrating back the metal excess with standardized Na₂H₂EDTA.

Ligand protonation constants and stability constants with Zn^{II}, Cu^{II} and Gd^{III} were determined by pH-potentiometric titration at 25 °C in 0.1 M KCl. The samples (2 or 3 ml) were stirred while a constant N₂ flow was bubbled through the solutions. The titrations were carried out adding standardized KOH solution with a Methrom Dosimat 665 automatic burette. A combined glass electrode (C14/02-SC, reference electrode Ag/AgCl in 3 M KCl, Moeller Scientific Glass Instruments, Switzerland) and a Metrohm 692 pH/ion-meter were used to measure pH. The H⁺ concentration was obtained from the measured pH values using the correction method proposed by Irving *et al.*¹³ The protonation and stability constants were calculated from parallel titrations with the program PSEQUAD.¹⁴ The errors given correspond to one standard deviation.

Computational methods

Full geometry optimizations of the $[Ln(L)(H_2O)]^{3-}\cdot 19H_2O$ (Ln = La, Nd, Eu, Gd, Ho or Lu) and $[Lu(L)]^{3-}\cdot 20H_2O$ (Ln = Lu) systems were performed *in vacuo* at the RHF level (L = L² or L³). For these calculations the effective core potential (ECP) of Dolg *et al.*¹⁵ and the related [5s4p3d]-GTO valence basis set were used for the lanthanides, while the 3-21G* basis set was used for the ligand atoms. The stationary points found on the potential energy surfaces as a result of the geometry optimizations have been tested to represent energy minima rather than saddle points *via* frequency analysis.

The relative free energies of the twist-wrap (*tw*) and twist-fold (*tf*) conformations of $[Ln(L)(H_2O)]^{3-}$ complexes were calculated in aqueous solution at the DFT (B3LYP functional)¹⁶ level, by using the 6-311G** basis set for the ligand atoms. In these calculations second-sphere water molecules were excluded, and solvent effects were included by using the polarizable continuum model (PCM). In particular, we used the C-PCM variant¹⁷ that,

employing conductor rather than dielectric boundary conditions, allows a more robust implementation. The solute cavity is built as an envelope of spheres centered on atoms or atomic groups with appropriate radii. Each sphere is subdivided in 60 initial tesserae in pentakisdodecahedral patterns. For the lanthanides the previously parametrized radius was used.¹⁸ Final free energies include both electrostatic and non-electrostatic contributions.

The NMR shielding tensors (GIAO¹⁹ method) of the $[La(L)(H_2O)]^{3-}$ (L = L² or L³) systems were calculated in aqueous solution at the B3LYP functional level by using the ECP of Stevens *et al.*^{20,21} and the 6-311G** basis set for the ligand atoms. For chemical shift calculation purposes, NMR shielding tensors of tetramethylsilane (TMS) were calculated at the same computational level. All HF and DFT calculations were performed by using the Gaussian 98 (Revision A.11.3)²² and Gaussian 03 (Revision C.1) program packages.²³

Results and discussion

Ligand protonation constants and stability constants of the metal complexes

The protonation constants of ligands L^2 and L^3 as well as the stability constants of their metal complexes formed with different metals (Gd^{III}, Zn^{II} and Cu^{II}) were determined by potentiometric titration; the constants and standard deviations are given in Table 1. Table 1 also lists the protonation constants of L¹ and the stability constant of its Gd^{III} complex reported by Mazzanti *et al.*⁶ The ligand protonation constants are defined as in eqn (1), and the stability constants of the complexes are expressed in eqn (2) and (3), respectively.

$$K_i = [H_i L] / [H_{i-1} L] [H^+]$$
(1)

$$K_{\rm ML} = [\rm ML]/[\rm M][\rm L]$$
⁽²⁾

Table 1 Protonation constants of the ligands and stability constants of their metal complexes (25 °C; I = 0.1 M KCl)

	$L^{1 a}$	L^2	L^3	
$\log K_1$	8.5	10.21(2)	10.03(3)	
$\log K_2$	5.2	8.84(3)	9.69(2)	
$\log K_3$	3.5	6.59(4)	5.88(4)	
$\log K_4$	2.9	5.16(4)	5.08(4)	
$\log K_5$		3.94(4)	4.39(4)	
$\log K_6$		1.4(1)	3.20(4)	
$\log K_{\rm GdL}$	15.1	b	17.62(8)	
$\log K_{\rm GdHL}$		6.01(3)	6.61(7)	
$\log K_{\rm GdH_2}$		5.00(5)	5.41(8)	
$\log K_{GdH_{2}}$			4.86(4)	
$\log K_{ZnL}$		Ь	b	
$\log K_{\rm ZnHL}$		6.94(7)	6.84(1)	
$\log K_{\rm ZnH_2L}$		6.60(4)	6.01(1)	
$\log K_{\rm ZnH_2L}$			5.13(2)	
$\log K_{CuL}$		Ь	18.17(8)	
$\log K_{\rm CuHL}$		7.08(7)	7.7(1)	
$\log K_{\rm CuH_2L}$		6.77(5)	7.03(5)	

^{*a*} From ref. 6. ^{*b*} The complex is too stable to determine the stability constant by direct titration.

$$K_{\rm MH_{iL}} = [\rm MH_{i}L]/[\rm MH_{i-1}L][\rm H^{+}]; i = 1, 2, 3$$
 (3)

In comparison with L^1 , the L^2 and L^3 ligands have higher protonation constants for the first and second protonation steps, which occur on the amine nitrogen atoms.⁶ Thus, replacement of the acetate pendants of L^1 by methylphosphonate groups leads to an important increase in the basicity of the two amine nitrogen atoms. The first protonation constant of L^2 and L^3 is very similar to that reported for ethylenediaminediphosphonic acid (EDDP, $\log K_1 = 10.29$), while the second protonation constant is higher in L^2 and L^3 than in EDDP ($\log K_2 = 7.85$).²⁴ The third and fourth protonation steps of L^2 and L^3 correspond to partial protonation of the phosphonate groups, which occur at slightly higher pH than in EDDP ($\log K_3 = 5.40$, $\log K_4 = 4.35$).²⁴ The last two protonation steps probably correspond to the protonation of the pyridylcarboxylate groups.⁶

