# APPLICATION OF THE EXTENDED HAMMETT RELATIONSHIP TO THE IONIZATION CONSTANTS OF SUBSTITUTED ANTHRANILIC ACIDS ${ }^{1}$ 

P. LegGate ${ }^{2}$ and G. E. Dunn<br>Department of Chemistry, University of Manitoba, Winnipeg, Manitoba<br>Received November 30, 1964


#### Abstract

The overlapping ionization constants of the carboxyl and amino groups in 14 substituted anthranilic acids have been determined by a spectrophotometric method. The results have been fitted to the extended Hammett relationship $\log K_{1} K_{2} / K_{1}{ }^{0} K_{2}{ }^{0}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}}$, where $A$ and $B$ refer to ionization of the carboxyl and amino group, respectively. The values of $\rho_{1}$ and $\rho_{2}$ so obtained have been used to estimate $K_{z}{ }^{0}$, the equilibrium constant for ionization of neutral anthranilic acid to zwitterion.


An earlier paper (1) described an investigation of the rates of decarboxylation of 4and 5 -substituted anthranilic acids in nitrobenzene. Recently a parallel study of the decarboxylation of substituted salicylic acids in nonaqueous solvents has been performed (2). The extension of this work to the decarboxylation of anthranilic acids in water requires, as a first step, the determination of the two overlapping ionization constants of the acids. The complex character of the ionization equilibria of such acids in aqueous solution provides the opportunity for a somewhat unusual application of a linear free energy relationship.

## THE HAMMETT EQUATIONS

In aqueous solutions of anthranilic acids there are assumed to exist four ionic and molecular species in equilibria (3,4). These are shown in the diagram below, with the accompanying hydronium ions omitted.
[1]


The ionization constants $K_{1}$ and $K_{2}$, which are obtained experimentally, define the equilibria:

$$
\begin{gather*}
\stackrel{K_{1}}{\mathrm{RH}_{2}+} \mathrm{RH}+\mathrm{H}^{+} \\
\mathrm{RH}  \tag{2}\\
\stackrel{K_{2}}{\rightleftarrows} \mathrm{R}^{-}+\mathrm{H}^{+} .
\end{gather*}
$$

${ }^{1}$ Presented at the 1962 Chemical Institute of Canada Conference, Edmonton, Alberta. ${ }^{2}$ N.R.C. Posidoctorate Fellow, 1960-1962.
$\mathrm{RH}_{2}{ }^{+}$and $\mathrm{R}^{-}$are the species I and III, respectively, of eq. [1], RH is a mixture of zwitterion, $\mathrm{RH}^{ \pm}$(IIB), and 'non-zwitterion', $\mathrm{RH}^{0}$ (IIA). However, in the equilibria of eqs. [2] and [3], RH can be treated as a single species since the ratio of $\mathrm{RH}^{ \pm}$to $\mathrm{RH}^{0}$ is independent of pH .

The experimental ionization constants $K_{1}$ and $K_{2}$ are related to the 'true' constants $K_{\mathrm{A}}, K_{\mathrm{B}}, K_{\mathrm{C}}$, and $K_{\mathrm{D}}$ by the equations:
[5]
[6]

$$
\begin{align*}
K_{1} & =K_{\mathrm{A}}+K_{\mathrm{B}}  \tag{4}\\
1 / K_{2} & =1 / K_{\mathrm{C}}+1 / K_{\mathrm{D}} \\
K_{1} K_{2} & =K_{\mathrm{A}} K_{\mathrm{D}}=K_{\mathrm{B}} K_{\mathrm{C}}
\end{align*}
$$

Furthermore,

$$
\begin{equation*}
K_{\mathrm{z}}=\frac{K_{\mathrm{A}}}{K_{\mathrm{B}}}=\frac{K_{\mathrm{C}}}{K_{\mathrm{D}}}, \tag{7}
\end{equation*}
$$

where

$$
K_{z}=\frac{\left[\mathrm{RH}^{ \pm}\right]}{\left[\mathrm{RH}^{0}\right]} .
$$

For a series of substituted anthranilic acids, each of the ionization constants $K_{\mathrm{A}}, K_{\mathrm{B}}$, $K_{\mathrm{C}}$, and $K_{\mathrm{D}}$ should obey a Hammett relationship. If, however, there is strong hydrogen bonding between the amino and carboxyl groups, then two electronic pathways are available for transmitting the substituent effect. The extension of the Hammett equation to reaction series of this type has been discussed by Jaffe (5) who proposes the use of an equation of the form:

$$
\begin{equation*}
\log \frac{K}{\bar{K}^{\overline{0}}}=\rho_{1} \sigma_{1}+\rho_{2} \sigma_{2} \tag{8}
\end{equation*}
$$

This equation provides the means of estimating the relative importance of the two possible electronic paths in reactions in which, either two side chains react with one another, or the site of reaction is linked to the benzene ring at two points. The ionization of ortho-substituted benzoic acids represents a special case of the latter type. In this special case a hydrogen bond provides one of the two electronic pathways and a distinction can be made between a 'direct' substituent effect and an 'indirect' (and presumably less potent) effect exerted through the hydrogen bond. Jaffe showed (5) that, among the acids so far investigated, only the $o$-(hydroxymethyl)-benzoic acids provide evidence of a significant 'indirect' effect. However, as there is almost certainly a strong interaction between the amino and carboxyl groups of anthranilic acids, the possibility of indirect effects must be taken into account.

If we consider as an example the ionization constant $K_{\mathrm{A}}$, a substituent in, say, the 4 -position will behave as if para to the reaction site in exerting a direct effect on the ionization of the - COOH group and as if meta in exerting an indirect effect via the $-\mathrm{NH}_{3}{ }^{+}$group. The Hammett equation* is:

$$
\begin{equation*}
\log \frac{K_{\mathrm{A}}}{K_{\mathrm{A}}{ }^{0}}={ }_{\mathrm{D}} \rho_{\mathrm{A}} \sigma_{\mathrm{A}}+{ }_{\mathrm{I}} \rho_{\mathrm{A}} \sigma_{\mathrm{B}} \tag{9a}
\end{equation*}
$$

[^0]The corresponding equations for $K_{\mathrm{B}}, K_{\mathrm{C}}$, and $K_{\mathrm{D}}$ are:
[9c]
[9d]

$$
\begin{align*}
& \log \frac{K_{\mathrm{B}}}{K_{\mathrm{B}}^{0}}={ }_{\mathrm{I}} \rho_{\mathrm{B}} \sigma_{\mathrm{A}}+{ }_{\mathrm{D}} \rho_{\mathrm{B}} \sigma_{\mathrm{B}}  \tag{9b}\\
& \log \frac{K_{\mathrm{C}}}{\bar{K}_{\mathrm{C}}^{0}}={ }_{\mathrm{D}} \rho_{\mathrm{C}} \sigma_{\mathrm{A}}+{ }_{\mathrm{I}} \rho_{\mathrm{C}} \sigma_{\mathrm{B}} \\
& \log \frac{K_{\mathrm{D}}}{\bar{K}_{\mathrm{D}}{ }^{0}}={ }_{\mathrm{I}} \rho_{\mathrm{D}} \sigma_{\mathrm{A}}+{ }_{\mathrm{D}} \rho_{\mathrm{D}} \sigma_{\mathrm{B}}
\end{align*}
$$

Equation [9a] can be rewritten as:

$$
\begin{equation*}
K_{\mathrm{A}}=K_{\mathrm{A}}^{0} 10^{\left(\mathrm{D} \rho_{\mathrm{A}} \sigma_{\mathrm{A}+1} \rho_{\mathrm{A}} \sigma_{\mathrm{B}}\right)} \tag{10}
\end{equation*}
$$

and $K_{\mathrm{B}}, K_{\mathrm{C}}$, and $K_{\mathrm{D}}$ can be redefined in a similar manner. Substitution of these expressions for $K_{\mathrm{A}}, K_{\mathrm{B}}, K_{\mathrm{C}}$, and $K_{\mathrm{D}}$ in eqs. [4] and [5] enables $K_{1}$ and $K_{2}$ to be expressed in terms of Hammett parameters:

$$
\begin{gather*}
\left.K_{1}=K_{\mathrm{A}}^{0} 10^{(\mathrm{D}} \rho_{\mathrm{A}} \sigma_{\mathrm{A}+1} \rho_{\mathrm{A}} \sigma_{\mathrm{B}}\right)+K_{\mathrm{B}}{ }^{0} 10^{\left(\mathrm{I} \rho_{\mathrm{B}} \sigma_{\mathrm{A}+\mathrm{D}} \rho_{\mathrm{B}} \sigma_{\mathrm{B}}\right)}  \tag{11a}\\
\frac{1}{K_{2}^{-}}=\frac{1}{K_{\mathrm{C}}^{0}} 10^{-\left(\mathrm{D} \rho_{\mathrm{C}} \sigma_{\mathrm{A}+\mathrm{I}} \rho_{\mathrm{C}} \sigma_{\mathrm{B}}\right)}+\frac{1}{K_{\mathrm{D}}^{0}} 10^{-\left(\mathrm{I} \rho_{\mathrm{D}} \sigma_{\mathrm{A}+\mathrm{D}} \rho_{\mathrm{D}} \sigma_{\mathrm{B}}\right)} \tag{11b}
\end{gather*}
$$

