

Article

Hg-Based Infrared Nonlinear Optical Material $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ Exhibits Good Phase-Matchability and Exceptional Second Harmonic Generation Response

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4 **Hg-Based Infrared Nonlinear Optical Material $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ Exhibits**
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6 **Good Phase-Matchability and Exceptional Second Harmonic**
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8 **Generation Response**
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ABSTRACT

High-performance infrared (IR) nonlinear optical (NLO) materials with large NLO response and suitable birefringence are urgently needed for various applications. A Hg-based IR NLO material $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ with such desirable properties has been newly discovered. In the structure, obviously distorted HgSe_4 and GaSe_4 tetrahedra are connected to each other by vertex-sharing to form a three-dimensional framework with the counter-ion K^+ residing in the cavities. Remarkably, all the NLO-active building units in the title compound are arranged in a completely parallel manner. Such a topological structure and the large susceptibility of the Hg–Se bonds enable the material to achieve good phase-matchability with a tremendous powder SHG response at $2.09 \mu\text{m}$ that is about 20 times that of the benchmark material AgGaS_2 (one of the largest responses among all the phase-matchable IR NLO chalcogenides reported to date). The optical band gap of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ was determined as 1.61 eV. Moreover, based on the electronic band structure, the real-space atom-cutting analysis, the SHG-weighted electronic densities, and the local dipole moments calculations, the origin of the superior linear and nonlinear optical properties of the title compound is ascribed to the $(\text{Hg}/\text{Ga})\text{Se}_4$ group. The calculated values for the maximum coefficient d_{33} and birefringence (Δn) at $2.09 \mu\text{m}$ are -65.257 pm/V and 0.072, respectively. Such values agrees well with experimental observations. Our study demonstrates that Hg-based metal chalcogenides are a class of IR NLO material with competitive features (good phase-matchability, very large SHG efficiency, wide transparency) desirable for practical applications.

INTRODUCTION

The growing demands for new IR coherent light sources have stimulated large-scale tentative synthetic activities in searching new IR NLO crystals, which can convert the frequencies of existing lasers to a favorable wavelength range with reasonable efficiency by second harmonic generation (SHG), sum frequency generation (SFG), difference frequency generation (DFG), optical parametric amplification (OPA) and optical parametric oscillation (OPO) processes, etc.¹⁻⁶ The chalcopyrite-type ternary compounds AgGaQ_2 ($Q = \text{S}, \text{Se}$)^{7,8} and ZnGeP_2 ⁹ are known as the benchmark IR NLO materials for decades. Unfortunately, all of them are subject to property shortcomings that severely restrict their further applications. Therefore, searching for alternatives with good overall performances are of significant importance.

As a rich family of compounds, metal chalcogenides, offer a fruitful source of potential IR NLO materials owing to their wide compositional and structural flexibility and inherently good optical transparency in the mid- and far-IR regions. By applying various synthetic strategies, many interesting IR NLO crystals have been successfully synthesized in the past several years. Some representing examples include LiMQ_2 ($M = \text{Ga}, \text{In}; Q = \text{S}, \text{Se}$),¹⁰⁻¹² AAsSe_2 ($A = \text{Li}, \text{Na}$),¹³ BaGa_4Q_7 ($Q = \text{S}, \text{Se}$),^{14,15} SnGa_4Q_7 ($Q = \text{S}, \text{Se}$),¹⁶ Na_2BaMQ_4 ($M = \text{Ge}, \text{Sn}; Q = \text{S}, \text{Se}$),¹⁷ $\text{Ba}_{23}\text{Ga}_8\text{Sb}_2\text{S}_{38}$,¹⁸ and $\text{Ba}_2\text{Ga}_8\text{MS}_{16}$ ($M = \text{Si}, \text{Ge}$),¹⁹ etc.

Very recently, our interests in the search for new IR NLO crystals have mainly focused on the d^{10} cations-containing metal chalcogenides, especially the Hg-based

ones, owing to the following thoughts: (1) Hg^{2+} is about the same size as Ca^{2+} , but it is a much more strongly polarizing ion as a result of the decreased shielding power of the $4f$ electrons and relativistic effects. Thus, the ion has a strong tendency to form covalent bonds rather than ionic bonds, especially with S-, Se-ligands and the Hg-chalcogens bonds should exhibit wide transparent window in the IR region. (2) The outer electron configuration of mercury is $6s^2$, the closed-shell configuration can effectively avoid the $d-d$ optical transition problem. Moreover, the outer orbital energies are very close and little energy is required to promote an electron from the $6s$ orbital to one of the $6p$ orbitals. In this case, the orbitals can combine to form sp^x hybrid orbitals to form linear, trigonal-planar, and tetrahedral coordination for $x = 1, 2,$ and 3 respectively. The trigonal-planar units and the tetrahedral units are typical NLO-active structural units. In addition, the highly polarizable Hg-chalcogen bond would further increase the SHG response and the birefringence of IR NLO materials. Hence, Hg-based chalcogenides may provide an attractive playground for IR-NLO materials (it should be mentioned that element Hg and most of the Hg-based compounds are extremely toxic and unfriendly to the environment. Therefore, all the manipulations should be performed with great care). According to our investigation, only a few Hg-based metal chalcogenides have been reported as promising IR NLO materials including HgGa_2S_4 ,²⁰ BaHgQ_2 ($Q = \text{S}, \text{Se}$),^{21,22} Li_2HgMS_4 ($M = \text{Si}, \text{Ge}, \text{Sn}$),²³ $\text{Li}_4\text{HgGe}_2\text{S}_7$,²⁴ and $\text{A}_2\text{Hg}_3\text{M}_2\text{S}_8$ ($A = \text{Na}, \text{K}; M = \text{Si}, \text{Ge}, \text{Sn}$).^{25,26} In particular, the $[\text{HgSe}_3]^{4-}$ groups in BaHgSe_2 were identified as the first π -conjugated anionic groups with large NLO susceptibilities and stable chemical properties in IR NLO

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3 materials.²² Among these Hg-based IR NLO materials, the largest SHG response was
4 reported to be 6.5 times that of AgGaS₂.
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9 As part of our recent explorations for promising Hg-based IR NLO materials, we
10 report in this paper a new Hg-based compound KHg₄Ga₅Se₁₂, which features a
11 three-dimensional framework composed of vertex-sharing HgSe₄ and GaSe₄
12 tetrahedra with the counter-ion K⁺ residing in the cavities. Interestingly, all of the
13 NLO-active chromophores (HgSe₄ and GaSe₄ tetrahedra) in KHg₄Ga₅Se₁₂ are arranged
14 in a completely parallel manner. Owing to such a cooperative packing mode and the
15 highly susceptible Hg–Se bonds, the material displays good phase-matchability with a
16 tremendous powder SHG responses at 2.09 μm that is about 20 times that of the
17 benchmark material AgGaS₂. Such intense NLO response is one of the largest among
18 all phase-matchable IR NLO materials reported so far. This work demonstrates that
19 Hg-based metal chalcogenides may be promising alternatives for IR nonlinear optics,
20 and may provide some insights in the further search for new IR NLO materials.
21 Herein, we represent the synthesis, crystal structure, linear and nonlinear optical
22 properties and the detailed theoretical calculations of this new IR NLO material.
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45 **EXPERIMENTAL SECTION**