Potentiometric titrations of the L^2 and L^3 ligands have been carried out in the presence of equimolar Gd^{III} in order to determine the stability constants of the metal complexes. The analysis of the titration curve for GdL² shows that already at the beginning of the titration (pH \sim 2), there is no free Gd^{III}, all metal being in the form of the diprotonated complex. Therefore, we could not calculate the stability constant for this complex; only an estimation of $\log K_{GdL^2} > 20$ can be made. Both mono- and diprotonated forms of the Gd^{III} complex have been detected over the pH range studied. These protonation steps are expected to occur on the phosphonate groups. Partial protonation of phosphonate groups in solution has been observed previously for Ln^{III} complexes with both cyclic^{25,26} and acyclic⁹ ligands. The species distribution diagram for the GdL² system (Fig. 1) shows the presence of monoprotonated complex in solution at pH < 8, while the second protonation of the complex occurs at pH < 7.

The species distribution curves obtained for GdL³ (Fig. 1) indicate dissociation of the complex at low pH, which allowed us to determine the stability constant for this complex. This result points to a lower stability of the Gd^{III} complex of L³ in comparison to that of L². Thus, increasing the rigidity of the ligand lowers the stability of the corresponding Gd^{III} complex. The stability constant obtained (log $K_{GdL}^3 = 17.62$, Table 1) is approximately 2 log units higher than that of GdL¹,⁶ and similar to that reported for GdEDTA (log $K_{GdL} = 17.37$).²⁷

 Cu^{II} and Zn^{II} complexes are found to be highly stable with both L^2 and L^3 ; a quantitative assessment by direct potentiometry was only possible for CuL^3 (Table 1). As for the Gd^{III} analogues, protonated complexes are present in all systems in an extended pH range.

Non-toxicity is primordial for *in vivo* application of Gd^{III} (or other metal) complexes as MRI contrast agents. It is evident that competitive equilibria cannot solely explain the *in vivo* behavior of Gd^{III} complexes. The excretion of low molecular weight Gd^{III} chelates from the body is very rapid ($t_{1/2} = 1.6$ h for Gd(DTPA)²⁻), whereas the dissociation and transmetallation of the Gd^{III} complexes can be relatively slow. Therefore, the system is far from equilibrium, and kinetic factors must be considered²⁸⁻³⁰ A detailed kinetic investigation was beyond the scope of this study. However, we know that the present complexes protonate readily and the protonated species are expected to have modest kinetic stability with respect to proton mediated decomplexation, as it



Fig. 1 Species distribution of the GdL² (top) and GdL³ (bottom) systems, $1:1 \text{ Gd}^{III}: L; [Gd^{III}] = 1 \text{ mM}, \mu = 0.1 \text{ M}$ (KCl), T = 25 °C.

was recently shown for DTPA analogues with a phosphonic acid pendant arm. $^{\rm 31}$

NMR spectra

The ¹H, ³¹P and ¹³C NMR spectra of the La^{III} complexes of L² and L^3 were obtained in D_2O solution at pH = 7.6. At this pH the major species in solution is expected to be the fully deprotonated form $[Ln(L)(H_2O)_n]^{3-}$, as demonstrated by our potentiometric measurements (see above). The proton spectra (Fig. 2) consist of 9 (L^2) and 12 (L^3) signals corresponding to the different proton magnetic environments of the ligand molecule (see Scheme 1 for labelling scheme). This points to an effective C_2 symmetry of the complexes in solution that is confirmed by the ¹³C spectra, which show nine NMR peaks for the 18 carbon nuclei of L² and 11 signals for the 22 carbon nuclei of L^3 in the corresponding complexes. The ¹³C NMR spectra show two doublets for the phosphonate carbon atoms C8 (${}^{2}J_{C8-P} \sim 140$ Hz) and C7 (${}^{3}J_{C7-P} \sim 16$ Hz). Similar coupling constants have been observed for other La^{III} complexes with ligands containing phosphonate groups.³² The ³¹P NMR spectra recorded at 298 K show a single peak at *ca*. 17 ppm, again in agreement with an effective C_2 symmetry of the complexes in solution. The assignments of the proton signals (Table 2) were aided with standard 2D homonuclear COSY experiments, which gave strong cross-peaks between the geminal CH₂-protons



Fig. 2 ¹H NMR spectra of the La^{III} complexes of L² (top) and L³ (bottom) recorded in D₂O solutions (30 mM, pH = 7.6, 298 K).

and between ortho-coupled pyridyl protons. A full assignment of the 1H and 13C NMR spectra was achieved with the aid of 2D heteronuclear HMOC and HMBC experiments. The HMBC spectra show a signal relating H5 with one of the aliphatic carbon nuclei of the ligand backbone, which was therefore assigned to C7. The signals corresponding to protons H8 could be easily identified due to the presence of important ${}^{2}J_{H-P}$ couplings (ca. 6 Hz, Table 2). Protons H7 and H8 yield two multiplets, consisting of the AB part of a ABX spectrum (X is the ³¹P nucleus). Although the specific CH₂ proton assignments H9ax/H9eq, H8a/H8b and H7ax/H7eq, were not possible on the basis of the 2D NMR spectra, they were carried out using the stereochemically dependent proton shift effects, resulting from the polarization of the C-H bonds by the electric field effect caused by the cation charge.³³ This results in a deshielding effect of the H9eq, H7eq and H8b protons, which are pointing away from the La^{III} ion.