These equations are obviously too complex to be fitted to the ionization constants, but fortunately a very much simpler Harmmett equation is available. Thus, from eq. [6] there may be obtained the logarithmic relationships:

$$
\begin{equation*}
\log \frac{K_{1} K_{2}}{K_{1}^{0} K_{2}{ }^{0}}=\log \frac{K_{\mathrm{A}} K_{\mathrm{D}}}{\bar{K}_{\mathrm{A}}^{0} \tilde{K}_{\mathrm{D}}{ }^{0}}=\log \frac{K_{\mathrm{B}} K_{\mathrm{C}}}{\bar{K}_{\mathrm{B}}{ }^{0} K_{\mathrm{C}}^{0}} \tag{12}
\end{equation*}
$$

Combining eqs. [12], [9a], and [9d] gives:

$$
\begin{equation*}
\log \frac{K_{1} K_{\mathrm{g}}}{K_{1}^{0} \bar{K}_{2}{ }^{0}}=\sigma_{\mathrm{A}}\left(\mathrm{D} \rho_{\mathrm{A}}+{ }_{\mathrm{I}} \rho_{\mathrm{D}}\right)+\sigma_{\mathrm{B}}\left({ }_{\mathrm{I}} \rho_{\mathrm{A}}+{ }_{\mathrm{D}} \rho_{\mathrm{D}}\right) \tag{13}
\end{equation*}
$$

Similarly, from eqs. [12], [9b], and [9c]:

$$
\begin{equation*}
\log \frac{K_{1} K_{2}}{K_{1}{ }^{0} \bar{K}_{2}{ }^{0}}=\sigma_{\mathrm{A}}\left({ }_{\mathrm{I}} \rho_{\mathrm{B}}+{ }_{\mathrm{D}} \rho_{\mathrm{C}}\right)+\sigma_{\mathrm{B}}\left({ }_{\mathrm{D}} \rho_{\mathrm{B}}+{ }_{\mathrm{I}} \rho_{\mathrm{C}}\right) \tag{14}
\end{equation*}
$$

However, if two or more sets of experimental data are available, a linear equation of general form:

$$
\log \frac{K_{1} K_{2}}{K_{1}^{0} K_{2}{ }^{0}}=A \sigma_{\mathrm{A}}+B \sigma_{\mathrm{B}}
$$

in which $A$ and $B$ are constants, must have a unique solution providing $\sigma_{\mathrm{A}}$ and $\sigma_{\mathrm{B}}$ are not themselves linearly related. Equations [13] and [14] can therefore be rewritten as a single equation.

$$
\begin{equation*}
\log \frac{K_{1} K_{2}}{K_{1}{ }^{0} K_{2}{ }^{0}}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}} \tag{15}
\end{equation*}
$$

where

$$
\begin{align*}
& \rho_{1}={ }_{\mathrm{D}} \rho_{\mathrm{A}}+{ }_{\mathrm{I}} \rho_{\mathrm{D}}={ }_{\mathrm{I}} \rho_{\mathrm{B}}+{ }_{\mathrm{D}} \rho_{\mathrm{C}},  \tag{16a}\\
& \rho_{2}={ }_{\mathrm{I}} \rho_{\mathrm{A}}+{ }_{\mathrm{D}} \rho_{\mathrm{D}}={ }_{\mathrm{D}} \rho_{\mathrm{B}}+{ }_{\mathrm{I}} \rho_{\mathrm{C}} .
\end{align*}
$$

Equation [15] defines a simple relationship between the experimental ionization constants and the Hammett parameters and it is, therefore, of importance that the chemical significance of this equation be defined. For this purpose it is convenient to consider the 'specific' case in which the postulated indirect substituent effects are assumed to be negligible. (Henceforth the 'general' case is that in which the indirect effects are taken into account and the 'specific' case is that in which indirect effects are assumed to be negligible.)

In the specific case the identities $[16 a]$ and $[16 b]$ simplify to:

$$
\begin{align*}
& \rho_{1}={ }_{\mathrm{D}} \rho_{\mathrm{A}}={ }_{\mathrm{D}} \rho_{\mathrm{C}},  \tag{17a}\\
& \rho_{2}={ }_{\mathrm{D}} \rho_{\mathrm{B}}={ }_{\mathrm{D}} \rho_{\mathrm{D}} . \tag{17b}
\end{align*}
$$

(For the remainder of this paper only $\rho_{\mathrm{A}}$ and $\rho_{\mathrm{B}}$ are referred to; the argument could equally well be pursued in terms of $\rho_{\mathrm{C}}$ and $\rho_{\mathrm{D}}$.)

The identity [17a] implies that the effect of a substituent on the ionization of the -COOH is the same whether an $\mathrm{NH}_{2}$ or $\mathrm{NH}_{3}{ }^{+}$group occupies the ortho position and the identity $[17 b]$ carries the same implication for the ionization of the $-\mathrm{NH}_{3}{ }^{+}$group. These conclusions are related to the principle, proposed by Jaffe (6), that the effect of a substituent is independent of a second substituent in an ortho position relative to the reacting side chain, provided that this ortho substituent does not participate in the reaction. The independence of the reaction constant on the nature of an ortho substituent should include the case where there is no ortho substituent. It follows, therefore, that within the limits of experimental error, $\mathrm{D}_{\mathrm{A}}$ should have the value 1.00 which is by definition the $\rho$-value for benzoic acid. Similarly, the value of ${ }_{D} \rho_{B}$ should show reasonable agreement with the experimentally determined value (7) of 2.889 for the Hammett reaction constant of the anilinium ion. From the identities [17a] and [17b] it follows that in the specific case eq. [15] becomes:

$$
\begin{equation*}
\log \frac{K_{1} K_{2}}{\bar{K}_{1}{ }^{0} K_{2}{ }^{0}}={ }_{\mathrm{D}} \rho_{\mathrm{A}} \sigma_{\mathrm{A}}+{ }_{\mathrm{D}} \rho_{\mathrm{B}} \sigma_{\mathrm{B}} \tag{18}
\end{equation*}
$$

This equation is mathematically identical to the eq. [8], proposed by Jaffe (5), for reactions in which the substituent effect can be transmitted by two electronic pathways. Equation [18], however, possesses a very different chemical significance. As implied by eq. [12], this equation provides a Hammett relationship for both the experimental constants $K_{1}$ and $K_{2}$ and the true constants $K_{\mathrm{A}}$ and $K_{\mathrm{D}}$ (or $K_{\mathrm{B}}$ and $K_{\mathrm{C}}$ ). When expressed in the latter terms it is seen as an application of the Hammett equation to two successive equilibria which are not readily distinguished by experimental means. The two equilibria may be represented (for example) by the lower half of eq. [1] which may be rewritten in an abbreviated form:

$$
\underset{\mathrm{I}}{K_{\mathrm{A}}} \stackrel{K_{\mathrm{D}}}{\rightleftarrows} \mathrm{IIB} \stackrel{\text { III }}{\rightleftarrows} .
$$

The character of the system requires that a substituent para (or meta) to the reaction center (the carboxyl group) in I is meta (or para) to the reaction center (the anilinium group) in $I I B$. The above interpretation can be extended to the general case represented by eq. [15]; this is an abbreviated form of eq. [13] which contains four Hammett reaction constants and represents the application of the Hammett relationship to a system of two successive equilibria, in each of which both indirect and direct substituent effects are assumed to operate. Whether or not the indirect effects are significant, eq. [15] enables
the product of the two experimental ionization constants to be fitted to a Hammett equation which can be solved for $\rho_{1}$ and $\rho_{2}$. Relationships between the individual constants ( $K_{1}$ or $K_{2}$ ) and the Hammett parameters are provided by eqs. [11] in the general case or in the specific case, by the equations

$$
\begin{gather*}
K_{1}=K_{\mathrm{A}}{ }^{0} 10^{\rho_{\mathrm{A}} \sigma_{\mathrm{A}}}+K_{\mathrm{B}}{ }^{0} 10^{\rho_{\mathrm{B}} \sigma_{\mathrm{B}}},  \tag{19a}\\
\frac{1}{K_{2}}=\frac{1}{K_{\mathrm{C}}^{0}} 10^{-\rho_{\mathrm{A}} \sigma_{\mathrm{A}}}+\frac{1}{K_{\mathrm{D}}{ }^{j}} 10^{-\rho_{\mathrm{B}} \sigma_{\mathrm{B}}} . \tag{19b}
\end{gather*}
$$

Thus, if a significant fit of the experimental data to eq. [15] is obtained, then the values of $\rho_{1}$ and $\rho_{2}$ required by this equation can be used to solve eqs. [11] or [19] for the true ionization constants $K_{A^{0}}{ }^{0}, K_{B_{B}}{ }^{0}, K_{\mathrm{C}}{ }^{0}$, and $K_{\mathrm{D}}{ }^{0}$ of anthranilic acid. Finally, by use of eq. [7] the zwitterion constant $K_{z}{ }^{0}$ and therefore the zwitterion content can be obtained. Providing that there is a statistically significant agreement between experimental data and the theoretical equations then we have a most unusual method for determining the zwitterion content of an aromatic amino acid. Furthermore, the fit of the experimental data to eqs. [11] or [19] could provide a criterion as to whether or not the indirect substituent effects are significant. However, this criterion must be used with caution as the extended computational sequence will greatly magnify errors in both the experimental data and the Hammett substituent constants. Lack of agreement between experiment and theory may well be due to these errors rather than indicative of indirect substituent effects.
In the above discussion the possible application of the Hammett equation to the $z$ witterion constant $K_{z}$ has been ignored. Actual $K_{z}$ values are difficult to determine and any such relationship could not be easily verified experimentally. Nevertheless, this equilibrium is of interest in that it involves the interaction of two side chains and is therefore subject to two 'direct' substituent effects. In this respect it is closely analogous to the intramolecular reaction of the $o$-nitroazides.