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48 **Synthesis.** K (3N), Ga (5N), Se (5N) and HgSe (4N) were directly purchased
49 from Sinopharm Chemical Reagent Co., Ltd. The binary starting materials K₂Se and
50 Ga₂Se₃ were synthesized by the stoichiometric reaction of the elements in sealed silica
51 tubes. All manipulations were performed in an Ar-filled glovebox with H₂O and O₂
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4 contents less than 0.1 ppm. Polycrystalline sample of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ was obtained by
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6 traditional solid state reaction²⁷⁻²⁹ in a stoichiometric mixture of K_2Se , HgSe and
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8 Ga_2Se_3 . The raw materials were loaded into fused-silica tubes and then, the ampoules
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10 were flame-sealed under a high vacuum of 10^{-3} Pa. The tubes were then placed in a
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12 computer-controlled furnace and heated to 873 K within 15 h, left for 48 h and, finally,
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14 the furnace was turned off.
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19 **Crystal Growth.** Single crystals of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ were prepared through
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21 spontaneous crystallization using excess K_2Se as flux. The reaction charge of K_2Se ,
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23 HgSe and Ga_2Se_3 in a molar ratio of 3: 8: 5 was mixed and loaded into a fused-silica
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25 tube. Then, the tube was flame-sealed and gradually heated to 1123 K in a
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27 computer-controlled horizontal furnace, kept for 72 h, and then, slowly cooled at a
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29 rate of 3 K/h, and finally cooled to room temperature by switching off the furnace.
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31 The product consists of hundreds of dark-red block-shaped crystals. These small
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33 crystals were stable in air for more than 5 months by now. The EDX-equipped field
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35 emission scanning electron microscope (Hitachi S-4800) analysis on several small
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37 crystals confirmed the presence of K, Hg, Ga and Se in the molar ratio of
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39 approximately 1 : 4 : 5 : 12. Then a crystal with good morphology was manually
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41 selected for structure characterization.
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49 **Structure Determination.** Single-crystal X-ray diffraction experiment was
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51 performed on a Xcalibur Ecos diffractometer equipped with a
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53 graphite-monochromated Mo-K_α ($\lambda = 0.71073 \text{ \AA}$) radiation at 293 K. The collection
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55 of the intensity data and cell refinement was carried out with CrysAlisPro software
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4 (Agilent Technologies, Version 1.171.35.11).³⁰ Multi-scan absorption corrections were
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6 performed numerically with the use of the program XPREP.³¹
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9 The structure was solved with the direct methods using SHELXTLS program
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11 and refined with the least-squares program SHELXL of the SHELXTL.PC program
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13 suite.³¹ The main structural data and refinement parameters for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ are
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15 given in Table 1. The atom positional coordinates and equivalent isotropic
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17 displacement parameters for the title compound are given in Table 2. The selected
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19 bond distances can be observed in Table 3.
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24 **Powder X-ray Diffraction (PXRD).** The PXRD pattern of the ground powder
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26 was performed at room temperature on a Bruker D8 Focus diffractometer with Cu K_α
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28 ($\lambda = 1.5418 \text{ \AA}$) radiation. The scanning step width of 0.05° and a fixed counting time
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30 0.2 s/step were applied to record the patterns in the 2θ range of $10 - 80^\circ$. The
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32 measured XRD powder pattern was found to perfectly match with the simulated
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34 pattern generated using the CIF of the refined structure. (see Figure 1).
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39 **Raman Spectroscopy.** The unpolarized Raman scattering spectrum was
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41 recorded from ground powder sample at room temperature with an inVia-Reflex
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43 instrument with a line of 532 nm of solid state laser. The spectral resolution was 2
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45 cm^{-1} , and the scanning range was $100 - 500 \text{ cm}^{-1}$.
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50 **Diffuse Reflectance Spectroscopy.** Appropriate amount of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$
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52 polycrystalline sample was thoroughly ground. A Cary 5000 UV-vis-NIR
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54 spectrophotometer with a diffuse reflectance accessory (the spectral resolution in the
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56 UV-vis and NIR range is 0.05 nm and 0.2 nm , respectively) was used to measure the
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4 spectrum of the title compound and BaSO₄ (as a reference) in the range from 400 nm
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6 (3.1 eV) to 2000 nm (0.62 eV).
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9 **Thermal Analysis.** By applying the LabsysTM TG-DTA16 (SETARAM) thermal
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11 analyzer equipped with the nitrogen flow at a rate of about 30 ml/min, the thermal
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13 stability of the title material was investigated in detail. Appropriate amounts of
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15 polycrystalline powder of KHg₄Ga₅Se₁₂ were thoroughly ground, then were placed in
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17 a silica tube (5 mm o.d. × 3 mm i.d.) and subsequently sealed under a high vacuum.
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19 The tube was heated from room temperature to 1273 K and then cooled to room
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21 temperature with the heating/cooling rate both at 15 K min⁻¹.
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26 **SHG Measurement.** The optical SHG response of KHg₄Ga₅Se₁₂ was measured
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28 on polycrystalline powder samples by means of the Kurtz–Perry method.³² The
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30 fundamental light was a 2090 nm light generated with a Q-switched Ho: Tm: Cr: YAG
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32 laser. The sample was thoroughly ground and sieved into a series of distinct particle
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34 size ranges of 20 – 41, 41 – 74, 74 – 105, 105 – 150 and 150 – 200 μm, respectively,
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36 which were then pressed into a disk with diameter of 8 mm that was put between glass
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38 microscope slides and secured with tape in a 1 mm thick aluminum holder.
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Microcrystalline AgGaS₂ was ground and sieved into the same particle size range of
150 – 200 μm as a reference.

50 COMPUTATIONAL SECTION

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First-principles Calculation. The first-principles calculations for KHg₄Ga₅Se₁₂
were performed by CASTEP,³³ a plane-wave pseudopotential total energy package

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4 based on density functional theory (DFT).³⁴ The functional developed by
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6 Perdew-Burke-Ernzerhof (PBE) functional within the generalized gradient
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8 approximation (GGA)^{35,36} form were adopted to describe the exchange-correlation
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10 energy. The optimized norm-conserving pseudopotentials³⁷ in the
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12 Kleinman-Bylander³⁸ form for all the elements are used to model the effective
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14 interaction between atom cores and valence electrons. And K $3s^23p^64s^1$, Ga
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16 $3d^{10}4s^24p^1$, Hg $5s^25p^65d^{10}6s^2$ and Se $4s^24p^4$ electrons were treated as valence
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18 electrons, allowing the adoption of a relatively small basis set without compromising
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20 the computational accuracy. The high kinetic energy cutoff 1000 eV and dense $2 \times 2 \times 4$
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22 Monkhorst-Pack³⁹ k -point meshes in the Brillouin zones were chosen for
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24 KHg₄Ga₅Se₁₂. For the calculations of the electronic structure, SHG coefficients and
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26 refractive indices, we used the structural data directly from the experimental
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28 determination, which means that we treated the disorder between Hg and Ga cations
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30 by the virtual crystal approximation (VCA) method rather than the super-cell method
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32 to conduct the first-principles simulations with a moderate computational cost. Our
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34 tests showed that the above computational setups are sufficiently accurate for present
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36 purposes.
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46 Based on the scissor-corrected⁴⁰ electronic band structure, the imaginary part of
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48 the dielectric function was calculated according to the electron transition from the
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50 valence bands (VBs) to conduction bands (CBs). The real part of the dielectric
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52 function is obtained by the Kramers-Kronig⁴¹ transform, from which the refractive
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54 indices are also determined. The second order susceptibility $\chi^{(2)}$ and the SHG
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coefficients d_{ij} are calculated by the formula developed by our group.^{42,43} The second-order susceptibility χ_{ijk} is represented as:

$$\chi_{ijk} = \chi_{ijk}(\text{VE}) + \chi_{ijk}(\text{VH}) + \chi_{ijk}(\text{twobands})$$

where χ_{ijk} (VE) and χ_{ijk} (VH) denote the contributions from virtual-electron processes and virtual-hole processes, respectively, and χ_{ijk} (two bands) gives the contribution from two band processes to $\chi^{(2)}$. The formulas for calculating χ_{ijk} (VE), χ_{ijk} (VH) and χ_{ijk} (two bands) are as following:

$$\begin{aligned} \chi_{ijk}(\text{VE}) &= \frac{e^3}{2\hbar^2 m^3} \sum_{vc'} \int \frac{d^3 \bar{k}}{4\pi^3} P(ijk) \text{Im}[p_{vc}^i p_{cc'}^j p_{c'v}^k] \left(\frac{1}{\omega_{cv}^3 \omega_{vc'}^2} + \frac{2}{\omega_{vc}^4 \omega_{c'v}} \right) \\ \chi_{ijk}(\text{VH}) &= \frac{e^3}{2\hbar^2 m^3} \sum_{v'c} \int \frac{d^3 \bar{k}}{4\pi^3} P(ijk) \text{Im}[p_{v'v}^i p_{v'c}^j p_{cv}^k] \left(\frac{1}{\omega_{cv}^3 \omega_{v'c}^2} + \frac{2}{\omega_{vc}^4 \omega_{cv'}} \right) \\ \chi_{ijk}(\text{twobands}) &= \frac{e^3}{\hbar^2 m^3} \sum_{vc} \int \frac{d^3 \bar{k}}{4\pi^3} P(ijk) \frac{\text{Im}[p_{vc}^i p_{cv}^j (p_{v'v}^k - p_{cc}^k)]}{\omega_{vc}^5} \end{aligned}$$

Here, i, j and k are Cartesian components, v and v' denote VB, and c and c' denote CB. $P(ijk)$ denotes full permutation. It should be emphasized that the refractive indices and SHG coefficients can be accurately obtained by DFT in principle because these optical properties are determined by the virtual electronic excited processes which are described by the first- and second-order perturbations, respectively, on the ground state wavefunctions.