The ¹H NMR spectra of the diamagnetic Lu^{III} complexes recorded at 298 K are more complex than those of the corresponding La^{III} analogues. Although this complexity prevented

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Table 2 ¹H shifts (ppm) for the Ln^{III} complexes of L^2 and L^3 in 30 mM D_2O solutions at pH 7.6

	La ^{III}	a	Ce ^{III}		Nd ^{III}		Eu ^{III}	
	$\overline{\mathbf{L}^{2 \ b}}$	L ^{3 c}	$\overline{L^2}$	L ³	$\overline{L^2}$	L ³	\mathbf{L}^2	L ³
H3	7.96	7.96	10.72	10.49	9.61	10.24	6.44	6.15
H4	7.99	7.96	9.94	9.70	9.42	9.82	6.60	6.50
H5	7.57	7.56	8.75	8.40	8.67	9.00	6.44	6.44
H7a	x 3.61	3.91	7.08	8.50	2.51	2.97	6.91	9.63
H7e	q 4.76	4.51	1.46	1.37	5.05	1.20	-1.22	2.36
H8a	2.49	2.43	-12.70	-2.27	-5.11	-8.35	16.13	10.95
H8b	2.63	2.87	-5.19	-6.75	1.68	-0.66	3.33	1.29
H9a	x 2.57	3.69	-3.51	1.20	-4.26	-4.98	11.63	15.77
H9e	q 3.86		-2.66		1.30		-0.11	
H10	•	1.55		0.44		-2.58		7.86
H10	/	2.24		-0.52		-1.95		8.04
H11		1.2		-1.40		-1.18		4.70
H11	/	1.82		-1.65		0.41		3.55

^{*a*} Assignment supported by 2D H,H COSY, HMQC, and HMBC experiments at 298 K. ^{*b*} $^{2}J_{9ax,9eq} = 9.4$ Hz; $^{2}J_{9eq,9ax} = 10.6$ Hz; $^{2}J_{7eq,7ax} = 14.6$ Hz; $^{2}J_{7ax,7eq} = 14.6$ Hz; $^{2}J_{8b,8a} = 14.8$ Hz; $^{2}J_{8a,8b} = 14.8$ Hz; $^{3}J_{5,4} = 7.3$ Hz; $^{3}J_{3,4} = 7.3$ Hz; $J_{H8-P} = 5.8$ Hz. $^{c}J_{7eq,7ax} = 14.4$ Hz; $^{2}J_{7ax,7eq} = 14.4$ Hz; $^{2}J_{8b,8a} = 14.9$ Hz; $^{2}J_{8a,8b} = 15.5$ Hz; $^{3}J_{5,4} = 6.4$ Hz; $^{3}J_{3,4} = 6.4$ Hz; $^{3}J_{H8-P} = 6.6$ Hz; $J_{H7-P} = 3.9$ Hz.

the assignment of the spectra, they suggest the presence of two species in solution with a C_1 symmetry. These results point to an increasing rigidity of the complexes in aqueous solutions on decreasing the ionic radius of the Ln^{III} ion, as previously observed for other Ln^{III} complexes.³⁴ In the case of the complex of L² the ³¹P NMR spectrum recorded at 298 K indicates the presence of an equilibrium between two species with an effective C_1 symmetry. It shows a pair of signals of equal intensity at 21.5 and 18.5 ppm and a second pair of less intense signals at 22.4 and 13.7 ppm.

¹H NMR spectra of the paramagnetic Ce^{III}, Nd^{III} and Eu^{III} complexes of L^2 and L^3 were obtained in D_2O solution at pH = 7.4, and were assigned by comparison to the spectra of L^1 complexes and with the aid of line-width analysis and COSY spectra, which gave cross-peaks between the geminal CH₂ protons and between *ortho* pyridyl protons. The spectra of the L^2 complexes show relatively sharp peaks, and they point to an effective C_2 symmetry of the complexes in solution (Table 2, Fig. S1, ESI[†]). The complexes of L³ behave differently in solution: the spectra indicate the formation of two distinct complex species whose concentration changes with time. The spectra acquired immediately after mixing stoichiometric amounts of the ligand and Ln^{III} show a single complex species in solution with C_1 symmetry, which converts slowly to a thermodynamically stable species with an effective C_2 symmetry. This behavior is illustrated in Fig. 3 with the ¹H NMR spectra of the Eu^{III} complex of L³ recorded immediately after the preparation of the complex and after heating the solution at 60 °C for 24 h. Our ab initio calculations discussed below provide two different minimum energy conformations for the L³ complexes: twist-wrap (tw), in which the ligand wraps around the metal ion by twisting the pyridyl units relative to each other, and twist-fold (*tf*), where the slight twisting of the pyridyl units is accompanied by an overall folding of the two pyridine units towards one of the phosphonate groups. Due to this folding, the tw form shows a molecular geometry that is closer to a C_2 symmetry than the tf conformation. Thus, we assign the thermodynamically stable form showing C_2 symmetry to the *tw* isomer, while the kinetic complex is attributed to the *tf* conformation. It should be noted that the two conformations of the Gd^{III} complex are characterized by identical proton relaxivities.



Fig. 3 ¹H NMR spectra of the Eu^{III} complex of L³ recorded in D₂O solution (30 mM, pH = 7.6, 298 K) immediately after the preparation of the complex and after heating the solution at 60 °C for 24 h. HOD and 'BuOH signals are denoted with an asterisk. The assignment of the spectrum recorded at t = 24 h is given in Table 2.