Andersen et al. (8) have recently correlated the rate constants for a series of substituted $o$-nitroazides by the use of a two-parameter Hammett equation of the type proposed by Jaffe (5):

$$
\begin{equation*}
\log \frac{K}{K^{0}}=\rho_{1} \sigma_{1}+\rho_{2} \sigma_{2} \tag{8}
\end{equation*}
$$

The $\sigma_{1}$ and $\sigma_{2}$ terms are the substituent constants of R relative to positions 1 and 2 , the points of attachment of the nitro and azido groups. Anderson found that $\rho_{1}$ is positive and $\rho_{2}$ negative in agreement with the rule that $\rho$-values are negative when a high electron density favors the reaction. Similarly, the tautomeric equilibrium defined by $K_{z}$ involves simultaneously the release of a proton from the - COOH group (favored by low electron density) and the acceptance of a proton by the $-\mathrm{NH}_{2}$ group (favored by high electron density). The expected Hammett equation would be:

$$
\log \frac{K_{Z}}{K_{\mathrm{Z}}{ }^{0}}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}},
$$

where $\rho_{1}$ is positive and $\rho_{2}$ negative. In the specific case in which the indirect substituent effects on the other equilibrium constants are ignored, $\rho_{1}$ and $\rho_{2}$ can be identified with the reaction constants $\rho_{\mathrm{A}}$ and $\rho_{\mathrm{B}}$. Thus

$$
\begin{equation*}
\log \frac{K_{\mathrm{Z}}}{K_{\mathrm{Z}}{ }^{\mathrm{V}}}=\rho_{\mathrm{A}} \sigma_{\mathrm{A}}-\rho_{\mathrm{B}} \sigma_{\mathrm{B}} . \tag{20}
\end{equation*}
$$

Both $\rho_{\mathrm{A}}$ and $\rho_{\mathrm{B}}$ are assumed to be positive as they are defined for reactions which are favored by a low electron density-the ionizations of the - COOH and $-\mathrm{NH}_{3}{ }^{+}$groups respectively. Equation [20] can also be deduced directly from eq. [7] on the assumption that $K_{\mathrm{A}}, K_{\mathrm{B}}, K_{\mathrm{C}}$, and $K_{\mathrm{D}}$ each obey a simple Hammett relationship.

Equation [15] is crucial to the present work in that it provides the simplest experimentally verifiable Hammett relationship for the system. However, in deducing this and other relationships, it has been assumed that eq. [1] is a valid representation of the equilibria existing in aqueous solutions of an anthranilic acid. The possibility must be considered that there are alternatives to this hypothesis. The only chemically reasonable alternative assumption is that the interactions between - COOH (or $-\mathrm{COO}^{-}$) and $-\mathrm{NH}_{2}$ (or $\mathrm{NH}_{3}{ }^{+}$) groups are so strong that it is impossible either to consider the zwitterion (IIB) and non-zwitterion (IIA) as separate species or to distinguish between ionizations from the -COOH and $-\mathrm{NH}_{3}{ }^{+}$groups. In such circumstances the ionic equilibria could be represented as:


Experimental and true ionization constants are now identical. The substituent effects will be somewhat similar to those found in reactions of the nitroazides, two 'direct' effects at a single reaction center. The Hammett equations would be:

$$
\begin{align*}
& \log \frac{K_{1}}{K_{1}{ }^{0}}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}},  \tag{22}\\
& \log \frac{K_{2}}{K_{2}{ }^{0}}=\rho_{3} \sigma_{\mathrm{A}}+\rho_{4} \sigma_{\mathrm{B}} . \tag{23}
\end{align*}
$$

A combination of eqs. [22] and [23] gives an equation which is mathematically identical to eq. [15]. This equation is therefore still valid even if the existing equilibria are represented by eq. [21]. However, if eq. [21] rather than eq. [1] represents the equilibria existing in aqueous solutions of anthranilic acids, then the data should fit eqs. [22] and [23] individually as well as eq. [15].

## DETERMINATION OF IONIZATION CONSTANTS

A spectrophotometric method for the determination of the overlapping ionization constants of dibasic acids was first described by Thamer and Voigt (9). This method was modified by Kok-Peng Ang (10) and, in this latter form, has been applied to aromatic amino acids by Bryson and Matthews (11). In the present work some further modifications were made, particularly as regards the method of computation.

The extinction coefficient, $\epsilon$, of an aqueous solution of a dibasic acid at any given wavelength is related to the hydrogen ion activity, $\alpha$, by the equation:

$$
\alpha^{2}\left(\epsilon-\epsilon_{1}\right)+\alpha K_{1}\left(\epsilon-\epsilon_{2}\right)+K_{1} K_{2}\left(\epsilon-\epsilon_{3}\right)=0 .
$$

In the present case $\epsilon_{1}, \epsilon_{2}$, and $\epsilon_{3}$ are the extinction coefficients of $\mathrm{RH}_{2}{ }^{+}$, RH, and Rrespectively, and $K_{1}$ and $K_{2}$ are the first and second ionization constants as defined in eqs. [2] and [3], $\epsilon_{1}$ and $\epsilon_{3}$ can be determined directly by measurements in acid or alkaline solutions, but $\epsilon_{2}$ is not directly available. In the present work all the solutions used in the determination of $K_{1}$ and $K_{2}$ for any particular acid were of the same concentration and it is therefore convenient to use $D$, the optical density, in place of $\epsilon$ in describing the method and carrying out the calculations. The above equation can therefore be rewritten:

$$
\begin{equation*}
\alpha^{2}\left(D-D_{1}\right)+\alpha K_{1}\left(D-D_{2}\right)+K_{1} K_{2}\left(D-D_{3}\right)=0 . \tag{24}
\end{equation*}
$$

Kok-Peng Ang's solution of this equation for $K_{1}$ and $K_{2}$ requires that some wavelength be found for which the variation of $D$ with pHI exhibits a maximum or minimum (Fig. 1). Any value of $D$ corresponding to the 'steep' portion of the curve will then define two values ( $\alpha_{1}, \alpha_{2}$ ) of $\alpha$ and thus provide two simultaneous equations of the form of eq. [24]. Combining these equations gives

$$
\begin{equation*}
D=D_{2}+K_{2} P \tag{25}
\end{equation*}
$$

where

$$
P=\frac{\left(D_{3}-D\right)\left(\alpha_{1}+\alpha_{2}\right)}{\alpha_{1} \alpha_{2}}
$$

and

$$
\begin{equation*}
D=D_{1}+K_{1} Q, \tag{26}
\end{equation*}
$$

where

$$
Q=\frac{D_{2}-D}{\alpha_{1}+\alpha_{2}} .
$$

A plot of $D$ against $P$ is linear with slope $K_{2}$ and intercept $D_{2}$. The value of $D_{2}$ is inserted into eq. [26] and $D$ is plotted against $Q$ to give $K_{1}$.

In the present work an IBM 1620 computer was available and computational labor


Fig. 1. Variation of optical density with pH at $\lambda=345 \mathrm{~m} \mu$ for anthranilic acid. Circles represent the experimental points of Table I and the line is calculated from eq. [24] using the parameters of Table II.
was not an important consideration. It was therefore possible to eliminate the following, otherwise unavoidable, wealknesses in the method of computation.
(i) The value of $K_{2}$ is highly dependent upon $D_{3}$, the optical density of an alkaline solution, which must therefore be determined with extreme accuracy to avoid undetectable, systematic error in $K_{2}$.
(ii) Similarly, and as previously pointed out by Bryson and Matthews (11), an error in the computed value of $D_{2}$ introduces a systematic error in to the calculation of $K_{1}$.
(iii) The usual 'least squares' procedure for determining the slope and intercept of a line assumes that only $y(=D)$ is in error and that $x(=P$ or $Q)$ is inerrant; this is clearly not true in the present case.