RESULTS AND DISCUSSION

Structure. $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ belongs to an enormous compounds family in trigonal space group $R\bar{3}$ with an overall formula $\text{AM}_4\text{M}'_5\text{Q}_{12}$,⁴⁴⁻⁴⁷ where A, M, M' and Q represent an alkali metal cation with relatively large radius, a bivalent transition cation,

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4 a trivalent main group cation and chalcogens, respectively. The most notable
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6 structural feature of the above family is a quasi-cubic closest packing of the chalcogen
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8 atoms with the tetrahedral interspaces occupied by M and M' cations. It is worth
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10 mentioning that lots of members in this family have been identified, in which the M
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12 and M' can accommodate various types of cations (Mn^{2+} , Zn^{2+} , Cd^{2+} , and Ga^{3+} , In^{3+} ,
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14 *etc.*, respectively), showing rich substitutability of this structure model. However, our
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16 newly synthesized compound $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ is the first example in this family to place
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18 Hg^{2+} as the bivalent cation. We have also made a lot of attempts to synthesize other
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20 Hg-containing analogues, but unfortunately, the crystals of the In-containing selenide
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22 analogue were of poor quality in our synthesis and no sulfide analogues were found.
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24 The unit cell parameters of the title compound are $a = b = 14.3203(5)$ Å, $c = 9.7057(4)$
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26 Å, and $Z = 3$. In an asymmetric unit of the title compound, K, Hg/Ga and Se occupy
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28 one, three, and four unique sites, respectively. The multivalent metal positions are
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30 disordered by Hg and Ga atoms with respective occupancies of $0.3 - 0.577$ for Hg
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32 and $0.423 - 0.7$ for Ga (More details are listed in Table 2). Since no intermetallic
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34 bonds or diselenide bonds exist in the structure, the common oxidation states of $1+$,
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36 $2+$, $3+$ and $2-$ could be respectively distributed to K, Hg, Ga, and Se atoms. The
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38 calculated bond valence sums (BVS)⁴⁸ for all atoms (see Table 4) are in good
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40 accordance with the expected weighted average values, indicating the atom
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42 assignments are reasonable.
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54 The overall structure of the title compound is shown in Figure 2a. Clearly, all
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56 HgN/GaN ($N = 1, 2, 3$) atoms are surrounded by four Se atoms to form $(\text{HgN/GaN})\text{Se}_4$
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($N = 1, 2, 3$) tetrahedra with relatively large distortion (see Figure 3a, b, c), which are well aligned in an additive manner parallel to the c axis. These tetrahedra are first linked to each other by vertex-sharing to form a two-dimensional layer parallel to the ab plane (see Figure 2b), and then, the layers are stacked along the c axis to construct a overall three-dimensional framework with K^+ filling in the voids. Such a arrangement leads to a relatively large packing density of the NLO-active functional groups $(\text{Hg}/\text{Ga})\text{Se}_4$. The basic repeating building unit of a constituent layer can be derived as a $(\text{Hg}/\text{Ga})_9\text{Se}_{24}$ block, which contains three $(\text{Hg}1/\text{Ga}1)\text{Se}_4$ tetrahedra, three $(\text{Hg}2/\text{Ga}2)\text{Se}_4$ tetrahedra and three $(\text{Hg}3/\text{Ga}3)\text{Se}_4$ tetrahedra. The detailed connecting mode within a $(\text{Hg}/\text{Ga})_9\text{Se}_{24}$ block is shown in Figure 2c. The Hg/Ga – Se bonds lengths and Se – Hg/Ga – Se angles are in the range of 2.444(3) – 2.571(2) Å and $100.37(9)^\circ - 121.29(7)^\circ$, respectively, which are comparable with those observed in HgGa_2Se_4 (Hg – Se : 2.610(5) Å; Ga – Se : 2.403(2) Å and 2.409(0) Å; Se – Hg – Se : $109.17(6)^\circ - 110.06(2)^\circ$; Se – Ga – Se : $103.21(3)^\circ - 119.51(8)^\circ$).⁴⁹ The interstitial K atoms are bound to twelve Se atoms by weak electrostatic interactions (see Figure 3d), giving a cuboctahedron with four sets of K – Se distances (3.741(6) Å, 3.763(6) Å, 3.780(1) Å and 3.828(2) Å). These data are a little larger than the observed values of 3.335(9) – 3.586(3) Å in $\text{K}_2\text{Sn}_2\text{ZnSe}_6$,⁵⁰ and in good accordance with those in $\text{KCd}_4\text{Ga}_5\text{Se}_{12}$ (3.772(5) – 3.848(1) Å)⁴⁵ and $\text{K}_4\text{GeP}_4\text{Se}_{12}$ (3.265(4) – 3.903(4) Å).⁵¹

Structurally, the covalently bonded frameworks of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ and its ternary prototype HgGa_2Q_4 (Q = S, Se) are both comprised of corner-sharing HgQ_4 and GaQ_4 tetrahedra. Nevertheless, some apparent structural differences can still be summarized:

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4 (1) The Hg and Ga atoms in HgGa_2Q_4 occupy totally different positions, while in
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6 $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$, the bivalent cation Hg and trivalent cation Ga are completely
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8 disordered. (2) The detailed stacking modes of the basic motifs differ greatly between
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10 these two compounds. For HgGa_2Q_4 , it can be regarded as a derivative of the
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12 chalcopyrite-type compound AgGaQ_2 : about half of the monovalent Ag^+ cations in
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14 AgGaQ_2 are substituted by the bivalent Hg^{2+} cations, leaving the other half of the
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16 mono-metallic sites being vacancies. As for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$, that the alkali metal K
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18 occupies one of the Se positions makes the arrangement of the Se atoms no longer a
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20 closest packing manner. Apart from their structural differences, it is worth noting that
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22 the sulfide HgGa_2S_4 has long been studied as promising IR NLO materials (the
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24 selenide HgGa_2Se_4 has not been studied in detail yet), however, it is extremely
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26 difficult to obtain high-quality large-size HgGa_2S_4 single crystals. For our compound
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28 $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$, it exhibits much enhanced SHG response and longer transparent range
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30 compared with the sulfide HgGa_2S_4 (these properties will be discussed in detail in the
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32 next sections).
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41 **Raman Spectroscopy and UV-vis-NIR Diffuse Reflectance Spectroscopy.** A