Ab initio calculations: molecular geometries

The $[Ln(L^2)(H_2O)]^{3-}$ systems (Ln = La, Nd, Gd, Ho or Lu)were investigated by means of *ab initio* calculations at the HF/3-21G* level. In the case of Gd^{III} complexes, the long electronic relaxation time of the metal ion prevents any observation of NMR spectra, and for this reason their solution structures and properties have to be deduced from the NMR spectra of other lanthanide complexes. Theoretical calculations provide direct information on gadolinium systems as well as on those dynamic processes that are usually too fast to be observed on the NMR time scale, such as the water exchange process. As there is not a good all-electron basis set for lanthanides, the effective core potential (ECP) of Dolg *et al.* and the related [5s4p3d]-GTO valence basis set was applied in these calculations.¹⁵ This ECP includes 46 + 4fⁿ electrons in the core, leaving the outermost 11 electrons to be treated explicitly, and it has been demonstrated to provide reliable results for the lanthanide aqua-ions,¹⁸ several lanthanide complexes with polyaminocarboxylate ligands^{35,36} and lanthanide dipicolinates.³⁷ Compared to all-electron basis sets, ECPs account to some extent for relativistic effects, which are believed to become important for the elements from the fourth row of the periodic table.

The *in vacuo* geometry optimization of the $[Gd(L^2)(H_2O)]^{3-1}$ system provides a minimum energy conformation very similar to that found for $[Gd(L^1)(H_2O)]^{-,5}$ in which the phosphonate pendant arms are alternatively situated above and below the planes of the pyridyl units. In this structure the distance between the Gd^{III} ion and the oxygen atom of the water molecule is large (Gd– O_w = 2.803 Å), and this water molecule is hydrogen bonded to one of the phosphonate pendants. Thus, we have tried geometry optimizations of the $[Gd(L^2)(H_2O)]^{3-}$ system including the surrounding solvent effects by using the C-PCM model. Unfortunately, because of the optimization convergence difficulty by the C-PCM model^{38,39} these studies were unsuccessful. An alternative to the use of a continuum model of solvation such as C-PCM is to perform cluster calculations that explicitly include a second hydration shell.38,40 These calculations have the advantage that minima and transition states can be optimized and characterized in order to study reactions. Moreover, cluster calculations may also provide useful direct information about the second sphere solvation shell, which has been shown to enhance the relaxivity of Gd^{III} chelates bearing phosphonate groups. The major disadvantage of cluster calculations is that adding extra solvent molecules to the first solvation sphere increases the computational cost. Moreover, the more atoms are included in the system, the larger the number of degrees of freedom and the higher the number of minimum energy structures. For the $[Gd(L)(H_2O)]^{3-}$ complexes $(L = L^2, L^3)$ we have explicitly included 19 H₂O molecules in the second hydration shell. Our calculations provide two different minimum energy geometries where the ligand adopts different conformations (Fig. 4): twist-wrap (tw), in which the ligand wraps around the metal ion by twisting the pyridyl units relative to each other, and twist-fold (*tf*), where the slight twisting of the pyridyl units is accompanied by an overall folding of the two pyridine units towards one of the phosphonate groups. The tf conformation shows a smaller N_{py}-Gd– N_{pv} angle than the *tw* one (N_{pv} = pyridine nitrogen atom). Both minimum energy structures are true energy minima because the vibrational frequency analyses give no imaginary frequencies. Calculated geometrical parameters (bond distances and angles) of the Gd^{III} coordination spheres of these systems are listed in Table 3. The calculated Gd– O_w distances (2.515–2.543 Å) are in excellent agreement with that normally assumed in the analysis of ¹⁷O NMR longitudinal relaxation data (2.50 Å). For the L³ complex, our calculations provide minimum energy conformations with the cyclohexyl unit in chair conformation.

In order to obtain information about the solution structures of this series of Ln^{III} complexes, we also performed geometry optimizations of the molecular clusters $[Ln(L)(H_2O)]^{3-}\cdot 19H_2O$ (Ln = La, Nd, Ho or Lu) at the HF/3-21G* level. Moreover, since the complexes appear to exist in aqueous solution as a mixture of two hydration isomers with q = 0 and q = 1,⁸ we also studied the $[Lu(L)]^{3-}\cdot 20H_2O$ systems. Frequency calculations show that all calculated structures correspond to energy minima.



Fig. 4 Molecular geometries of the twist-wrap (tw) and twist-fold (tf) isomers of $[Gd(L^2)(H_2O)]^{3-}$ complexes obtained from cluster calculations on the $[Gd(L^2)(H_2O)]^{3-}\cdot 19H_2O$ system. Uncoordinated water molecules have been removed for better visualization.

Optimized Cartesian coordinates obtained for the different Ln^{III} systems presented in this work are given in the ESI.[†] Calculated geometrical parameters (bond distances and angles) of the Ln^{III} coordination spheres of these systems are listed in Table 3.

Attempts to model the $[Ln(L)]^{3-}$ complexes (Ln = La, Nd, Gd or Ho) were unsuccessful, since a water molecule systematically entered the metal coordination sphere during the optimization process. However, the smaller ionic radius of Lu^{III} allowed us to model both the $[Lu(L)]^{3-}$ and $[Lu(L)(H_2O)]^{3-}$ complexes in *tw* conformation. A comparison of the bond distances of the Lu^{III} coordination sphere in the $[Lu(L)(H_2O)]^{3-}.19H_2O$ and $[Lu(L)]^{3-}.20H_2O$ molecular clusters reveals that the depletion of the coordinated water molecule results in a considerable shortening of the Lu^{III}–L bond distances (Table 3).