For the computation used in the present work eqs. [25] and [26] are rearranged;

$$
\begin{equation*}
D=\frac{D_{2}+K_{2} D_{3} A}{1+K_{2} A} \quad \text { from }[25] \tag{27}
\end{equation*}
$$

where
[28]

$$
A=1 / \alpha_{1}+1 / \alpha_{2}
$$

$$
D=\frac{D_{1}+K_{1} D_{2} A^{1}}{1+K_{1} A^{1}} \quad \text { from }[26]
$$

where

$$
A^{1}=1 /\left(\alpha_{1}+\alpha_{2}\right)
$$

Equations [27] and [28] were solved on the computer by Dolittle's least squares method $(12,13)$ which takes into account errors in both $D$ and $\alpha$ and thus provides more reliable estimates of the standard errors of the parameters. By this method independent values for $K_{1}$ and $K_{2}$ are obtained without the necessity of determining either $D_{1}$ or $D_{3}$. Furthermore two independent estimates of $D_{2}$ are available as a test of the consistency of the calculations.

The method of obtaining the values of $D, \alpha_{1}$, and $\alpha_{2}$ for use in the computation of $K_{1} K_{2}$ was also modified. Kok-Peng Ang's procedure required that a continuous curve be constructed through the experimental points (pII, D). The values of $\alpha_{1}$ and $\alpha_{2}$ are then read from the curve. However, the responsibility of drawing a 'true' curve can be avoided. Thus, in the present work, using the determination of $K_{2}$ as the example, the values of $D$ and $\alpha_{2}$ which are used in the calculation are the actual experimental points. To obtain the corresponding values of $\alpha_{1}$ it is still necessary to draw a curve through the experimental points on the low pH side of the maximum. However, in eq. [27] the terms $\alpha_{1}$ and $\alpha_{2}$ appear only in the function $A=1 / \alpha_{1}+1 / \alpha_{2}$. For most values $1 / \alpha_{2} \gg 1 / \alpha_{1}$, and errors in $\alpha_{1}$ due to inaccurate curve construction have a negligible effect on the accuracy of the overall calculation.

Similarly for $K_{1}, D$ and $\alpha_{1}$ are experimental points and $\alpha_{2}$ is obtained from a constructed curve.

## EXPERIMENTAL

## (A) Preparation of the Substituted Anthranilic Acids

The 5 -chloro, 5 -hydroxy, and 5 -methyl anthranilic acids, and anthranilic acid itself, were commercial products. The 5 -bromo, 4 -chloro, 4 -nitro, and 5 -nitro acids were prepared as described by Dunn and Prysiazniuk (1). The compound described in that paper as the 4 -bromoanthranilic acid was found to be the 5 -bromo isomer; an unambiguous synthesis of the 4 -bromo acid is described in the present paper.

All the anthranilic acids were purified by one or more recrystallizations from aqueous ethanol in the presence of animal charcoal. The melting points given are for the recrystallized acids. All melting points were determined with a Hershberg melting point apparatus (14) using Anschutz thermometers and are expressed in ${ }^{\circ} \mathrm{C}$.
'Analar' acetone was purified for use in the permanganate oxidations by distillation from solid potassium permanganate.

4-Methylanthranilic Acid
4-Methyl-2-nitrobenzoic acid was prepared by the procedure described by Grob (15). 4-Methyl-2nitroaniline was diazotized and the diazonium solution treated with cuprous cyanide to yield the 4 -methyl-2nitrobenzonitrile, which was hydrolyzed to the 4 -methyl-2-nitrobenzoic acid. The crude nitro acid ( 10 g ) in ethanol ( 75 ml ) was hydrogenated during 20 min at 3 atm pressure in the presence of $10 \%$ palladium-oncharcoal ( 1.0 g ). 4-Methylanthranilic acid ( $6.0 \mathrm{~g}, 65 \%$ ) was recovered from the reaction mixture and, after recrystallization from aqueous ethanol, had m.p. 181-182 ${ }^{\circ}$ (lit. (15) $178-180^{\circ}$ ).
4-Methoxyanthranilic Acid
4-Methoxy-2-nitrobenzoic acid, m.p. 192-193 ${ }^{\circ}$, was prepared from 4 -methoxy-2-nitroaniline by the procedure of Steven et al. (16) who give m.p. 195-196 ${ }^{\circ}$. The nitro acid was hydrogenated under conditions already described (for the 4 -methyl-2-nitro acid) to give a $73 \%$ yield of 4 -methoxyanthranilic acid, m.p. $180-181^{\circ}$ (lit. (16) $180-181^{\circ}$ ).

## 5-Methoxyanthranilic Acid

4-Methoxy-2-methylaniline ( 93 g ) was dissolved in 0.4 N hydrochloric acid (1.71) to give a darkbrown solution which was stirred with animal charcoal and filtered. To this filtrate at $50^{\circ}$ were added acetic anhydride ( 82 ml ) and then sodium acetate trihydrate ( 109 g ). The solution was cooled to $15^{\circ}$ to precipitate the 4 -methoxy-2-methylacetanilide ( $100 \mathrm{~g}, 82 \%$ ) which had m.p. $135-136^{\circ}$ (lit. (17) $132-134^{\circ}$ ). The anilide $(10.00 \mathrm{~g})$ in acetone ( 500 ml ) was treated with potassium permanganate ( 27.0 g ) and magnesium sulfate during 48 h at room temperature. Sodium sulfite was then added to destroy excess permanganate and the reaction mixture was filtered. The filtrate was evaporated to 100 ml , diluted with water, and extracted with chloroform to remove unreacted starting material. Acidification yielded N -acetyl-5-methoxyanthranilic acid ( $3.9 \mathrm{~g}, 85 \%$ of reacted material), m.p. $165-166^{\circ}$ (lit. (18) $165-166^{\circ}$ ). Hydrolysis of the acetylanthranilic acid ( 7.6 g ) was accomplished by warming for 30 min with 6 N sodium hydroxide solution. Acidification of the alkaline solution precipitated 5 -methoxyanthranilic acid ( $2.5 \mathrm{~g}, 42 \%$ ), m.p. $151-152^{\circ}$ (lit. (19) $151^{\circ}$ ).

## 4-Fluoroanthranilic Acid

The preparation of this acid from 5-fluoro-2-methylaniline followed the published procedure of Steck and Fletcher (20). The 4-fluoroanthranilic acid so prepared had m.p. 198-199 (lit. (20) 192.5-193.0 ${ }^{\circ}$ ).

## 5-Fluoroanthranilic Acid

The 5 -fluoro acid was obtained from 4 -fluoro- 2 -methylaniline by the successive acetylation, oxidation, and hydrolysis steps which are described in detail for the preparation of 5 -methoxyanthranilic acid. Acetylation of the aniline gave an $87 \%$ yield of 4-fluoro-2-methylacetanilide, m.p. 110-112 (lit. (21) $113^{\circ}$ ), which was oxidized in $43 \%$ yield to 5 -fuoro-N-acetylanthranilic acid, m.p. $178^{\circ}$. Hydrolysis of this compound gave a $91 \%$ yield of the 4 -fluoroanthranilic acid, m.p. 183-184 (lit. (22) $180^{\circ}$ ).

5-Phenoxyanthranilic Acid
2-Nitro-5-chlorobenzoic acid ( 25 g ) was reacted with potassium phenoxide in nitrobenzene solution as described by Süs and Möller (23) to give 5-phenoxy-2-nitrobenzoic acid ( $14 \mathrm{~g}, 65 \%$ ), m.p. $154-155^{\circ}$ (lit. (23) $157^{\circ}$ ). Hydrogenation of the crude nitro acid ( 14 g ) under conditions already described in the present paper gave 5 -phenoxyanthranilic acid ( $9 \mathrm{~g}, 70 \%$ ), m.p. $148-149^{\circ}$ (lit. (23) $148^{\circ}$ ). Attempts to apply the same method to the preparation of the 4-phenoxyanthranilic acid were unsuccessful, even though the more reactive 2 -nitro- 4 -bromobenzoic acid was used in place of the 4 -chloro compound. This failure is to be expected in the absence of an activating nitro group para to the halogen atom.

4-Bromoanthranilic Acid
4-Bromo-2-nitrobenzoic acid was prepared from o-nitroaniline by the three stage procedure of Erickson et al. (24). Bromination of the $o$-nitroaniline gave an $84 \%$ yield of 4 -bromo- 2 -nitroaniline, m.p. $105-106^{\circ}$ (lit. (24) $111-112^{\circ}$ ), which was then diazotized and the diazonium solution treated with cuprous cyanide to give 4 -bromo- 2 -nitrobenzonitrile in $67 \%$ yield. The nitrile was hydrolyzed to 4 -bromo- 2 -nitrobenzoic acid, m.p. $161-162^{\circ}$ (lit. (24) $164-165^{\circ}$ ). The nitroacid ( 10.8 g ) was dissolved in ammonium hydroxide solution and treated with ferrous ammonium sulfate hexahydrate ( 100 g ) in water ( 200 ml ). The reaction mixture was boiled briefly, cooled, and filtered. Acidification of the filtrate gave 4 -bromoanthranilic acid $\left(7.0 \mathrm{~g}, 83 \%\right.$ ), m.p. $225^{\circ}$ (lit. ( 25 ) $222^{\circ}$ ). A melting point depression was observed on mixing with 5 -bromoanthranilic acid (m.p. 215-216 ${ }^{\circ}$ ).
A small quantity of the 4 -bromo compound was converted by a diazotization procedure to 4 -bromosalicylic acid, m.p. $203-204^{\circ}$ (lit. (26) $214^{\circ}$ ). This compound was readily distinguished both by melting point and mixed melting point from the 5-bromo isomer which has m.p. $169^{\circ}$. It is of interest that in one recent paper (27) a melting point of $164-165^{\circ}$ is quoted for 4 -bromosalicyclic acid; it is almost certain that this was in fact the 5 -isomer.