42 Raman spectrum was recorded on the polycrystalline sample of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ (Figure
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44 4). Several obvious absorption peaks can be seen from 100 cm^{-1} to 500 cm^{-1} . The
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46 most distinct Raman shift at 196 cm^{-1} is attributed to the symmetric stretch of Hg – Se
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48 bonds, which is in good agreement with the observed 191 cm^{-1} peak in
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50 $\text{Cs}_2\text{HgSn}_3\text{Se}_8$.⁵² The peaks at 328 cm^{-1} and 413 cm^{-1} can be assigned to Ga – Se
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52 absorption modes, agreeing well with the fact that the lighter weight of a atom always
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4 results in a higher stretching frequency. Other absorptions below 200 cm^{-1} may arise
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6 from the K – Se vibrations.
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9 The optical band gap of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ was surveyed by the plot of $F(R)$
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11 (absorption data) versus $h\nu$ (photon energy) based on the Kubelka-Munk equation.⁵³⁻⁵⁶
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13 As displayed in Figure 5, a sharp absorption edge appears at about 770 nm
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15 corresponding to a band gap of 1.61 eV, which is in good accordance with the
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17 ‘dark-red’ color of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$. In addition, it is worth noting that very little optical
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19 absorption emerges below the band gap, indicating the polycrystalline sample has
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21 high purity and the light transmission cross over the title compound has not been
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23 disturbed. Such a band gap is close to that of commercial ZnGeP_2 (1.75 eV) and
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25 AgGaSe_2 (1.80 eV) and makes the material suitable for the common 2 μm laser as
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27 pumping source for IR laser generation. The band gap is smaller than that of
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29 commercial sulfide AgGaS_2 (2.56 eV) and may not be beneficial for increasing the
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31 laser damage threshold. However, the laser damage threshold is also influenced by
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33 other factors such as chemical composition, the thermal conductivity, and crystal
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35 quality. For example, ZnGeP_2 demonstrates much larger laser damage threshold than
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37 AgGaQ_2 (Q = S, Se) do for 2 μm pumping sources. For the transparent edge in the IR
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39 range, the crystal currently obtained via the spontaneous nucleation method is too
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41 small for measuring the transmission spectrum in the mid-far IR range, but as a
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43 selenide containing heavy metal Hg, its IR transparent range can be up to 20 μm ,
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45 significantly longer than those of the sulfide HgGa_2S_4 and AgGaS_2 as well as the
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47 phosphide ZnGeP_2 (around 13 μm). It is worthy noting that the search for NLO
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3 materials in the far IR or even the terahertz range is becoming increasingly important.
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6 **Thermal Stability.** The differential scanning calorimetric curve of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$
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8 is shown in Figure 6. The material is stable up to 700°C , then melts incongruently with
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10 two endothermic peaks at 742°C and 781°C and two exothermic peaks at 680°C and
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12 712°C during the entire heating/cooling cycle. The DSC curve indicates that
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14 $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ has relatively high thermal stability.
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18 **SHG Properties.** Owing to its structural asymmetry and favorable alignments of
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20 the functional groups, $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ is expected to exhibit strong SHG response. By
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22 applying the Kurtz–Perry method,³² the powder SHG response of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ has
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24 been studied in detail with a Q-switched Ho: Tm: Cr: YAG laser ($2.09\ \mu\text{m}$, 3Hz, 50 ns).
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26 As shown in Figure 7a, the SHG intensities grow gradually as the particle size
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28 increase and then reach a plateau, indicating that the title compound is
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30 phase-matchable at the common $2\ \mu\text{m}$ pumping sources. It should be emphasized that
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32 good phase-matchability is a highly desirable attribute for a IR NLO compound to
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34 become real applicable. Marvelously, if the SHG signals are compared at the same
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36 particle size range of $150 - 200\ \mu\text{m}$, the SHG response of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ would be
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38 about 20 times that of the commercialized material AgGaS_2 (see Figure 7b). To our
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40 best knowledge, such a value is one of the largest responses among all the
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42 phase-matchable IR NLO chalcogenides reported to date. For comparison, the SHG
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44 responses of some promising phase-matchable materials BaGa_4S_7 ,¹⁴ $\text{Ba}_6\text{Zn}_7\text{Ga}_2\text{S}_{16}$,⁵⁷
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46 $\text{Na}_4\text{MgGe}_2\text{Se}_6$,⁵⁸ $\text{NaGaIn}_2\text{Se}_5$,⁵⁹ and BaGa_4Se_7 ¹⁵ are only about 1.0, 1.0, 1.3, 2.1, 3.0
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48 times that of AgGaS_2 , respectively. Moreover, it is noteworthy that the Zn- and
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4 Cd-containing analogues⁴⁵⁻⁴⁷ have also been reported to exhibit large SHG efficiency,
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6 for example, by using the 2.05 μm pumping sources, the respective SHG responses of
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8 RbZn₄In₅Se₁₂, CsZn₄In₅Se₁₂ and KCd₄Ga₅Se₁₂ were experimentally determined as
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10 26.7, 25.0 and 26.8 times that of AgGaS₂ at the particle size of 46 – 74 μm . However,
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12 all these analogues exhibit non phase-matchable feature with the maximum SHG
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14 intensity realized at the small particle size of 46 – 74 μm , resulting from the relatively
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16 low birefringence (*e.g.*, the static birefringence of CsCd₄Ga₅Se₁₂, CsCd₄Ga₅Se₁₂ and
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18 CsCd₄In₅Se₁₂ at 2.05 μm were calculated as 0.003, 0.014 and 0.01, respectively).
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21 When compared at other larger particle size range (*e.g.*, 150 – 200 μm), the SHG
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23 responses of these analogues were significantly decreased (*e.g.*, the respective SHG
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25 intensities of RbZn₄In₅Se₁₂ and CsZn₄In₅Se₁₂ are only about 3.9 and 3.5 times that of
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27 AgGaS₂ at the particle size of 150 – 200 μm). But for our newly discovered
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29 compound KHg₄Ga₅Se₁₂, the introduction of the highly polarizable Hg–Se bonds with
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31 large susceptibility into the crystal structure of the title compound strengthen its
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33 anisotropic polarizability to a large extent, and thus exhibiting a favorable
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35 phase-matching feature (in other words, the SHG intensity of KHg₄Ga₅Se₁₂ increases
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37 as the particle size increases). As one may know, the birefringence (Δn) of a crystal is
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39 mainly decided by the anisotropic polarizability of its structure and a suitable
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41 birefringence is very practically profitable to achieve the phase-matching condition.
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43 From a structural point of view, the SHG response and birefringence of a crystal are
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45 closely related with the distortion degree and the packing density of the NLO-active
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47 functional groups. Basically, a dense packing and completely parallel alignment of the
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4 functional groups with large distortion would lead to a large SHG response and a
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6 appreciable birefringence. Take $AZn_4In_5Se_{12}$ ($A = Rb, Cs$) and $KCd_4Ga_5Se_{12}$ for
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8 example, the Zn/In – Se and Cd/Ga – Se bond lengths are in the range of 2.511(4) –
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10 2.545(4) Å, 2.458(2) – 2.554(2) Å, respectively, while in the case of $KHg_4Ga_5Se_{12}$, as
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12 discussed in the foregoing section, the Hg/Ga – Se bond lengths range from 2.444(3)
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14 to 2.571(2) Å. Clearly, the (Hg/Ga)Se₄ tetrahedra exhibit much more pronounced
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16 distortion than that (Zn/In)Se₄ and (Cd/Ga)Se₄ tetrahedra do, indicating that the
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18 Hg–Se bonds play a vital role in obtaining the phase-matching feature, while
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20 concurrently acquiring the large SHG efficiency. Additionally, considering the
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22 second-order coefficients of a compound are proportional to the square root of the
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24 SHG intensities, the corresponding coefficient of $KHg_4Ga_5Se_{12}$ can be derived as
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26 large as 58.1 pm/V, further suggesting the title compound may be used as a frequency
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28 converting material with very high efficiency.
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36 **Calculated Band Structure.** The electronic band structure along the highly
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38 symmetrical path of $KHg_4Ga_5Se_{12}$ clearly demonstrate that the title compound is a
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40 direct transition semiconductor with the calculated energy band gap of 0.9 eV (see
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42 Figure 8). It is generally accepted that the calculated band gap should be a little
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44 smaller than the measured value due to the discontinuity of exchange-correlation
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46 energy. Therefore, the scissor operators were adopted to shift all the conduction bands
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48 to match the calculated band gap with the measured value. Meanwhile, Figure 9
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50 displays the density of states (DOS) and the partial density of states (PDOS) projected
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52 on the constitutional atoms of the title compound. Accordingly, the following
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electronic characteristics could be inferred: (1) The region lower than -7 eV is consisted of the isolated inner-shell states of the constitutional atoms (K $3p$, Ga $3d$, Hg $5d$ and Se $4s$ orbitals). These orbitals have little interaction with neighboring atoms and contribute very little to the optical properties of the title compound. (2) The upper part of VBs is mainly composed of the Hg $6s$, Ga $4s4p$ and Se $4p$ orbitals, indicating that these atoms are involved in the formation of chemical bonding with relatively strong covalency. (3) The bottom part of CBs is dominated by the orbitals of all atoms. Since the optical behavior of a crystal mainly originates from the electronic transitions between the quantum states of the VBs and the CBs close to the band gap, the Hg/Ga-Se groups should be responsible for the linear and nonlinear optical properties of the compound, while the contribution from the alkali metal cation K^+ could be neglected.