The relative free energies of the twist-wrap (*tw*) and twist-fold (*tf*) conformations of $[Ln(L)(H_2O)]^{3-}$ ($L = L^2, L^3$) complexes were calculated in aqueous solution by using the B3LYP model and the 6-311G** basis set for the ligand atoms. In these calculations second sphere water molecules were excluded, and solvent effects were included by using the polarizable continuum model (C-PCM). It has been demonstrated that this computational approach provides relative energies of the two isomers of $[Ln(DOTA)(H_2O)]^-$ in close agreement to the experimental ones.³⁶ Relative free energies were calculated as $\Delta G^{sol} = G^{sol}_{(ff)} - G^{sol}_{(nv)}$, and therefore a positive relative energy indicates that the *tw* conformation is more stable than the *tf* one. According to our results (Fig. 5), the relative energy of the *tf* conformation decreases along the first half of

		L^2			L^3		
	La	tw(q=1)	tf(q = 1)	tw(q=0)	tw(q=1)	tf(q = 1)	tw (q = 0)
	L - N (1)	2.0(1	2.041		2.071	2 004	
	$La-N_{am}(1)$ La-N(2)	2 962	2.941		3.071	2.904	
	$La - N_{nv}(1)$	2.861	2.757		2.807	2.752	
	$La-N_{py}(2)$	2.741	2.731		2.722	2.730	
	$La=O_{COO}(1)$	2.513	2.500		2.525	2.606	
	$La-O_{COO}(2)$	2.487	2.527		2.491	2.519	
	$La-O_{PO_3}(1)$	2.441	2.436		2.408	2.437	
	$La - O_{PO_3}(2)$	2.408	2.426		2.424	2.437	
	La–O _w	2.657	2.637		2.652	2.634	
	N _{py} -La-N _{py}	159.923	153.431		158.776	154.233	
	O _{PO3} -La-O _{PO3}	146.181	151.109		146.441	152.520	
	NT 1						
	Nd						
	$Nd-N_{am}(1)$	3.081	2.923		3.097	2.897	
	$Nd-N_{am}(2)$	2.965	2.899		3.095	2.977	
	$Nd-N_{nv}(1)$	2.830	2.709		2.771	2.698	
	$Nd-N_{pv}(2)$	2.698	2.696		2.682	2.680	
	$Nd-O_{COO}(1)$	2.464	2.548		2.474	2.559	
	$Nd-O_{COO}(2)$	2.427	2.462		2.427	2.460	
	$Nd-O_{PO_3}(1)$	2.381	2.382		2.347	2.379	
	$Nd-O_{PO_3}(2)$	2.350	2.371		2.363	2.371	
	Nd–O _w	2.604	2.590		2.601	2.576	
		150 210	152 495		150 171	150 505	
	N _{py} -Nd-N _{py}	159.219	153.485		158.1/1	152.595	
	OPO3-IND-OPO3	140.332	151.195		145.996	151.577	
	Cd						
	Gu						
	Gd-N _{am} (1)	3.134	2.920		3.158	2.881	
	$Gd-N_{am}(2)$	2.991	2.893		3.155	2.944	
	$Gd-N_{py}(1)$	2.805	2.665		2.738	2.660	
	$Gd-N_{py}(2)$	2.656	2.642		2.647	2.644	
	$Gd-O_{COO}(1)$	2.406	2.502		2.412	2.521	
	$Gd-O_{COO}(2)$	2.360	2.392		2.356	2.386	
	$Gd-O_{PO_3}(1)$	2.314	2.321		2.280	2.319	
	$Gd-O_{PO_3}(2)$	2.287	2.309		2.295	2.318	
	Gd–O _w	2.543	2.518		2.538	2.515	
	N CAN	157 715	152 220		156 296	152.057	
	n_{py} -Gu- n_{py}	146 352	150.847		144 709	152.937	
	003 84 0003	110.552	150.017		111.709	191.797	
	Но						
	$Ho-N_{am}(1)$	3.196	2.928		3.232	2.902	
	$Ho-N_{am}(2)$	3.027	2.909		3.217	2.975	
	$Ho-N_{py}(1)$	2.793	2.637		2.721	2.631	
	$Ho-N_{py}(2)$	2.632	2.618		2.629	2.621	
	$H_0 - O_{COO}(1)$	2.363	2.468		2.367	2.485	
	$H_0 - O_{COO}(2)$	2.312	2.346		2.306	2.339	
	$H_0 - O_{PO_3}(1)$	2.241	2.207		2.232	2.272	
	$H_0 - O_{PO_3}(2)$	2.208	2.278		2.249	2.272	
	HO O _W	2.500	2.407		2.477	2.402	
	N _{nv} -Ho-N _{nv}	156.140	152.711		154.378	152.324	
	OPO3-HO-OPO3	145.709	149.804		143.138	150.160	
	Lu						
	Lu-N _{am} (1)	3.283	2.957	3.121	3.327	2.973	3.136
	$Lu-N_{am}(2)$	3.098	2.938	2.895	3.307	3.038	2.960
	$Lu - N_{py}(1)$	2.785	2.613	2.710	2.704	2.602	2.665
	$Lu - N_{pv}(2)$	2.610	2.593	2.570	2.612	2.593	2.588
	$Lu - O_{COO}(1)$	2.308	2.425	2.274	2.310	2.426	2.272
	$Lu-O_{COO}(2)$	2.253	2.290	2.226	2.245	2.282	2.220
	$Lu-O_{PO_3}(1)$	2.212	2.225	2.190	2.193	2.215	2.181
	$Lu-O_{PO_3}(2)$	2.188	2.218	2.143	2.177	2.214	2.138
	Lu–O _w	2.454	2.419		2.444	2.414	
	N. I N	152 522	151 757	160.942	151 402	151 162	160 251
	$N_{py}-Lu-N_{py}$	133.333	131./5/ 148 752	163 346	131.463	131.103	162 891
	0P03 Du-0P03	177,112	140.752	105.540	170./12	170.131	102.071
0							

Table 3	Values of the main geometrical parameters o	f calculated structures for [Ln(L)(H2O)]3	$-\cdot 19 \mathrm{H}_2\mathrm{O} (\mathrm{L} = \mathrm{L}^2, \mathrm{L}^3)$	complexes at the HF/3-21G* level ^a
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" Distances (Å), angles (°). N_{am} = amine nitrogen atoms; N_{py} = pyridyl nitrogen atoms; O_{COO} = carboxylate oxygen atoms; O_{PO_3} = phosphonate oxygen atoms; O_w = water oxygen atom.





