

Characterization of the electronic properties of YB₄ and YB₆ using ¹¹B NMR and first-principles calculations

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Abstract

Two compounds, tetragonal YB₄ and cubic YB₆, have been investigated by electric-field gradient (EFG) and Knight shift measurements at the boron sites using the ¹¹B nuclear magnetic resonance (NMR) technique and by performing first-principles calculations. In YB₆ ¹¹B ($I = 3/2$) NMR spectra reveal patterns typical for an axially symmetric field gradient with a quadrupole coupling frequency of $\nu_Q = 600 \pm 15$ kHz. In the second boride (YB₄) three different EFGs were observed corresponding to the three inequivalent crystallographic sites for the boron atoms (4*h*, 4*e*, and 8*j*). They correspond to: $\nu_Q(4h) = 700 \pm 30$ kHz with an asymmetry parameter $\eta = 0.02 \pm 0.02$, $\nu_Q(4e) = 515 \pm 30$ kHz, $\eta = 0.00 \pm 0.02 / -0.00$, and $\nu_Q(8j) = 515 \pm 40$ kHz, $\eta = 0.46 \pm 0.08$. The Knight shifts measured by magic-angle spinning (MAS) NMR at room temperature are very small being 0.6 ± 8 and -1 ± 8 ppm for YB₄ and YB₆, respectively. For the theoretical calculations structure optimizations were performed as a first step. For the obtained structural parameters the EFGs were computed within the local-density approximation. Very satisfactory agreement between experimental and theoretical results is obtained both for the structural parameters and the B EFGs, thus confirming the underlying structural models. In addition to the EFGs, band structures, densities of states, and valence-electron densities are presented and the bonding situation in the two yttrium borides is discussed. The band-structure results are compatible with the very low values for the Knight shifts mentioned above.

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1. Introduction

Through their specific properties, transition metal borides became attractive both from scientific and technical point of view. For instance, YB₆, like some other rare-earth and actinide hexaborides, shows superconductivity below 7.1 K [1] and has been considered as a possible candidate for high-temperature thermoelectric materials [2].

Detailed knowledge of the electronic structure of a material is a key ingredient for an in-depth understanding of many of its macroscopic features. A combination of experimental methods as well as computations on an ab-initio level has proved very efficient, in particular, relating electronic structure calculations to results of nuclear magnetic resonance (NMR) technique. The value of the electric-field

gradient (EFG), measured by NMR quadrupole interaction, is directly determined by the charge distribution around the nucleus. Thus, theoretical EFG studies based on the electronic structure are important in order to give a reliable interpretation of the experimental data. One of the strengths of NMR measurements is that, being a microscopic tool, they are sensitive to the symmetry of the crystallographic sites and in particular to the electron density in the vicinity of the nucleus. In a recent study, this sensitivity was used to provide criteria for the determination of crystal structures that are still under debate [3–5].

In the present paper, we report the EFG values for YB₆ and YB₄ and the determination of the Knight shifts by using the magic-angle spinning (MAS) technique. The experimental EFGs are compared and interpreted with the theoretical ones obtained from ab-initio calculations.

The structure of cubic YB₆ (space group $Pm\bar{3}m$, no. 221) consists of a simple cubic lattice of corner-connected B₆ octahedra with Y atoms filling the cubic holes. In this

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and other borides with the same structure the B–B distance between neighbouring octahedra is slightly shorter than within the octahedron (for YB₆: 1.64 Å compared to 1.75 Å). In agreement with this crystallographic structure there is only a single EFG value. A previous ¹¹B NMR study for YB₆ [6] reported the spin-lattice relaxation time and the spectrum. However, the authors were unable to determine the EFG because of the widely broadened satellite lines and the weak NMR signal used in their instrumentation.

On the other hand, tetragonal YB₄ (space group *P4/mbm*, no. 127) has a quasilayer structure with alternating sheets of Y atoms and B₆ octahedra linked together laterally by B₂ units. In this structure, five different nearest-neighbor B–B distances between 1.64 and 1.81 Å are observed. In YB₄ the boron atoms are situated in three different crystallographic positions with different EFGs for each of them, as will be demonstrated in the present paper.