First-principles Calculation of the Optical Properties. Being restricted by the Kleinman's symmetry rule, $KHg_4Ga_5Se_{12}$ should have four non-zero independent SHG coefficients (d_{11} , d_{15} , d_{22} and d_{33}) owing to its $R3$ space group. The static SHG tensors (*i.e.*, obtained at input photon energy of 0.0 eV) are calculated as below: $d_{11} = -44.945$ pm/V, $d_{15} = 45.238$ pm/V, $d_{22} = -42.481$ pm/V, $d_{33} = -65.257$ pm/V. The maximum coefficient ($d_{33} = -65.257$ pm/V) agrees with the powder SHG determination (58.1 pm/V). Meanwhile, it should be mentioned that the SHG coefficients are related to the input photon energy. Basically, there is a positive correlation between the SHG coefficients and the frequencies of the input photons. However, within a relatively small energy region (*e.g.*, 0 – 0.593 eV, corresponding to

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4 0 – 2090 nm), the change for the calculated values is small.⁴⁵ Hence, the above static
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6 values may still provide a approximate assessment about the experimental results. In
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8 order to gain a better understanding of the relationship between the optical properties
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10 and crystal structure of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$, a so-called real-space atom-cutting method was
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12 intend to be applied to assess the respective contribution of the functional anionic
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14 groups and cations to the SHG response. In the above method, the whole real space of
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16 the crystal cell is partitioned into several individual sphere zones corresponding to the
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18 respective ions (groups). The sizes of the sphere zones are mainly determined by the
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20 radius of the ions (the radii of the atoms contained in the groups). However, it should
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22 be noted that partially occupied structure (like the title compound) can not be used
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24 directly for the atom-cutting analysis. To make the atom-cutting analysis operable,
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26 several different configurations of the structure are designed in the symmetry of $P1$,
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28 where twelve Hg and fifteen Ga cations are randomly distributed over the
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30 twenty-seven $9b$ Wyckoff positions with 100% occupancy. By calculating the
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32 respective energy of these configurations, the most energy favorable one was
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34 identified. Then the real-space atom-cutting technique was conducted on this designed
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36 model. As shown in Table 5, the maximum coefficient d_{33} is -0.898 pm/V for K^+ (1.4%
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38 of d_{33}) and -63.938 pm/V for $(\text{Hg}/\text{Ga})\text{Se}_4$ (98.6% of d_{33}). This verifies the band
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40 structure analysis very well and further demonstrate that the origin of the SHG
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42 response of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ mainly arise from the $(\text{Hg}/\text{Ga})\text{Se}_4$ chromophores. To
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44 intuitive see the origin of the macroscopic SHG response of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$, the
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46 SHG-weighted densities of the occupied (see Figure 10a) and unoccupied electronic
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4 states (see Figure 10b) have been calculated. Obviously, the (Hg/Ga)Se₄ groups are
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6 the major source of the SHG-weighted electron densities in both occupied and
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8 unoccupied states. This result further indicates that the HgSe₄ and GaSe₄
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10 chromophores make the definitive contributions for the nonlinear optical properties of
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12 the title compound.
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16 It is generally accepted that, in a polar compound, the magnitude and direction of
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18 the local dipole moments of the functional groups determine the macroscopic SHG
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20 effects. To make the origin of the SHG response more clear, we have also quantified
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22 the local dipole moments of the Hg/Ga – Se groups for KHg₄Ga₅Se₁₂ with a simple
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24 bond-valence method as described previously.^{60,61} As calculated, the *x* and *y*
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26 components of the polarizations from all groups cancelled each other to zero, while a
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28 net dipole moment remained along the *z* direction, which is in accordance with the
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30 symmetry of its specific space group (*R*3). The *z* component of the static dipole
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32 moments of different groups (Hg1/Ga1)Se₄, (Hg2/Ga2)Se₄ and (Hg3/Ga3)Se₄ are
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34 -0.48 D, -0.11 D and 0.57 D, respectively. Considering a unit cell of the title
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36 compound contains twenty-seven such tetrahedra, thus, the corresponding local dipole
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38 moment of a unit cell would be -0.18 D. Such a remanent value is responsible for the
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40 large SHG efficiency of KHg₄Ga₅Se₁₂.
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49 Furthermore, the dispersion curves of the refractive indexes for KHg₄Ga₅Se₁₂ are
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51 depicted in Figure 11. On account of its specific symmetry, the title compound has
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53 two independent refractive indexes (*n_x* = *n_y*, and *n_z*). The derived birefringence (Δn) at
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55 1.06 μm and 2.09 μm are calculated as 0.054 and 0.072, respectively. Generally, good
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4 IR phase-matchability of a crystal normally require a moderate birefringence (0.04 –
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6 0.10).⁶² The too small birefringence ($\Delta n < 0.04$) is not adequate to achieve the
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8 phase-matching condition, while the too large birefringence ($\Delta n > 0.10$) may lead to
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10 some destructive optical behaviors. The calculated Δn value at 2.09 μm (0.072)
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12 indicates the title compound is likely to be phase-matchable, which corroborates the
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14 experimental observation very well. Particularly, although the title compound may be
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16 not suitable for the 1.06 μm laser as pumping source for IR laser generation due to its
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18 relatively narrow band gap, the calculated birefringence at 1.06 μm (0.054) still
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20 suggests that this material has very strong anisotropic polarizability at this specific
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22 wavelength. Hence, one may conclude that the introduction of the highly polarizable
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24 Hg–chalcogens bonds into a crystal structure would be an effective pathway to fulfill
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26 the phase-matchable requirements, while simultaneously acquiring large SHG
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28 efficiency.
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38 CONCLUSION

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41 To sum up, a new Hg-based infrared nonlinear optical material $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ has
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43 been synthesized and characterized. Its three-dimensional framework is composed of
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45 corner-sharing HgSe_4 and GaSe_4 tetrahedra with the counter-ion K^+ filling in the voids.
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47 Though $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ and its ternary prototype HgGa_2Se_4 have similar covalent
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49 structure, the cation occupancies and the detailed stacking modes of the basic motifs
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51 differ greatly between these two compounds. For this new material, it is very
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53 interesting that all the NLO-active chromophores (HgSe_4 and GaSe_4 tetrahedra) are
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4 arranged in a completely cooperative manner. The introduction of the highly
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6 polarizable Hg-Se bond can induce more pronounced distortion in the tetrahedral
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8 building units, and strengthen its anisotropic polarizability to a large extent, and thus
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10 result in a favorable phase-matching feature along with very large SHG response.
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12 According to the diffuse reflectance spectrum and electronic structure calculation,
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14 $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ is characterized as a direct transition semiconductor with the band gap
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16 of 1.61 eV. Moreover, the electronic band structure, the real-space atom-cutting
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18 analysis, together with the SHG-weighted electronic densities and the local dipole
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20 moments calculations reveal that the origin of the excellent linear and nonlinear
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22 optical properties of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ can be ascribed to the $(\text{Hg}/\text{Ga})\text{Se}_4$ group. These
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24 competitive features (good phase-matchability, very large SHG efficiency, wide
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26 transparency) make our newly discovered compound $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ a promising IR
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28 NLO material. Furthermore, this study further corroborates our consideration that
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30 Hg-based metal chalcogenides may be used as promising alternatives for IR NLO
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32 optics and may provide some insights for further exploration of IR NLO materials.
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34 Further effort, *i.e.*, growth on large-size single crystal for comprehensive assessment
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36 of this new IR NLO material is ongoing.
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ASSOCIATED CONTENT

Supporting Information

The crystallographic file in CIF format for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$. This material is available free of charge via the Internet at <http://pubs.acs.org>.