## (B) $p K_{a}$ Determinations

All measurements were made on solutions of ionic strength $\mu=0.10$ since for the stronger acids it was necessary to measure optical densities at pH 's as low as 1 . Consequently, only apparent $\mathrm{p} K$ values are reported. These are adequate for the present purpose since the Hammett relationships always concern differences between the $\mathrm{p} K$ 's of substituted and unsubstituted aromatic acids where the activity coefficients will be very similar and cancel.

Experimental Procedure
Stock solutions of each acid were prepared by dissolving the appropriate weight of the acid in a slight excess of sodium hydroxide ( 0.1 N ) and then diluting to 11 with distilled water containing sufficient potassium chloride to give an ionic strength of 0.10 . Aliquots ( 10 ml ) of this stock solution, delivered from an automatic burette, were diluted to 50 ml with the appropriate buffer to give the solutions on which pH and optical density $(D)$ determinations were made. Preliminary experiments were performed on solutions of each acid in 10 to 12 buffers spauning the range 1.0-5.5. The absorption spectra of these solutions in the range $2750-4500 \AA$ were recorded. These spectra indicated the optimum wavelength for a $p K_{a}$ determination, the required concentration of the stock solution, and the approximate pH ranges of the 'steep' portions of $\mathrm{pH} / D$ curve at the chosen wavelength. In the actual $\mathrm{p} K_{\mathrm{n}}$ determinations the buffers were chosen so as to concentrate the experimental points in these steep portions.

Solutions of all the acids eventuaily became colored on standing, but in the case of the 5-methoxy, 5 -hydroxy, and 5-bromo acids and in particular the 5-phenoxy acid, discoloration was observed within a few hours and anomalous optical density readings resulted. Stock solutions of these acids were therefore prepared in oxygen-free water and stored in opaque bottles under nitrogen. Under these conditions no significant variations in optical density were observed during the course of the $\mathrm{p} K_{\mathrm{a}}$ determination.
Buffer Solutions
Hydrochloric acid (pH1 1.0-1.8), chloroacetate (1.9-3.6), acetate (3.7-5.4), and phosphate (5.7, 6.0, 6.8) buffers were used. All buffers were adjusted to ionic strength 0.10 by addition of potassium chloride. In some initial experiments citrate buffers were used. It was found, however, that the optical density of an acid in a citrate buffer was significantly higher than that in hydrochloric acid or acetate buffers of the same pH and it was assumed that some degree of complex formation was occurring.

## pH Measurements

These were made with a Radiometer Model 4C pHI meter with shielded g lass and silver chIoride electrodes in a water bath thermostatically controlled at $25.0 \pm 0.1^{\circ}$. The instrument was standardized at pH 's 1.68 , 4.01 , and 6.80 with potassium tetroxalate ( 0.1 N ), potassium hydrogen phthalate ( 0.1 N ), and sodium hydrogen phosphate - potassium hydrogen phosphate ( 0.25 N ) buffers prepared from the corresponding National Bureau of Standards pH standards.

## Optical Density Measurements

A Beckman DK1 spectrophotometer was used with matched cells contained in a thermostated cell holder at $25.0 \pm 1.0^{\circ}$. The appropriate buffer solution was used as a standard in the reference cell. In making a $\mathrm{p} K_{\mathrm{a}}$ determination the instrument was set at the predetermined optimum wavelength throughout the determination. For each solution a record was made of the optical density over a period of several minutes during which the temperature of the cell oscillated between $24^{\circ}$ and $26^{\circ}$ several times. This temperature variation produced changes in the optical density of not more than 0.001 absorbance units, except in the case of strongly acid solutions of the nitro acids, in which slightly larger variations were observed.

## RESULTS

Table I details the experimental data for anthranilic acid itself. Solutions Nos. 1-11 define the steep portion of the curve on the low pH side of the maximum and solutions Nos. $12-25$ the steep portion on the high pH side. These data were used to solve eqs. [27] and [28] by the methods already described.

The values of $\mathrm{p} K_{1}$ and $\mathrm{p} K_{2}$ (and $K_{1}$ and $K_{2}$ ) calculated from these data are given in Table II, row 1 , which also shows the excellent agreement between the two values obtained for $D_{2}$, and between the computed value for $D_{3}$ and an experimental value. The values of $K_{1}$ and $K_{2}$ from a second, independent experiment using a different concentration of anthranilic acid are also given in Table II. The mean values of $K_{1}$ and $K_{2}$ from the two experiments are seen to be in agreement with previously published values.

Figure 1 compares the experimental data of Table I with a pH vs. $D$ curve defined by eq. [24], using the computed values for the parameters $K_{1}, K_{2}, D_{1}, D_{2}$, and $D_{3}$. (The mean of the two computed values of $D_{2}$ was used.) A test of the degree of coincidence between experimental data and theoretical equation is given by the value of $s$ (ext.), the external estimate of error.* This is 0.005 for both equation [27] which gives $K_{2}$ and eq. [28] which

[^1]TABLE I
Optical densities of $3.34 \times 10^{-4} M$ solutions of anthranilic acid at $\lambda=345 \mathrm{~m} \mu$ and $\mu=0.10$

| Soln. No. | pH | Optical density | Soln. No. | pH | Optical density |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.879 | 0.769 | 12 | 4.458 | 0.779 |
| 2 | 2.820 | 0.753 | 13 | 4.557 | 0.775 |
| 3 | 2.756 | 0.735 | 14 | 4.647 | 0.718 |
| 4 | 2.667 | 0.684 | 15 | 4.723 | 0.687 |
| 5 | 2.582 | 0.666 | 16 | 4.813 | 0.678 |
| 6 | 2.523 | 0.629 | 17 | 4.897 | 0.643 |
| 7 | 2.458 | 0.608 | 18 | 4.982 | 0.620 |
| 8 | 2.408 | 0.573 | 19 | 5.074 | 0.592 |
| 9 | 2.339 | 0.533 | 20 | 5.182 | 0.562 |
| 10 | 2.268 | 0.492 | 21 | 5.266 | 0.541 |
| 11 | 2.206 | 0.467 | 22 | 5.350 | 0.515 |
|  |  |  | 23 | 5.444 | 0.499 |
|  |  |  | 24 | 5.533 | 0.480 |
|  |  |  | 25 | 5.634 | 0.460 |
|  |  |  | 26 | 0.1 N NaOH | 0.390 |

gives $K_{1}$. The actual experimental uncertainty in the optical density, $D$, (i.e., the internal estimate of error) is about 0.005 .

Ionization constants were obtained for 15 substituted anthranilic acids. Values of $K_{1}, K_{2}$, and $D_{2}$ are given in Table III, including duplicate determinations which were made for four of the acids. For these acids the weighted mean of the duplicate values of $K_{1}$ and $K_{2}$ were used in the calculations of the Hammett relationships described in the next section. No value of $K_{1}$ is given for the 5 -nitro acid, which exhibited a very broad maximum at a very low pH . The determination of $K_{1}$ would have required the use of very strongly acidic solutions for which sufficiently accurate pH data were unobtainable.

The third ionization constant of 5 -hydroxyanthranilic acid, involving ionization of the hydroxyl group, was readily accessible from our data so it was calculated although it was not needed for the purposes of this paper.

$$
K_{3}=\frac{\left[\mathrm{A}^{-}\right]\left[\mathrm{H}^{+}\right]}{\left[\mathrm{A}^{-}\right]} .
$$

On the assumption that there is no significant overlapping of the second and third ionization constants, $K_{3}$ may be determined approximately by use of the relationship:

$$
K_{3}=\frac{\left(D-D_{3}\right) a}{D_{4}-D},
$$

where $D_{3}$ and $D_{4}$ are optical densities of solutions of the same concentration containing only $\mathrm{A}^{-}$and $\mathrm{A}^{-}$respectively. $D$ is the optical density at hydrogen ion concentration $a$. A value of $D_{3}$ has already been computed in the calculation of $K_{2} ; D_{4}$ was obtained by measurement of a solution in 0.10 N sodium hydroxide. Using $D_{3}=0.154, D_{4}=0.929$, $D=0.414$ at $\mathrm{pH}=9.069$, the values $K_{3}=4.31 \times 10^{-10}, \mathrm{p} K_{3}=9.36$ were obtained.