2. Structure optimization

For confirmation of the validity of the available experimental lattice parameters and the atomic positions, calculations have been performed using the Vienna ab-initio simulation package (VASP) [7–9]. By this method, the Kohn–Sham equations of density-functional theory [10,11] with periodic boundary conditions are solved within a plane-wave basis set with electron–ion interactions described by the projector augmented wave (PAW) method [12,13]. For exchange and correlation the generalized gradient approximation (GGA) [14] was applied. The structural parameters were calculated by atomic forces and stress-tensor minimization. For each of the two borides two different energy cutoffs for the plane-wave basis were used (400 eV and a cutoff higher by at least a factor of 2), which lead to practically the same results, so that adequate convergence is ensured. The experimental and calculated structural parameters for YB₄ and YB₆ are given in Tables 1 and 2, respectively. For cubic YB₆, where the lattice parameter *a* and the positional parameter of the B atom are the only free parameters, the minimum-energy structure was also found by the full-potential linearized augmented plane-wave (FLAPW) method within the LDA approximation which is described in the next section.

The structural parameters optimized by VASP have been used to calculate the EFGs for YB₆ and YB₄.

3. Electric-field gradients

3.1. Experimental

To avoid skin-depth effects for better RF penetration, the samples were used in powder form and obtained by crushing the single crystals. The crystals were obtained by crucible free inductive zone melting of the YB₄ and the YB₆ source

Table 1

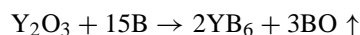
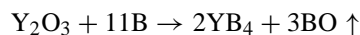
Experimental and calculated structural parameters for YB₄ adopting the ThB₄ structure (*P4/mbm*, no. 127)

Lattice parameters	Positional parameters	Atom	Site	Remarks
<i>a</i> = 7.111	<i>x</i> = 0.3179	Y	4 <i>g</i>	Experimental, Ref. [15]
<i>c</i> = 4.017	<i>z</i> = 0.2027	B(1)	4 <i>e</i>	
	<i>x</i> = 0.0871	B(2)	4 <i>h</i>	
	<i>x</i> = 0.1757	B(3)	8 <i>j</i>	
	<i>y</i> = 0.0389			
<i>a</i> = 7.1035				Experimental, Ref. [16]
<i>c</i> = 4.0206				
<i>a</i> = 7.1091	<i>x</i> = 0.3182	Y	4 <i>g</i>	Calculated, VASP (GGA)
<i>c</i> = 4.0280	<i>z</i> = 0.2030	B(1)	4 <i>e</i>	
	<i>x</i> = 0.0870	B(2)	4 <i>h</i>	
	<i>x</i> = 0.1760	B(3)	8 <i>j</i>	
	<i>y</i> = 0.0386			

The lattice parameters are in Å.

rods that provides a high purity and single-phase material. They, in turn, were prepared in the following steps:

- (1) Mixing of Y₂O₃ (purity 99.999%) and boron components in proper ratios.
- (2) Synthesis of the YB₄ and the YB₆ powders by routine solid-state reaction of borothermic reduction:



- (3) Slip casting of source rods, removal of the binder and sintering of the rods in the vacuum.

The ¹¹B NMR experiments were carried out with a Bruker DSX Avance spectrometer at a frequency of 96.29 MHz. The static spectra were obtained by the Fourier transform of the free induction decay (FID) following a short single pulse (in the range of 0.9–2.5 μs). The spectra contain up to 256 accumulations with a repetition time of 20 s. A 4 mm MAS probe was used with rotation frequencies between 7 and 9 kHz. The chemical shifts are given with respect to external BF₃Et₂O. In Fig. 1 the ¹¹B NMR spectra for YB₄ and YB₆ are given.

Table 2

Experimental and calculated structural parameters for YB₆ adopting the CaB₆ structure (*Pm3̄m*, no. 221)

Lattice parameter	Positional parameter	Remarks
<i>a</i>	<i>x</i>	
4.102		Experimental, Ref. [17]
4.1025	0.202	Experimental, Ref. [18]
4.113		Experimental, Ref. [19]
	0.199	Experimental, Ref. [20]
4.0436	0.1989	Calculated, FLAPW (LDA)
4.1004	0.1988	Calculated, VASP (GGA)

The lattice parameters are in Å, the positional parameter refers to site 6f of B.