ACKNOWLEDGMENTS

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Figure Captions

Figure 1 The experimental powder X-ray diffraction pattern (red) and simulated pattern (black) of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 2 (a) The crystal structure of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$, in which a constituent layer is marked with a black dashed border. Tetrahedra: $(\text{Hg}/\text{Ga})\text{Se}_4$. (b) A single two-dimensional layer parallel to the ab plane. (c) The basic repeating building unit, $(\text{Hg}/\text{Ga})_9\text{Se}_{24}$, with the detailed atom numbers marked. 1: Hg1/Ga1; 2: Hg2/Ga2; 3: Hg3/Ga3.

Figure 3 The detailed coordination environment of (a) Hg1/Ga1; (b) Hg2/Ga2; (c) Hg3/Ga3; (d) K^+ . 1: Hg1/Ga1; 2: Hg2/Ga2; 3: Hg3/Ga3.

Figure 4 Raman spectrum of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 5 The UV-vis-NIR diffuse reflectance spectrum of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 6 The differential scanning calorimetric curve of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 7 (a) The phase-matching curve, i.e., SHG response versus particle size, for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$. (b) Oscilloscope traces of SHG signals of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ and AgGaS_2 (reference) in the particle size of 150 – 200 μm .

Figure 8 Electron band structure along highly symmetrical path in Brillouin zone of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 9 The partial density of states (PDOS) projected onto the constituted atoms of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 10 SHG-weighted densities for the (a) occupied and (b) unoccupied electronic states in $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Figure 11 The dispersion curves of the refractive indexes for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ in the range of 700 – 3500 nm.