DISCUSSION
Equation [15] can be written in the form:

$$
\begin{equation*}
\log K_{1} K_{2}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}}+\log K_{1}{ }^{0} K_{2}{ }^{0} . \tag{15}
\end{equation*}
$$

TABLE II
Apparent ionization constants of anthranilic acid at $25^{\circ} \mathrm{C}$ and $\mu=0.10$

|  | $K_{1} \times 10^{3}$ | $K_{2} \times 10^{5}$ | $\mathrm{p} K_{1}$ | pK 2 | $D_{2}$ |  | $D_{3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | (From $K_{1}$ ) | (From $\mathrm{K}_{2}$ ) | (Calcd.) | (Expt.) |
| Experiment ${ }^{*}$ | $6.97 \pm 1.20$ | $1.46 \pm 0.14$ | $2.16 \pm 0.07$ | $4.84 \pm 0.04$ | $0.935 \pm 0.016$ | $0.944 \pm 0.018$ | 0.387 | 0.387 |
| Experiment $2^{*}$ | $6.72 \pm 0.37$ | $1.40 \pm 0.10$ | $2.17 \pm 0.02$ | $4.85 \pm 0.03$ | $0.912 \pm 0.008$ | $0.919 \pm 0.010$ | 0.383 | 0.381 |
| Weighted Mean* | $6.74 \pm 0.36$ | $1.42 \pm 0.08$ | $2.17 \pm 0.02$ | $4.85 \pm 0.03$ |  |  |  |  |
| Liquori and Ripamonti (28) $\dagger$ | 7.32 | 1.60 | 2.14 | 4.80 |  |  |  |  |
| Kilpe and |  |  |  |  |  |  |  |  |
| Harjanne (29) $\ddagger$ | 9.34 | 1.05 | 2.05 | 4.95 |  |  |  |  |

TABLE III
Ionization constants $K_{1}$ and $K_{2}$

| Substituent | $\lambda, \mathrm{m} \mu$ | $\begin{gathered} \text { Concr. } \\ \times 10^{1} M \end{gathered}$ | $D_{2}$ |  | $K_{1} \times 10^{3}$ | $K_{2} \times 10^{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | From $K_{1}$ | From $K_{2}$ |  |  |
| $5-\mathrm{OMe}$ | 307 (min.) | 3.54 | $0.158 \pm 0.008$ | $0.177 \pm 0.008$ | $4.25 \pm 0.34$ | $0.300 \pm 0.032$ |
| $5-\mathrm{Me}$ | 290 (min.) | 4.06 | $0.201 \pm 0.013$ | $0.230 \pm 0.019$ | $4.35 \pm 0.34$ | $0.252 \pm 0.057$ |
| $5-\mathrm{F}$ | 288 (min.) | 9.02 | $0.200 \pm 0.020$ | $0.225 \pm 0.005$ | $9.32 \pm 0.49$ | $1.56 \pm 0.05$ |
| $5-\mathrm{Br}$ | 360 (max.) | 6.12 | $1.184 \pm 0.034$ | $1.038 \pm 0.018$ | $19.9 \pm 2.7$ | $3.89 \pm 0.31$ |
|  |  | 5.14 |  |  | $27.3 \pm 1.7$ |  |
| $5-\mathrm{Cl}$ | 355 (max.) | 3.84 | $0.861 \pm 0.014$ | $0.852 \pm 0.009$ | $20.6 \pm 4.1$ | $4.50 \pm 0.28$ |
| $5-\mathrm{OH}$ | 308 (max.) | 8.54 | $0.442 \pm 0.004$ | $0.454 \pm 0.004$ | $1.91 \pm 0.11$ | $0.432 \pm 0.023$ |
| None | 345 (max.) | 6.68 | $0.935 \pm 0.016$ | $0.944 \pm 0.018$ | $6.97 \pm 1.20$ | $1.46 \pm 0.14$ |
|  |  | 6.59 | $0.912 \pm 0.008$ | $0.919 \pm 0.010$ | $6.72 \pm 0.37$ | $1.40 \pm 0.10$ |
| $4-\mathrm{OMe}$ | 340 (max.) | 3.42 | $0.572 \pm 0.011$ | $0.571 \pm 0.007$ | $8.74 \pm 0.94$ | $1.33 \pm 0.07$ |
| 4-Me | 347 (max.) | 7.42 | $0.951 \pm 0.033$ | $0.945 \pm 0.014$ | $4.51 \pm 1.01$ | $0.845 \pm 0.057$ |
| 4-F | 325 (max.) | 5.42 | $1.053 \pm 0.020$ | $0.993 \pm 0.010$ | $38.4 \pm 5.3$ | $2.50 \pm 0.14$ |
| ${ }_{4}^{4-\mathrm{Br}}$ | 340 (max.) | 2.64 | $1.033 \pm 0.008$ | $1.027 \pm 0.013$ | $57.5 \pm 4.3$ | $4.30 \pm 0.25$ |
| $4-\mathrm{Cl}$ | 340 (max.) | 2.94 | $1.015 \pm 0.016$ | $0.963 \pm 0.057$ | $59.5 \pm 9.0$ | $3.29 \pm 0.80$ |
|  |  | 2.94 | $0.995 \pm 0.015$ | $0.994 \pm 0.007$ | $66.1 \pm 13.6$ | $3.64 \pm 0.16$ |
| $4-\mathrm{NO}_{2}$ | 408 (max.) | 3.92 | $0.921 \pm 0.009$ | $0.931 \pm 0.007$ | 222. $\pm 43$. | $20.6 \pm 2.6$ |
|  |  | 3.86 |  |  |  | $18.8 \pm 3.1$ |
| $5-\mathrm{OPh}$ | 302 (min.) | 5.06 | $0.345 \pm 0.010$ | $0.339 \pm 0.018$ | $4.55 \pm 0.31$ | $1.65 \pm 0.17$ |
| $5-\mathrm{NO}_{2}$ | 345 (max.) | 0.63 |  |  |  | $12.3 \pm 0.1$ |

This equation was solved for the constant terms $\rho_{1}, \rho_{2}$, and $\log K_{1}{ }^{0} K_{2}{ }^{0}$ by application of Dolittle's least squares procedure $(12,13)$ to the experimental data for 13 of the 14 acids for which both $K_{1}$ and $K_{2}$ had been determined. Data for the 5 -phenoxy acid were rejected for reasons given below. The $\sigma$-values which were used are listed in Table IV and are those given by McDaniel and Brown (30) with the exception of the $\sigma_{\mathrm{B}}$ values for the 5 -fluoro and 5 -nitro acids. The values reported by Biggs and Robinson (7) are used for these two $\sigma_{\mathrm{B}}$ 's which define the effect of a $p$-fluoro and of a $p$-nitro substituent, respectively, on the amino group. Statistical weights were calculated from an assumed standard deviation (30) of 0.020 for all the $\sigma$ 's, and from standard deviations of $\log K_{1} K_{2}$ values which were calculated from the standard deviations given in Table III for each of the individual ionization constants.

TABLE IV
Comparison of experinental and calculated values of $\log K_{1} K_{2}$

| Substituent | $\sigma_{A}$ | $\sigma_{B}$ | $\log K_{1} K_{2}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Experimental | Calculated |
| 5-OMe | 0.115 | -0. 268 | $7.91 \pm 0.05$ | 7.79 |
| $5-\mathrm{Me}$ | -0.069 | $-0.170$ | $7.61 \pm 0.04$ | 7.62 |
| $5-\mathrm{F}$ | 0.337 | -0.026 | $6.84 \pm 0.03$ | 6.87 |
| $5-\mathrm{Br}$ | 0.391 | 0.232 | $6.01 \pm 0.09$ | 6.02 |
| $5-\mathrm{Cl}$ | 0.373 | 0.227 | $6.03 \pm 0.09$ | 6.05 |
| $5-\mathrm{OH}$ | 0.121 | -0.370 | $8.08 \pm 0.03$ | 8.10 |
| None | 0.000 | 0.000 | $7.02 \pm 0.03$ | 7.04 |
| $4-\mathrm{OMe}$ | -0.268 | 0.115 | $6.93 \pm 0.05$ | 6.88 |
| 4-Me | $-0.170$ | $-0.069$ | $7.42 \pm 0.10$ | 7.38 |
| 4-F | 0.062 | 0.337 | $6.02 \pm 0.07$ | 5.94 |
| $4-\mathrm{Br}$ | 0.232 | 0.391 | $5.61 \pm 0.04$ | 5.65 |
| $4-\mathrm{Cl}$ | 0.227 | 0.373 | $5.65 \pm 0.06$ | 5.71 |
| $4-\mathrm{NO}_{2}$ | 0.778 | 0.710 | $4.35 \pm 0.10$ | 4.25 |
| $5-\mathrm{OPh}$ | 0.252 | $-0.320$ | $7.12 \pm 0.05$ | (7.85) |

Solution of eq. [15] gave $\rho_{1}=0.751, \rho_{2}=3.111$, and $\log K_{1}{ }^{0} K_{2}{ }^{0}=-7.039$. These calculated constants were inserted into eq. [15] to obtain calculated values ( $\tilde{y}$ ) of $\log K_{1} K_{2}$ which are listed, together with the corresponding experimental values ( $y$ ), in Table IV.

When data for all 14 acids were fitted to eq. [15] the difference, $y-\tilde{y}$, between the experimental and the calculated values for the 5 -phenoxy acid was several times larger than the corresponding value for any other acid and also its own standard deviation. The $K_{1}$ and $K_{2}$ constants for this acid were, therefore, not used in subsequent calculations. This large discrepancy between observed and calculated values of $\log K_{1} K_{2}$ for 5 -phenoxyanthranilic acid is shown in Table IV where the Hammett parameters defined by the other 13 acids have been used to calculate $\log K_{1} K_{2}$ for the 5 -phenoxy acid.