Fig. 5 Top: In aqueous solution (C–PCM) relative free energies of the *tf* isomer $(\Delta G^{sol} = G^{sol}_{(ff)} - G^{sol}_{(nv)})$ for $[Ln(L)(H_2O)]^{3-}$ ($L = L^2, L^3$) complexes. Bottom: Calculated values of the bond distance between the lanthanide ion and the amine nitrogen atoms (Ln–N_{am}) in the *tw* and *tf* isomers of $[Ln(L^2)(H_2O)]^{3-}$ complexes.

the lanthanide series, reaches a minimum with Gd, and then increases for the heaviest lanthanides. The *tw* form is the most stable along the whole lanthanide series for the L^3 complexes, while for those of L^2 only the Gd^{III} complex is more stable in the *tf* conformation by *ca*. 0.5 kcal mol⁻¹. The L^3 complexes present higher relative energies of the *tw* conformation than the L^2 complexes. The reason is probably the higher flexibility of L^2 , which allows the folding of the pyridine units relative to each other without increasing importantly the strain of the ligand in the complexes. It is noteworthy that the *tf* conformation has been observed by ¹H NMR for EuL³. As discussed above, this conformation slowly converts to the thermodynamically stable *tw* form.

For the $[Ln(L^3)(H_2O)]^{3-}$ complexes a third minimum energy geometry has been obtained, in which the cyclohexyl unit adopts twist-boat conformation. The calculated geometries are given in the ESI.[†] Calculated relative free energies indicate that the conformational change from chair to twist-boat (*tb*) provokes an important destabilization of the system: $\Delta G^{sol} = G^{sol}_{(tb)} - G^{sol}_{(tw)} =$ 10.93 (Nd), 4.85 (Gd) and 6.87 kcal mol⁻¹ (Lu). According to these values, the twist-boat form is less stable than the *tw* and *tf* conformations described above.

The variation of the relative energies of the two isomers of L^2 and L^3 complexes along the lanthanide series appears to be related, at least in part, to the bond distances of the metal coordination environment. Most of the calculated bond distances between the lanthanide and the coordinated donor atoms (Table 3)

decrease along the lanthanide series, as usually observed for Ln^{III} complexes.³⁴ The destabilization of the *tw* conformation along the first half of the lanthanide series can be attributed to the weakening of the interaction between the Ln^{III} ion and the amine nitrogen atoms, since the $Ln-N_{am}$ distances clearly increase along the lanthanide series (Fig. 5). A similar enlargement of Ln-N bond distances has been previously observed for lanthanide complexes with crown ethers, which has been attributed to a better size match between the ligand cavity and the lightest Ln^{III} ions.⁴¹ On the contrary, the $Ln-N_{am}$ distances decrease along the first half of the lanthanide series for the *tf* form, reaching a minimum with Gd^{III}, and then increasing for the heaviest lanthanide ions. According to the variation of the $Ln-N_{am}$ bond distances for the *tw* and *tf* conformations one expects a maximum stabilization of the *tf* form for the middle of the lanthanide series.

Second-sphere hydration shell

Recent studies have demonstrated that due to their charge and important structure ordering effect, phosphonate groups have a tendency to induce a second hydration sphere around the metal complexes.^{9,10} By remaining in the proximity of the paramagnetic Gd^{III} center for a non-negligible time, these second sphere water molecules may represent a significant contribution to the overall proton relaxivity of MRI contrast agents. The analysis of the NMRD profiles of phosphonic acid derivatives of diethylenetriamine suggested the presence of two second sphere water molecules contributing to the overall proton relaxivity.⁹

The ab initio calculations presented here provide useful direct information about the second sphere solvation shell. The calculations on molecular clusters [Gd(L)(H₂O)]³⁻·19H₂O indicate that most of the second sphere water molecules are hydrogen bonded to the highly charged phosphonate groups. The distances between the Gd^{III} ion and the oxygen and hydrogen atoms of second sphere water molecules hydrogen bonded to the phosphonate groups are given in Table S1 (ESI[†]). Our calculations indicate that at least six or seven water molecules are hydrogen-bonded to each phosphonate group. For the complexes in tw conformation only three second sphere water molecules are in close proximity of the Gd^{III} ion with Gd–O distances of 4.1–4.2 Å, whereas the other second-sphere water molecules are relatively distant (Gd-O distances above 5.4 Å). Among the three water molecules close to the Gd^{III} ion two are hydrogen bonded to the phosphonate group situated close to the inner sphere water molecule (Fig. 4), while the third one is interacting with the second (more sterically crowded) phosphonate group. A similar situation occurs for the $[Lu(L)]^{3-}$ systems, which show two second sphere water molecules in the close proximity of the Lu^{III} ion with Lu-O distances of 3.9-4.0 Å, and a third water molecule showing an intermediate Lu-O distance (ca. 4.6 Å). The remaining second sphere water molecules are relatively far from the lanthanide ion. Since both ¹H and ¹⁷O longitudinal relaxation rates depend on $1/r^6$, where r represents the distance between the observed nucleus and the Gd^{III} ion,⁴² only water molecules relatively close to the paramagnetic centre are expected to provide a substantial second sphere contribution. Thus, it appears reasonable to assume three second sphere water molecules in the analysis of the relaxivity and ¹⁷O NMRD data of the Gd^{III} complexes with L² and L^{3.8} In contrast to the tw conformation in the tf form all three closely situated second sphere water molecules are hydrogen-bonded to one of the phosphonate groups, for steric reasons.