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Figure 1

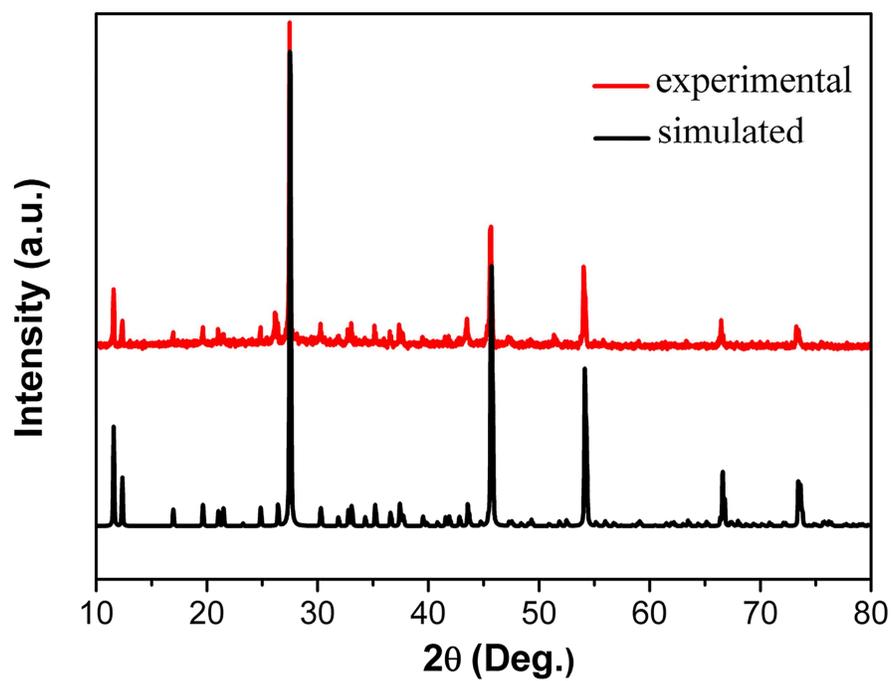


Figure 2

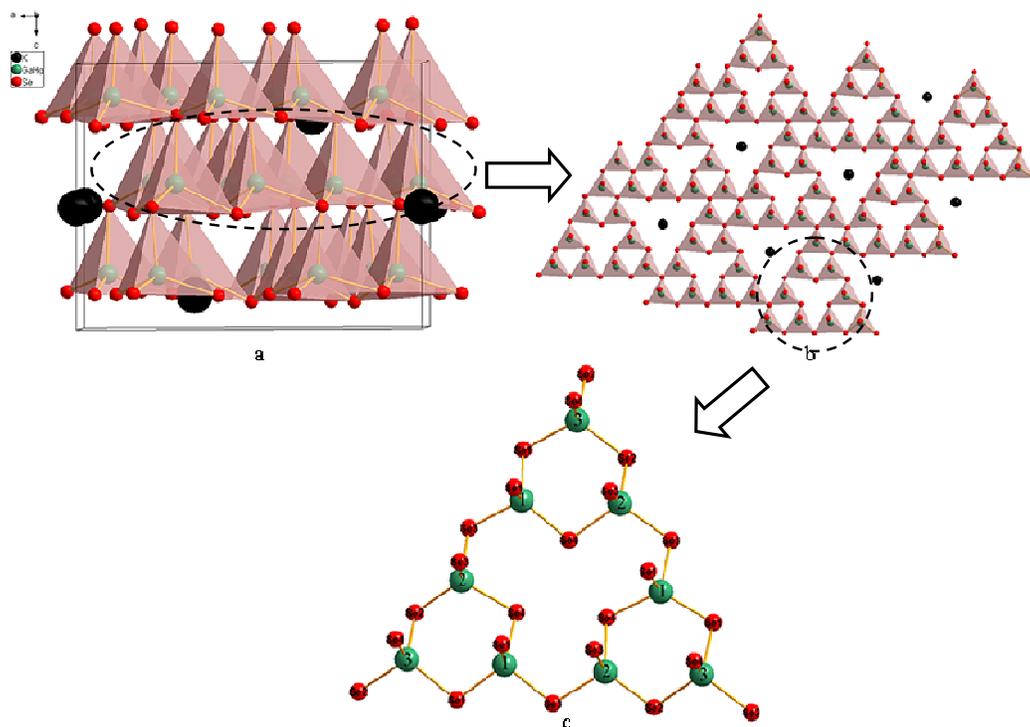


Figure 3

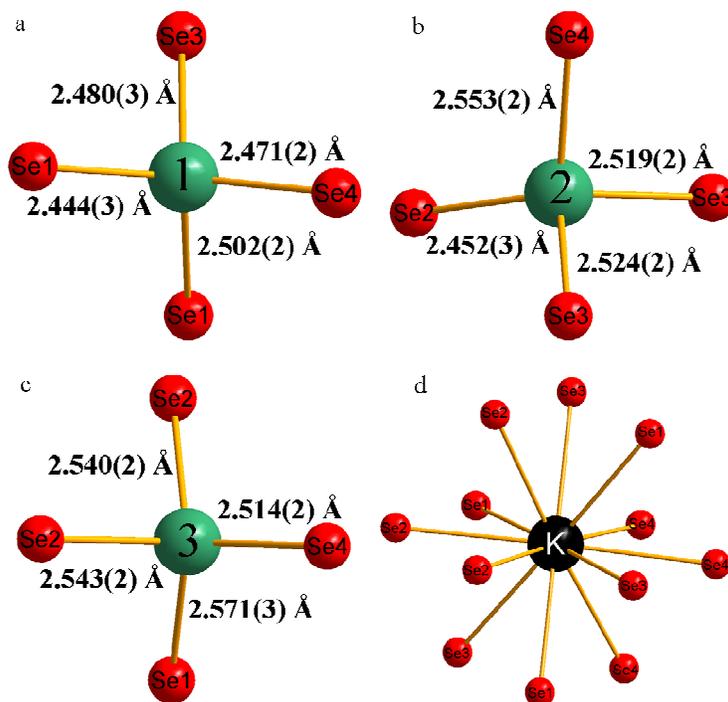


Figure 4

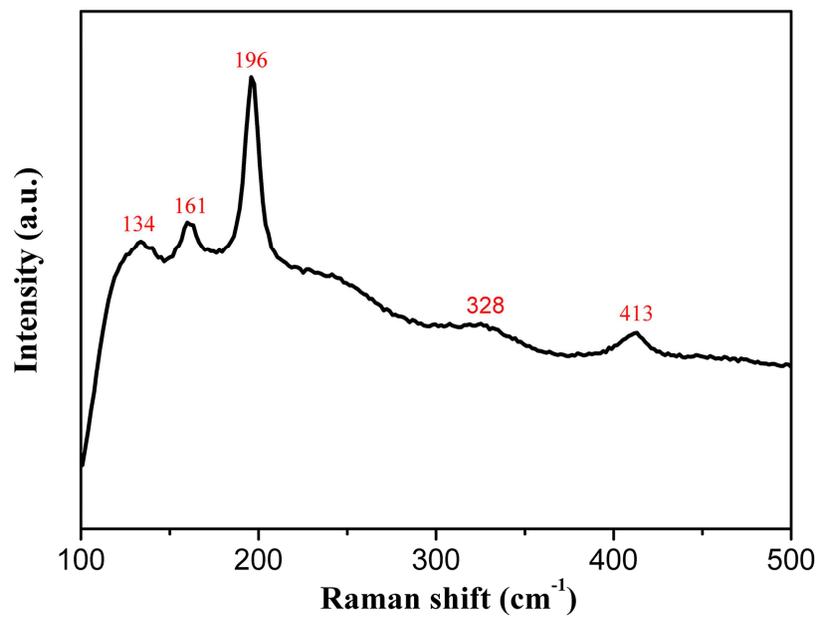


Figure 5

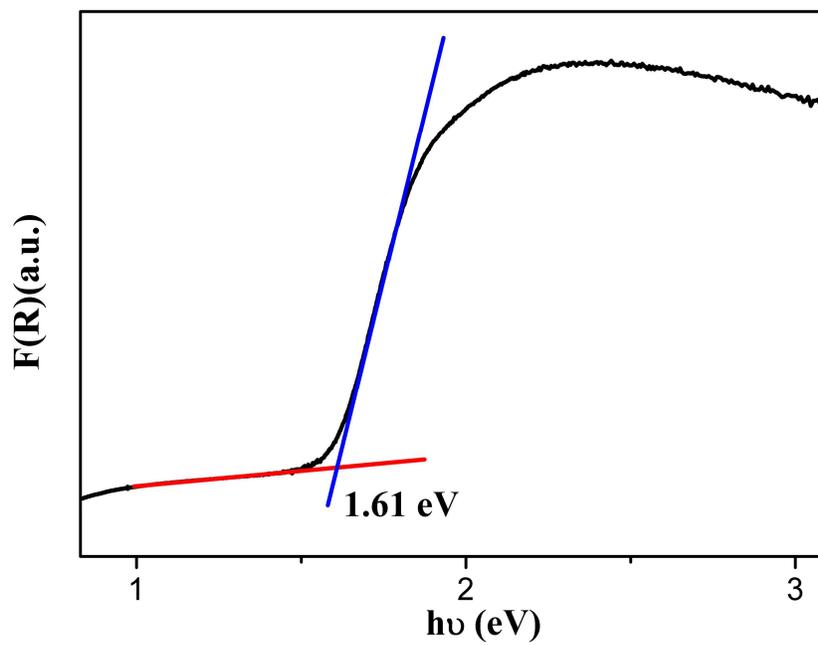
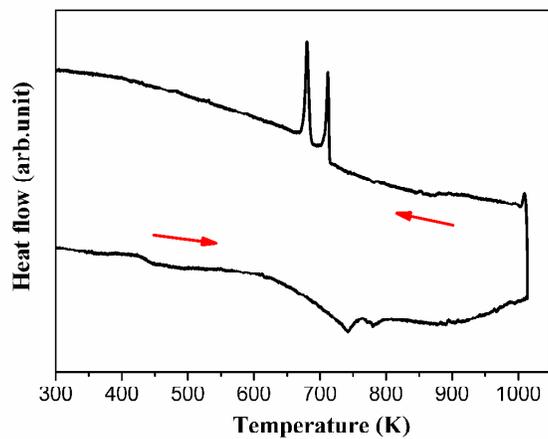