The data for the same 13 acids were also fitted to the four other equations following.

$$
\begin{gather*}
\log K_{1}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}}+\log K_{1}^{0}  \tag{22}\\
\log K_{2}=\rho_{1} \sigma_{\mathrm{A}}+\rho_{2} \sigma_{\mathrm{B}}+\log K_{2}^{0}  \tag{23}\\
\log K_{1} K_{2}=\rho_{1} \sigma_{\mathrm{A}}+\log K_{1}^{0} K_{2}^{0}  \tag{29}\\
\log K_{1} K_{2}=\rho_{1} \sigma_{\mathrm{B}}+\log K_{1}^{0} K_{2}^{0} \tag{30}
\end{gather*}
$$

Table $V$ gives the calculated parameters for these equations. Equations [22] and [23] are valid only if the existing equilibria can be represented by eq. [21] rather than the generally accepted eq. [1.]. Equations [29] and [30] have no obvious physical significance; they are included only for purposes of comparison in estimating the significance of the fit of the data to eq. [15].

TABLE V
Comparison of Hammett equations

| Eq. | $\rho_{1}$ |  | $\rho_{2}$ | $s^{2}$ (ext.)* | $s^{2}$ (int.) $\dagger$ | $R \ddagger$ | $F \S$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $[15]$ | $0.751 \pm .084$ | $3.111 \pm .071$ | 0.0039 | 0.0057 | 0.997 | 1.560 | 73 |
| $[22]$ | $0.491 \pm .146$ | $1.727 \pm .114$ | 0.0091 | 0.0024 | 0.981 | 255 |  |
| $[23]$ | $0.426 \pm .144$ | $1.254 \pm .130$ | 0.0113 | 0.0009 | 0.949 | 93 |  |
| $[29]$ | $2.086 \pm .121$ |  | 0.640 | 0.0057 | 0.481 |  |  |
| $[30]$ | $3.331 \pm .019$ |  | 0.0419 | 0.0057 | 0.983 |  |  |

$*_{s^{2}}$ (ext.) $=\Sigma(y-y)^{2} /(n-3)$, where the numerator is the sum of the squares of the deviations from the estimated regression equation and the denominator is the degrees of freedom.
$\dagger s^{2}($ int. $)=\Sigma$ (observed standard error of $\left.y\right)^{2} /(n-3)$
$\ddagger R=$ multiple correlation coefficient.
$\S F$ is the variance ratio comparing the equation in question with a completely random distribution and tests the lypothesis $\rho_{1}=0$. $\rho_{2}=0$.
gives a significantly better fit to the data.
The statistics of Table $V$, which describe the significance of the fit of the data to each equation, amply demonstrate the superiority of eq. [15] as an accurate interpretation of the experimental results. Only for this equation is $s^{2}$ (int.), calculated from the known experimental uncertainties, greater than $s^{2}$ (ext.) which is calculated from the fit of the data to the theoretical equation. The data give a considerably less significant fit to eqs. [22] and [23], indicating that the zwitterion and neutral acid cannot be treated as a single species.

The multiple correlation coefficient and the $F$-test show eq. [15] to be significant within the $99 \%$ confidence limit. Jaffe (5) has pointed out that equations of the same mathematical form as eq. [15] may give an excellent but entirely fallacious fit of the data if $\sigma_{A}$ and $\sigma_{B}$ are highly correlated. He has proposed that equations of this type should only be considered to give a meaningful interpretation of the data if $r_{A B}<0.9$, where $r_{A B}$ is

TABLE VI
Comparison of experimental and calculated values of $\mathrm{p} K_{1}$ and $\mathrm{p} K_{2}$

| Substit－ uent | $\mathrm{p} K_{1}$ |  |  | $\mathrm{p} K_{2}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Expt． | $\begin{aligned} & \text { From } \\ & \text { eq. }[11 a] \end{aligned}$ | $\begin{aligned} & \text { From } \\ & \text { eq. }[19 a] \end{aligned}$ | Expt． | $\begin{aligned} & \text { From } \\ & \text { eq. }[11 b] \end{aligned}$ | $\begin{aligned} & \text { From } \\ & \text { eq. }[19 b] \end{aligned}$ |
| $5-\mathrm{OMe}$ | $2.37 \pm .03$ | 2.38 | 2.54 | $5.57 \pm .06$ | 5.45 | 5.38 |
| $5-\mathrm{Me}$ | $2.48 \pm .03$ | 2.43 | 2.54 | $5.13 \pm .01$ | 5.20 | 5.16 |
| 5－F | $2.03 \pm .02$ | 2.03 | 2.17 | $4.82 \pm .01$ | 4.86 | 4.76 |
| $5-\mathrm{Br}$ | 1．60土．03 | 1.66 | 1.61 | $4.41 \pm .03$ | 4.34 | 4.39 |
| $5-\mathrm{Cl}$ | $1.69 \pm .08$ | 1.68 | 1.63 | $4.35 \pm .03$ | 4.36 | 4.40 |
| $5-\mathrm{OH}$ | $2.72 \pm .02$ | 2.42 | 2.58 | $5.37 \pm .02$ | 5.72 | 5.67 |
| None | $2.17 \pm .03$ | 2.18 | 2.23 | $4.85 \pm .05$ | 4.85 | 4.83 |
| 4－OMe | $2.06 \pm .05$ | 1.98 | 1.99 | $4.88 \pm .02$ | 4.85 | 4.86 |
| 4－Me | 2．35土． 10 | 2.35 | 2.42 | $5.07 \pm .03$ | 5.02 | 5.00 |
| 4－F | $1.42 \pm .07$ | 1.45 | 1.34 | $4.60 \pm .02$ | 4.44 | 4.55 |
| $4-\mathrm{Br}$ | $1.24 \pm .03$ | 1.33 | 1.17 | $4.37 \pm .03$ | 4.27 | 4.42 |
| $4-\mathrm{Cl}$ | $1.21 \pm .07$ | 1.37 | 1.22 | $4.44 \pm .03$ | 4.29 | 4.43 |
| $4-\mathrm{NO}_{2}$ | 0．65土．08 | 0.56 | 0.19 | $3.70 \pm .06$ | 3.63 | 3.99 |
| $5-\mathrm{OPh}$ | $2.34 \pm .08$ | （2．28） | （2．48） | $4.88 \pm .04$ | （5．58） | （5．53） |
| $s^{2}$（ext．） |  | 0.125 | 0.282 |  | 0.196 | 0.207 |

the correlation coefficient between $\sigma_{\mathrm{A}}$ and $\sigma_{\mathrm{B}}$ ．The value of $r_{\mathrm{AB}}=0.590$ for our sub－ stituents amply fulfills this condition and，indeed，is lower than in any of the cases discussed by Jaffe．

It was pointed out earlier that in the specific case，where indirect effects are negligible， $\rho_{1}={ }_{\mathrm{D}} \rho_{\mathrm{A}}$ and $\rho_{2}={ }_{\mathrm{D}} \rho_{\mathrm{B}}$ ．Furthermore，${ }_{\mathrm{D}} \rho_{\mathrm{A}}$ and ${ }_{\mathrm{D}} \rho_{\mathrm{B}}$ should，in theory，be approximately equal to 1.00 and 2.89 ，respectively．These theoretical values are outside the standard deviations of $\rho_{1}(=0.751 \pm 0.084)$ and $\rho_{2}(=3.111 \pm 0.071)$ shown in Table V．This might be considered evidence for the existence of an indirect effect，although the differences between theoretical and experimental values are no greater than some reported by Jaffe （6）for ortho－substituted systems where chelation is impossible．However，it may be worthwhile to explore the possibility of indirect effects as an explanation for the dis－ crepancy．In that case eq．［16］would give

$$
\begin{aligned}
& \rho_{1}={ }_{\mathrm{D}} \rho_{\mathrm{A}}+{ }_{\mathrm{I}} \rho_{\mathrm{D}}=0.751, \\
& \rho_{2}={ }_{\mathrm{I}} \rho_{\mathrm{A}}+{ }_{\mathrm{D}} \rho_{\mathrm{D}}=3.111 .
\end{aligned}
$$

If ${ }_{D} \rho_{A}$ and ${ }_{D} \rho_{\mathrm{D}}$ were given their theoretical values of 1.000 and 2.889 ，respectively，the indirect effects would become ${ }_{\mathrm{I}} \rho_{\mathrm{D}}=-0.249$ and ${ }_{\mathrm{I}} \rho_{\mathrm{A}}=+0.222$ ．Since the former of these represents the indirect effect of substituents via chelation upon the ionization of a $\mathrm{NH}_{3}{ }^{+}$ group，it would be expected to be positive．It seems unlikely，therefore，that the deviation from the theoretical values is really the result of an indirect effect．This conclusion is reinforced by the fact that no indirect effect is observed in the similar but simpler system of salicylic acids $(5,31)$ ．

A further test of the indirect effect would be to compare the fit of the experimental $K_{1}$＇s and $K_{2}$＇s to eqs．［11a］and［11b］which include the indirect effect，with the fit of the same data，to［19a］and［19b］which do not．This was attempted using $\mathrm{D}_{\mathrm{A}}=1.000$ ， ${ }_{\mathrm{I}} \rho_{\mathrm{A}}=0.222,{ }_{\mathrm{D}} \rho_{\mathrm{D}}=2.889$ ，and ${ }_{\mathrm{I}} \rho_{\mathrm{D}}=-0.249$ for eqs．［11］，or $\rho_{\mathrm{A}}=0.751$ and $\rho_{\mathrm{B}}=3.111$ for eqs．［19］，and weighting the $K$＇s inversely as the squares of their standard deviations． Table VI compares the observed $\mathrm{p} K_{1}$＇s and $\mathrm{p} K_{2}$＇s with those calculated by the two methods．It is seen that，while the $\mathrm{p} K_{1}$＇s fit eq．［11］somewhat better than eq．［19］，there is little to choose between［11］and［19］as methods for calculating $\mathrm{p} K_{2}$ ．Since for both
series $s^{2}$ (ext.) is at least double $s^{2}$ (int.), the better fit to eq. [11] can hardly be taken as evidence for an indirect effect.