¹³C NMR shielding constants

It has been demonstrated that quantum-mechanical GIAO calculations of ¹³C NMR chemical shifts can be used as a tool for structure validation of coordination compounds,43 including lanthanide complexes.^{36,44} Thus, the ¹³C NMR shielding constants of the tw and tf forms of the $[La(L)(H_2O)]^{3-}$ (L = L², L³) complexes were calculated on the in vacuo optimized structures of $[La(L)(H_2O)]^{3-} \cdot 19H_2O$ by using the GIAO method. Due to the importance of including electronic correlation effects the calculations of the NMR shielding constants were performed at the B3LYP/6-311G** level, by using the 46 core electron ECP by Stevens et al.²⁰ In these calculations solvent effects (water) were included by using the C-PCM model. The calculated ¹³C NMR shifts are compared with the experimental values in Table 4. We notice a systematic deviation to lower fields of the calculated values with respect to the experimental ones. Thus, in order to asses the agreement between the experimental and calculated ¹³C NMR spectra, we have plotted the experimental ¹³C chemical shift values vs. the corresponding GIAO calculated ¹³C chemical shifts for the tw and tf isomers. These plots give straight lines whose slopes and intercepts are given in Table 4. The correlation plots obtained for the complexes of L^3 are shown in Fig. 6. In general, the linear correlation of these plots is better for the tw than for the tf form in both L^2 and L^3 complexes, as indicated by the R^2 values obtained from the linear least squares fit. This implies that the tf form is a less probable structure of the complexes in solution. To confirm this we have calculated scaled theoretical chemical shift values $(\delta_{i,\text{esc}})$ obtained as:⁴⁵

$$\delta_{i,\text{esc}} = (\delta_{i,\text{calc}} - A)/B \tag{4}$$

where $\delta_{i,\text{calc}}$ are the GIAO calculated chemical shifts, and A and B are the intercept and slope obtained from the linear correlation plots of the same compound. Fig. 6 shows a plot of differences between experimental and scaled theoretical ¹³C NMR shift values

 $(\Delta\delta)$ for the *tw* and *tf* complexes of L³ obtained at the B3LYP/6-311G** level, where it is possible to appreciate larger deviations from the experimental values for most carbon nuclei of the *tf* form than for the same nuclei in the *tw* one. An analogous analysis of the scaled theoretical shifts calculated for the complex of L² leads to similar conclusions. These results therefore confirm that the La^{III} complexes of L² and L³ are present in solution in *tw* conformation, in agreement with the relative free energies of the two isomers discussed above.

Nd^{III}-Induced relaxation rate enhancement effects

Information on the solution structure of the complexes was obtained from Nd^{III}-induced relaxation rate enhancements of the ¹H nuclei of ligands L² and L³. Among the lighter Ln^{III} ions (Ln = Ce \rightarrow Eu), Nd^{III} has the longest electron relaxation times,^{46,47} and therefore this cation is very suitable for obtaining structural information of lanthanide complexes in solution.⁴⁸ The Nd^{III}-induced ¹H NMR relaxation enhancements for both ligands were measured at 7.05 T and 25 °C (Table 5). In order to correct for diamagnetic contributions, the relaxation rates for the corresponding La^{III} complex were subtracted from the measured values of the Nd^{III} complex (see Table 5).

Since the outer-sphere contribution $(1/T_{1os})$ becomes significant only for remote nuclei, this contribution was neglected. The electron relaxation for Nd^{III} is very fast $(T_{1e} \approx 10^{-13} \text{ s})$ and, consequently, the contact contribution to the paramagnetic relaxation is negligible. Two contributions are of importance: the "classical" dipolar relaxation and the Curie relaxation. Eqn (5) can be derived from a simplified Solomon–Bloembergen equation⁴⁹ and from the equation for the Curie relaxation (assuming extreme narrowing):^{50,51}

$$\frac{1}{T_{1}} = \left[\frac{4}{3} \left(\frac{\mu_{0}}{4\pi} \right)^{2} \mu^{2} \gamma_{1}^{2} \beta^{2} t_{1e} + \frac{6}{5} \left(\frac{\mu_{0}}{4\pi} \right)^{2} \frac{\gamma_{2}^{1} H_{0}^{2} \mu^{4} \beta^{4}}{(3kT)^{2}} \tau_{R} \right] \frac{1}{r^{6}}$$
(5)

Table 4 Experimental ¹³C shifts (ppm) for the La^{III} complexes of L² and L³ in 30 mM D₂O solutions at pH 7.6 and calculated (GIAO method) ¹³C NMR chemical shift values for the *tw* and *tf* conformations (see Scheme 1 for labelling)

	L^2			L^3			
	$\overline{\delta_{i, ext{exptl}}}$	$\delta_{i, ext{calc}(tw)}$	$\delta_{i, ext{calc}(tf)}$	$\overline{\delta_{i, ext{exptl}}}$	$\delta_{i,\mathrm{calc}(tw)}$	$\delta_{i,\mathrm{calc}(tf)}$	
1	175.1	178.2	179.1	175.0	178.2	179.2	
2	153.1	156.9	157.8	152.7	157.1	157.9	
3	124.9	127.6	127.4	124.8	127.7	127.3	
4	141.4	143.8	144.2	141.5	143.7	144.0	
5	127.6	130.2	129.8	128.2	131.0	130.3	
6	159.4	167.6	168.4	159.6	168.5	169.1	
7	62.5	67.5	69.3	58.0	62.7	64.3	
8	57.2	59.4	63.0	52.6	55.0	57.1	
9	55.4	58.7	59.8	63.2	66.2	64.2	
10				24.8	28.8	27.1	
11				26.3	31.7	25.0	
$R^{2 a}$		0.9992	0.998		0.9994	0.9990	
A^a		2.6 ± 1.9	5.4 ± 2.2		3.7 ± 1.3	1.1 ± 1.7	
B^{a}		1.01 ± 0.01	0.99 ± 0.02		1.00 ± 0.01	1.02 ± 0.02	

^a Intercept, slope and correlation coefficient obtained by linear fitting of calculated vs. experimental ¹³C NMR chemical shift plots (see text).