Figure 6



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Figure 7

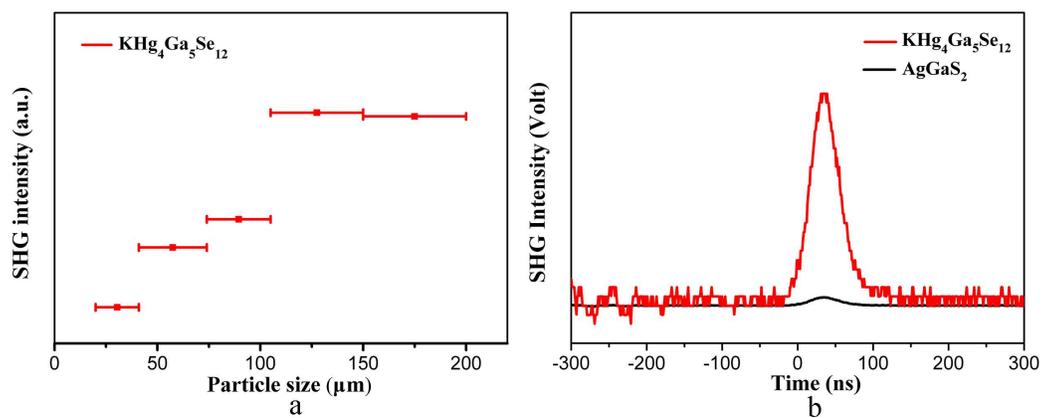


Figure 8

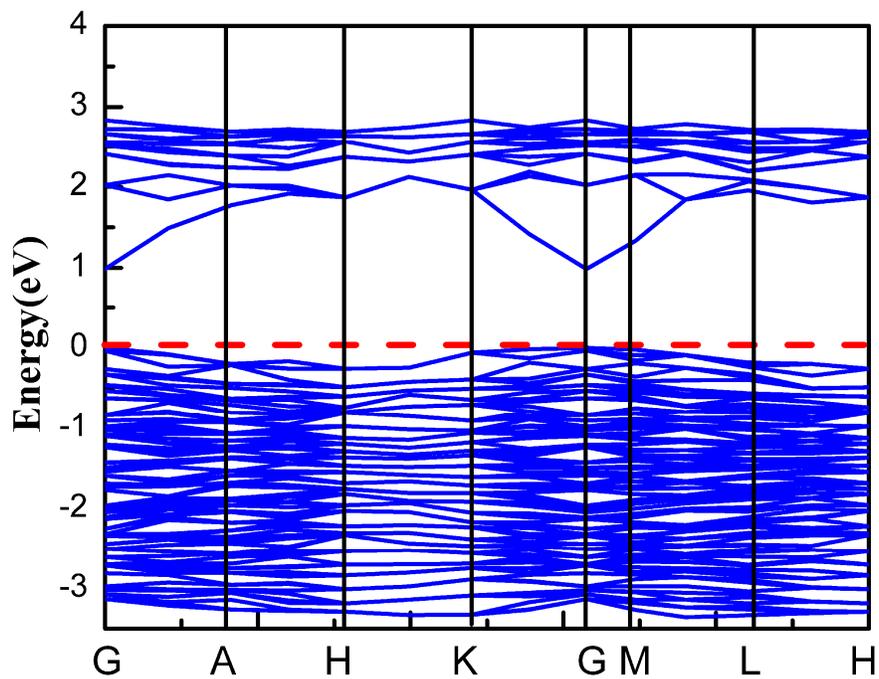


Figure 9

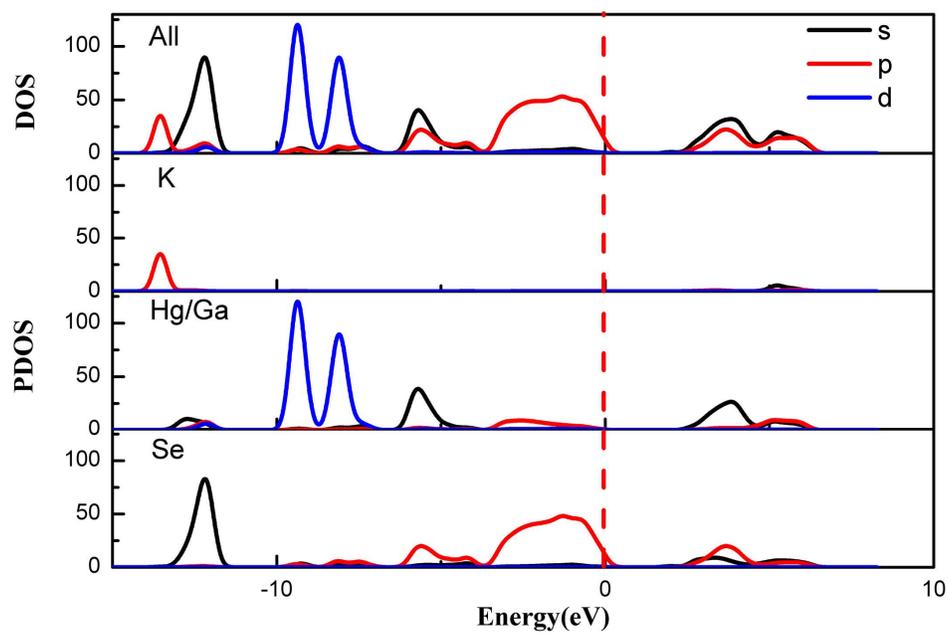


Figure 10

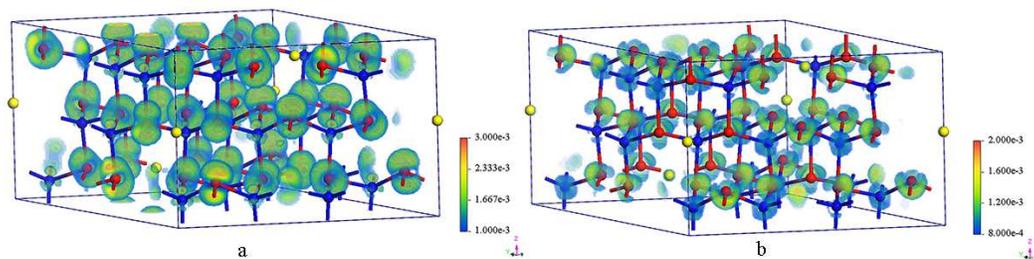


Figure 11

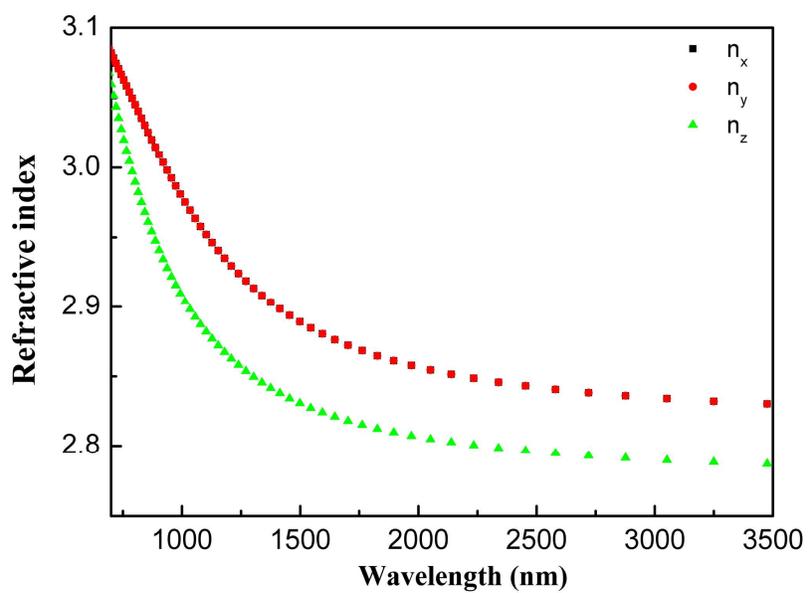


Table 1. Crystal data and structure refinement for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Chemical content	$\text{KHg}_4\text{Ga}_5\text{Se}_{12}$
Fw	2137.58
$a(\text{\AA})$	14.3203(5)
$b(\text{\AA})$	14.3203(5)
$c(\text{\AA})$	9.7057(4)
$\gamma(^{\circ})$	120.00
Space group	$R\bar{3}$
$V(\text{\AA}^3)$	1723.7(1)
Z	3
T(K)	293(2)
$\lambda(\text{\AA})$	0.7107
$\rho_c(\text{g/cm}^3)$	6.178
$\mu(\text{mm}^{-1})$	51.547
$R(F)^a$	0.0434
$R_w(F_o^2)^b$	0.0905
Flack parameter	-0.05(3)

$$^a R(F) = \sum | |F_o| - |F_c| | / \sum |F_o| \text{ for } F_o^2 > 2\sigma(F_o^2). \quad ^b R_w(F_o^2) = \{ \sum [w(F_o^2 - F_c^2)^2] / \sum w F_o^4 \}^{1/2}$$

for all data. $w^{-1} = \sigma^2(F_o^2) + (zP)^2$, where $P = (\text{Max}(F_o^2, 0) + 2F_c^2)/3$.

Table 2. Positional coordinates and equivalent isotropic displacement parameters for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

Atom	Wyckoff	x/a	y/b	z/c	$U_{\text{eq}} [\text{\AA}^2]$	Occupancy
K	$3a$	0.0000	0.0000	0.5403(7)	0.0287(2)	1.000
Hg1/Ga1	$9b$	0.0996(1)	0.7400(6)	0.4626(7)	0.0073(4)	0.300/0.700
Hg2/Ga2	$9b$	0.4132(4)	0.9821(4)	0.4607(0)	0.0096(3)	0.456/0.544
Hg3/Ga3	$9b$	0.7948(3)	0.5133(6)	0.4534(4)	0.0100(2)	0.577/0.423
Se1	$9b$	0.9227(3)	0.7060(5)	0.5392(8)	0.0179(4)	1.000
Se2	$9b$	0.5399(2)	0.1551(0)	0.5677(0)	0.0194(4)	1.000
Se3	$9b$	0.2242(0)	0.9284(3)	0.5357(6)	0.0182(4)	1.000
Se4	$9b$	0.4503(6)	0.8314(7)	0.5285(1)	0.0136(3)	1.000

Table 3. Selected bond lengths(Å) for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

$\text{KHg}_4\text{Ga}_5\text{Se}_{12}$	
Hg1/Ga1—Se1	2.444(3)
Hg1/Ga1—Se4	2.471(3)
Hg1/Ga1—Se3	2.480(2)
Hg1/Ga1—Se1	2.502(2)
Hg2/Ga2—Se2	2.452(2)
Hg2/Ga2—Se3	2.519(2)
Hg2/Ga2—Se3	2.524(3)
Hg2/Ga2—Se4	2.553(3)
Hg3/Ga3—Se4	2.514(2)
Hg3/Ga3—Se2	2.540(3)
Hg3/Ga3—Se2	2.543(2)
Hg3/Ga3—Se1	2.571(2)
K—Se2	3.741(6)×3
K—Se4	3.763(6)×3
K—Se1	3.780(1)×3
K—Se3	3.828(2)×3

Table 4. Calculated bond valence sums for $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$.

site	expected weighted averages	bond valence sums
K	1	0.711
Hg1/Ga1	2.7	2.856
Hg2/Ga2	2.544	2.754
Hg3/Ga3	2.423	2.656
Se1	-2	-2.107
Se2	-2	-2.028
Se3	-2	-2.089
Se4	-2	-2.109

Table 5. Calculated linear and nonlinear optical coefficients of $\text{KHg}_4\text{Ga}_5\text{Se}_{12}$ and real-space atom-cutting analysis.

	d_{11} (pm/V)	d_{15} (pm/V)	d_{22} (pm/V)	d_{33} (pm/V)
$\text{KHg}_4\text{Ga}_5\text{Se}_{12}$	-44.945	45.238	-42.481	-65.257
K^+	-0.486 (1.5%)	0.374 (1.8%)	-0.339 (1.9%)	-0.898 (1.4%)
$(\text{Hg}/\text{Ga})\text{Se}_4$	-32.763 (98.5%)	19.931 (98.2%)	-17.595 (98.1%)	-63.938 (98.6%)

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