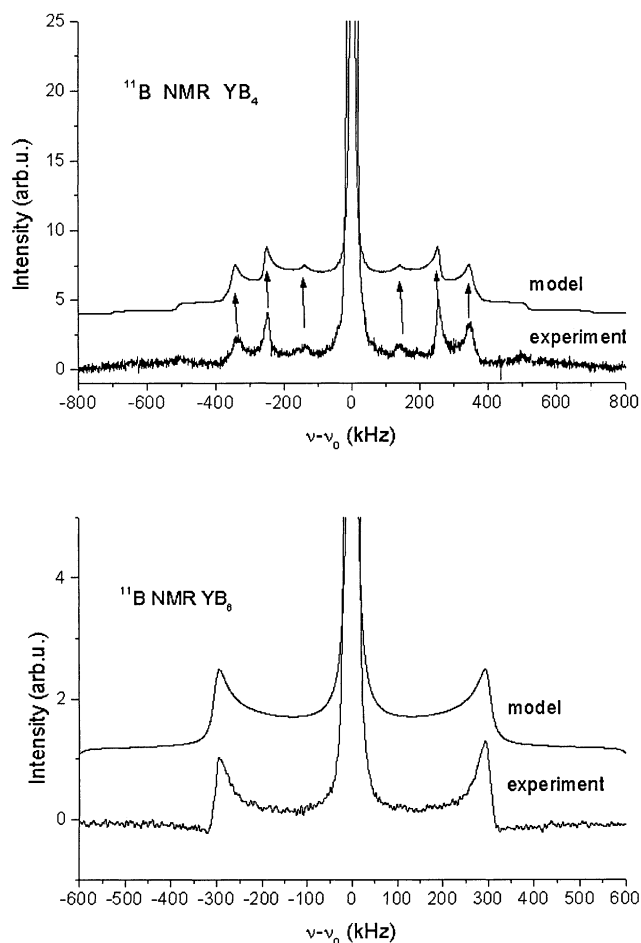


Fig. 1. Experimental and theoretical (model) powder-pattern ^{11}B spectrum for YB_4 (top) and YB_6 (bottom). For better readability the model spectra are shifted up with respect to the experimental ones. For YB_4 the arrows indicate positions of 90° singularities ($\eta \sim 0$) for B(2) (outermost arrows) and B(1) (middle arrows) except for the singularity for B(3) (innermost arrows) where the angle is different from 90° ($\eta = 0.46$).

3.2. First-principles calculations

The all-electron band-structure calculations for the calculation of EFGs are based on the density-functional theory (DFT) [10,11] and the local-density approximation and have been performed by the linearized augmented plane-wave (LAPW) method [21] in its full-potential version [22–25] using an exchange-correlation potential by Hedin and Lundqvist [26,27].

The EFGs have been calculated from the $l = 2$ components of the Coulomb potential near the nuclei. The formalism by Herzig [28] and Blaha et al. [29] has also been employed to split the calculated EFG components into the contributions from the surrounding electrons within the respective muffin-tin sphere (“sphere contribution”) and the remainder that comes from outside this sphere (“lattice contribution”). This partitioning depends, to a small extent, on the choice of the muffin-tin radii. The valence contribution can be split further into the allowed ll' con-

tributions (only sd, pp, pf are important in the present context) which provide useful information about the influence of particular l -like wave functions on the EFGs [30]. As is common practice the EFG component with the largest absolute value is always designated as V_{zz} . For further algorithmic details on the EFG calculation see our recent paper [4].

3.3. EFGs: results and discussion

Fig. 1 shows the ^{11}B spectra which are typical for a nuclear spin $I = 3/2$ in the presence of first-order quadrupole effects. For YB_6 (bottom of Fig. 1) the separation of the satellite lines is given by $\delta\nu = \nu_Q(3\cos^2\Theta - 1)$, where Θ are the powder singularities. Thus, $\Theta = 90^\circ$, yields $\nu_Q = e^2qQ/2h$. Here, $eq = V_{zz}$ and Q is the largest component of the electric-field gradient tensor and the nuclear quadrupole moment, respectively. The axially symmetric field gradient is consistent with the local symmetry at the boron site. The existence of three inequivalent boron sites in YB_4 is the origin of the more complex satellite spectrum compared to YB_6 (Fig. 1). The ν_Q value and the asymmetry parameter $\eta = (V_{xx} - V_{yy})/V_{zz}$ were obtained using the *dmfit* simulation program [31]. The ν_Q value translates into $C_q = 2\nu_Q$ and it follows for $V_{zz} = 4.136 \times 10^{19} C_q/Q$ (in V/m^2) when the appropriate Q value (in barn) for ^{11}B is used and C_q is inserted in units of MHz. Since different nuclear quadrupole moments can be found in the literature, the experimental values for V_{zz} were determined for two different values, namely $Q = 0.04$ and 0.0355 b [32]. The former Q value has been taken from the almanac of the spectrometer manufacturer Bruker and is very close to $Q = 0.04059$ [33] recommended by Pyykkö [34] in his compilation of nuclear quadrupole moments. The results are shown in Tables 3 and 4 for YB_6 and YB_4 , respectively. Experimentally, only the absolute value of V_{zz} and η can be determined for the powder specimens.