Fig. 6 Top: data points and fitting straight lines of calculated *vs.* experimental ¹³C NMR chemical shifts at the B3LYP/6-311G** level for the *tw* and *tf* structures of $[La(L^3)(H_2O)]^{3-}$ complexes in aqueous solution. The plot relative to *tf* has been displaced by 30 ppm along the ordinate axis for better visualization. Bottom: Differences between experimental and scaled theoretical ¹³C NMR chemical shifts (B3LYP/6-311G** level) for the *tw* and *tf* isomers of $[La(L^3)(H_2O)]^{3-}$.

where the first term between the square brackets represents the "classical" dipolar contribution, and the second term describes the Curie relaxation. Here, $\mu_0/4\pi$ is the magnetic permeability in a vacuum, μ is the effective magnetic moment of the lanthanide ion, γ_I is the gyromagnetic ratio of the nucleus under study, β is the Bohr magneton, T_{1e} is the electron spin relaxation time, r is the distance between the ¹H nucleus in question and the lanthanide ion, H_0 is the magnetic field strength, k is the Boltzmann constant, T is the temperature, and τ_R is the rotational tumbling time of the complex. The contribution of the Curie spin mechanism to the total relaxation becomes significant for larger molecules (τ_R increases), particularly at higher fields.

At constant temperature and B_0 , application of eqn (5) allows the determination of relative *r* values in the complexes without the need to estimate T_{1e} and τ_R , which would be needed to calculate absolute distances. Plots of $1/T_1$ vs. $1/r^6$, where *r* stands for the Nd ··· H distances obtained from the *ab initio* optimized structures give straight lines ($R^2 > 0.996$) passing through the origin with

Table 5 Relaxation rates (s^-1) determined for 40 mM solutions of Ln^{III} complexes in D₂O (300 MHz, 25 °C, pH = 7.6) and Nd ··· H distances (Å)calculated from H NMR relaxation data

	$1/T_{1(Nd)}$		$1/T_{1(La)}$		$Nd \cdots H$ (Calc.) ^{<i>b</i>}		$Nd \cdots H$ (Exptl.) ^c	
	$\overline{L^2}$	L ³	L ²	L ³	$\overline{L^2}$	L ³	$\overline{L^2}$	L ³
H3	9.221	8.718	0.683	0.524	5.600	5.572	5.89	5.63
H4	4.384	4.337	0.756	0.524	6.562	6.529	6.79	6.26
H5	8.454	8.326	0.914	1.294	5.799	5.762	6.02	5.75
H7ax	95.111	75.896	3.650	6.976	3.997	3.989	3.97	4.02
H7eq	27.054	а	4.0	5.786	4.764	4.766	4.99	а
H8a	102.135	а	3.630	4.086	3.946	3.868	3.92	а
H8b	29.619	28.490	3.057	5.814	4.727	4.744	4.88	4.81
H9ax	86.08	66.05	3.481	3.519	4.015	4.137	4.04	4.08
H9eq	a		4.552		4.823		а	
H10		14.95		7.196		5.634		5.67
H10′		13.038		6.954		5.767		5.87
H11		8.423		а		6.641		а
H11′		6.798		5.519		7.471		7.06

" Not obtained. " Nd^{III} · · · H distances obtained from *ab initio* calculations (*tw* conformations). " Nd^{III} · · · H distances obtained from experimental ¹H NMR relaxation data.

slopes $k = (3.57 \pm 0.09) \times 10^{-55} \text{ m}^6 \text{ s}^{-1} (\mathbf{L}^2)$ and $k = (2.88 \pm 0.07) \times 10^{-55} \text{ m}^6 \text{ s}^{-1} (\mathbf{L}^3)$. The slope obtained from this plot represents the term between the brackets in eqn (5). Using the τ_R obtained from ²H NMR relaxation data at a concentration of 40 mM ($\tau_R = 152 \text{ ps}$)⁸ we obtain $T_{1e} = 2.69 \times 10^{-13} \text{ s}$ for the L² complex, a value substantially longer than the one determined by Alsaadi *et al.* for the aqua ion ($T_{1e} = 1.15 \times 10^{-13} \text{ s}$).⁵² The experimental values of *k* were used to obtain experimental Nd^{III} ··· H distances in solution from relaxation data by using eqn (5). In general, the experimental distances are in satisfactory agreement with those obtained from the theoretical calculations (Table 5), thereby confirming that the computational approach provides a reliable description of the solution structures.

Conclusions

The octadentate ligands L^2 and L^3 form thermodynamically stable Gd^{III} complexes in aqueous solution, and thus can be considered as new basic structural frameworks for the design of novel MRI contrast agents. Our results show an improved stability of the Gd^{III} complexes in aqueous solution when the acetate arms of L^1 are replaced by phosphonate pendants. NMR studies in solution indicate octadentate binding of L^2 and L^3 to the Ln^{III} ions. Quantum mechanical calculations performed at the HF level provide two minimum energy geometries of the complexes where the ligand adopts different conformations: twist-wrap (tw), in which the ligand wraps around the metal ion by twisting the pyridyl units relative to each other, and twist-fold (tf), where the slight twisting of the pyridyl units is accompanied by an overall folding of the two pyridine units towards one of the phosphonate groups. The tw form is the most stable one along the whole lanthanide series for the complexes of L^3 , while for those of L^2 only the Gd^{III} complex is more stable in the *tf* conformation by *ca*. 0.5 kcal mol⁻¹. Our results indicate that the relative energy of the tf conformation decreases along the first half of the lanthanide series, reaches a minimum with Gd, then increases for the heaviest lanthanides. ¹H NMR studies of EuL³ show the initial formation of the *tf* complex in aqueous solution, which slowly converts to the thermodynamically stable *tw* form. The calculated structures for the Nd^{III} complexes are in reasonably good agreement with the experimental solution structures, as demonstrated by Nd^{III}induced relaxation rate enhancement effects in the ¹H NMR spectra. The computational approach presented in this work, in combination with experimental information obtained by NMR spectroscopy, represents a powerful tool to obtain structural information of lanthanide complexes in solution.

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