TABLE VII
Calculated ionization constants for eq. [1]

| Eq. | $K_{\text {A }}{ }^{0} \times 10^{3}$ | $K_{\text {B }}{ }^{0} \times 10^{3}$ | $\left(K_{\mathrm{A}}{ }^{0}+K_{\mathrm{B}}{ }^{0}\right) \times 10^{3}$ | Experimental $K_{1}{ }^{0} \times 10^{3}$ | $\mathrm{K}_{\mathrm{z}}{ }^{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| [11a] | $3.2 \pm .3$ | $3.4 \pm .6$ | $6.6 \pm .8$ | $6.7 \pm .4$ | $1.0 \pm .3$ |
| [19a] | $1.9 \pm .2$ | $3.9 \pm .6$ | $5.9 \pm .8$ | $6.7 \pm .4$ | $0.5 \pm .1$ |
| Eq. | $K c^{0} \times 10^{5}$ | $K_{0}{ }^{0} \times 10^{5}$ | $\left(1 / K_{C}{ }^{0}+1 / K_{\mathrm{D}}{ }^{0}\right) \times 10^{-5}$ | Experimental $1 / K_{2}{ }^{0} \times 10^{-5}$ | $K z^{0}$ |
| [11b] | $3.2 \pm .4$ | $2.5 \pm .2$ | $0.71 \pm .04$ | $0.70 \pm .04$ | 1. $2 \pm .3$ |
| [19b] | $2.7 \pm .1$ | $3.2 \pm .3$ | $0.68 \pm .04$ | $0.70 \pm .04$ | $0.9 \pm .1$ |

In fitting the $K_{1}$ 's and $K_{2}$ 's to eqs. [11] and [19] the data for 5 -phenoxyanthranilic acid were omitted, as indicated previously, because of their poor fit to eq. [15]. The values of $K_{\mathrm{A}}{ }^{0}, K_{\mathrm{B}}{ }^{0}, K_{\mathrm{C}}{ }^{0}$, and $K_{\mathrm{D}}{ }^{0}$ obtained from the remaining 13 acids were used to calculate $\mathrm{p} K_{1}$ and $\mathrm{p} K_{2}$ for the 5 -phenoxy acid and these are shown in parentheses in Table VI. It is seen that the calculated $\mathrm{p} K_{1}$ agrees reasonably well with experiment but that $\mathrm{p} K_{2}$ is widely out. Examination of eq. [19b] shows that the calculated value of $K_{2}$ for this acid is largely determined by the second term of the equation, which depends upon $\sigma$ for the para-phenoxy group. It appears, therefore, that either the experimental value of $K_{2}$ is grossly in error or $\sigma_{\text {para }}$ is incorrect. In order to fit the experimental $K_{2}$ into eqs. [15] and [19b] a value of $\sigma=-0.088$ would be required for the $p$-phenoxy group, and it is interesting to note that this is in good agreement with the $\sigma_{p}$ reported by Jaffe (6) for reactions other than ionization constants of benzoic acids. However, our data ought, in principle, to correlate with the ionization constants of benzoic acids, and the 5 -phenoxy acid is particularly susceptible to oxidative side reactions, so that it is probably not safe to attach any particular significance to our apparent $\sigma$-value.

Table VII shows the values for $K_{\mathrm{A}}{ }^{0}, K_{\mathrm{B}}{ }^{0}, K_{\mathrm{C}}{ }^{0}$, and $K_{\mathrm{D}}{ }^{0}$ obtained from eqs. [11] and [19] and for the values of $K_{z^{0}}$ derived from these by means of eq. [7]. The extended series of computations from the original data causes an accumulation of uncertainties in the quantities presented in Table VII but it is seen that they are consistent within their standard deviations. For example, eq. [4], which requires that $K_{\mathrm{A}}{ }^{0}+K_{\mathrm{B}}{ }^{0}=K_{1}{ }^{0}$, and eq. [5], which requires that $1 / K_{C^{0}}{ }^{0}+1 / K_{D}{ }^{0}=1 / K_{2}{ }^{0}$, are both satisfied. The uncertainty in $K_{z}{ }^{0}$ is correspondingly large, but $K_{z}{ }^{0}$ evidently lies in the region $0.4-1.5$, with the theoretically preferable eq. [19a] giving a range of $0.4-1.0$, equivalent to $30-50 \%$ zwitterion.
Previous calculations giving $K_{\mathrm{z}}{ }^{0}=0.2$, or $17 \%$ zwitterion, have been based on the assumption that $K_{\mathrm{A}}{ }^{0}$ may be equated to the ionization constant of the methyl ester of anthranilic acid, $\mathrm{p} K_{\mathrm{E}}=2.09$ (3). This assumption, as applied to $p$-aminobenzoic acid, has been criticized by Bryson and Matthews (11) on the grounds that the various alkyl esters have different ionization constants and that among these the methyl ester is out of line. The assumption may be particularly questionable when applied to anthranilic acid esters because of the known acid-strengthening effect of bulky ortho substituents in anilinium ions (32). The reported ionization constant of the ester, $K_{\mathrm{E}}=8.13 \times 10^{-3}$, is indeed larger than our $K_{\mathrm{A}}{ }^{0}$, whether one considers its most probable value of $1.9 \times 10^{-3}$ or the maximum value of $3.5 \times 10^{-3}$ obtained by inclusion of indirect substituent effects
via eq. [11a]. In fact, Table II shows that the ionization constant of the ester is larger than most modern estimates of $K_{1}{ }^{0}$, which, since $K_{1}{ }^{0}=K_{A}{ }^{0}+K_{B}{ }^{0}$, makes the assumption that $K_{\mathrm{E}}=K_{\mathrm{A}}{ }^{0}$ untenable.

Finally, it may be pointed out that, although the equilibrium constant for zwitterion formation by anthranilic acid is still not known with great precision, the relative equilibrium constants for zwitterion formation by substituted anthranilic acids may be calculated from eq. [20] with considerable certainty. If $K_{z}{ }^{0}$ is assumed to be 1.0 , then among our acids $K_{z}$ varies from 17.5 ( $95 \%$ zwitterion) for 5 -hydroxy to 0.019 ( $2 \%$ zwitterion) for 4-nitroanthranilic acid.

## SUMMARY

The ionization constants of substituted anthranilic acids give an excellent fit to the two-parameter Hammett eq. [15], showing that these acids at the isoelectric point are better represented as a mixture of zwitterion and neutral acid than as a single hybrid species; previous estimates of the $\%$ zwitterion are low because of the erroneous assumption that the ionization of the amino group is the same in anthranilic acid as in its methyl ester; and indirect transmission of substituent effects via chelation is very improbable since in some cases it would have to act in the sense opposite to that predicted by theory.

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[^0]:    *In this and subsequent equations $p_{\mathrm{A}}$ and $\rho_{\mathrm{B}}$ are the Hammett constants for a given substituent considered in relation to the - COOH (or - $\mathrm{COO}^{-}$) and the $-\mathrm{NH}_{3}{ }^{+}$(or- $\mathrm{NH}_{2}$ ) groups, respectively. Reaction constants are defined by a suffix ( $A, B, C$, or $D$ ) referring to the constants $K_{A}, K_{B}, K_{C}$, and $K_{D}$ of eq. [1], and a prefix ( $I$ or $D$ ) indicating whether a direct or indirect effect is involved. In other cases where it is necessary to distinguish between two or more $\rho$ or a values, numerical suffixes are used.

[^1]:    *Throughout this paper, for any set of experimentally derived data, $y, x_{1}, x_{2}, \ldots \ldots$, , vhich are ased to determine the constant parameters $a_{1}, a_{2}, \ldots$ of an equation $y=f\left(x_{1}, x_{2} \ldots a_{1}, a_{2} \ldots \ldots\right)$, the "external estimate of error" is defined as $s^{2}($ ext. $)=\sum(y-\bar{y})^{2} /($ degrees of freedom $)$, where $\tilde{y}$ is the value of $y$ calculated by inserting the computed values of $a_{1}, a_{2}, \ldots \ldots$ into the equation.