For YB_6 the B EFG corresponds to the axially symmetric case (site symmetry C_{4v}) where there is only one independent EFG component. In YB_4 the situation is more complicated. The three crystallographically distinct B sites (site symmetries: C_4 for B(1), C_{2v} for B(2), and C_s for B(3)) lead to one, two, and three independent EFG components, respectively. This means that for B(2) and B(3) a non-zero asymmetry parameter η is observed.

The comparison between calculated and measured EFGs shows very good agreement, if the absolute values are con-

Table 3
Calculated B EFGs (in 10^{20} V/m^2) for YB_6 for the optimized structure compared to the experimental results assuming an ^{11}B nuclear quadrupole moment of 0.04 and 0.0355 $|e| \times 10^{-28} \text{ m}^2$, respectively

Calculated optimized structure V_{zz}	Experimental $Q = 0.04$ $ V_{zz} $	Experimental $Q = 0.0355$ $ V_{zz} $
−13.5	12.4 ± 0.3	14.0 ± 0.3

Table 4

Calculated B EFGs (in 10^{20} V/m²) for YB₄ for the experimental structure [15] and the optimized structure compared to the experimental results assuming an ¹¹B nuclear quadrupole moment of 0.04 and 0.0355 |e| × 10^{−28} m², respectively

Site	<i>i</i>	Calculated experimental structure		Calculated optimized structure		Experimental <i>Q</i> = 0.04		Experimental <i>Q</i> = 0.0355	
		<i>V_{ii}</i>	<i>η</i>	<i>V_{ii}</i>	<i>η</i>	<i>V_{ii}</i>	<i>η</i>	<i>V_{ii}</i>	<i>η</i>
B(1)	<i>z</i>	−11.0	0.0	−10.8	0.0	10.6 ± 0.6	0.0	12.0 ± 0.6	0.0
B(2)	<i>x</i>	−8.1		−8.2					
	<i>y</i>	−8.3		−8.4					
	<i>z</i>	16.4	0.02	16.6	0.01	14.5 ± 0.6	0.02	16.3 ± 0.6	0.02
B(3)	<i>x</i>	2.7		2.9					
	<i>y</i>	7.9		7.9					
	<i>z</i>	−10.6	0.48	−10.8	0.47	10.6 ± 0.9	0.46 ± 0.09	12.0 ± 0.9	0.46 ± 0.08

Table 5

Split of the B EFG for YB₆ (optimized structure) into lattice and sphere components and the latter into its main contributions, i.e. sd, pp, and pf

Site	<i>V_{zz}</i>	<i>V_{zz}</i> ^{lat}	<i>V_{zz}</i> ^{sph}	<i>V_{zz}</i> ^{sd}	<i>V_{zz}</i> ^{pp}	<i>V_{zz}</i> ^{pf}
B	−13.5	9.0	−22.5	−1.9	−17.8	−2.3

All *V_{zz}* values are in units of 10²⁰ V/m².

sidered. In general for the EFG tensor either one or two components are negative. The corresponding principal axes are determined by the strongest bonding interactions. In the case of YB₄ the negative EFG component for B(1) (*V_{zz}*) is related to the axis of the inter-octahedral B–B bond along the *c*-axis, for B(2) the two negative components (*V_{xx}* and *V_{yy}*) refer to the (001) plane through B(2) and its three B neighbours, and finally for B(3) the negative EFG component (*V_{zz}*) refers to the axis of the bond between the adjacent atoms of a B₆ octahedron and a B₂ unit.

Now the splits of the B EFGs into the lattice and sphere contributions and the latter into their main components (sd, pp, and pf) are considered (Tables 5 and 6). The sphere contribution is the one with the largest absolute value, but also the lattice contribution is relatively large. This behaviour has been observed previously for borides and other second-group elements by Schwarz et al. [35]. For the H atom in hydrides the lattice contribution is even larger than the sphere contribution, as has been found recently [4]. It is not surprising that the pp component dominates the sphere contribution with the sd and pf components being the largest other components.

Table 6

Split of the B EFGs for YB₄ (optimized structure) into lattice and sphere components and the latter into its main contributions, i.e. sd, pp, and pf

Site	<i>V_{zz}</i>	<i>V_{zz}</i> ^{lat}	<i>V_{zz}</i> ^{sph}	<i>V_{zz}</i> ^{sd}	<i>V_{zz}</i> ^{pp}	<i>V_{zz}</i> ^{pf}
B(1)	−10.8	7.2	−18.0	−1.4	−14.6	−1.7
B(2)	16.6	−4.0	20.6	1.3	17.8	1.3
B(3)	−10.8	5.0	−15.7	−1.3	−12.6	−1.6

All *V_{zz}* values are in units of 10²⁰ V/m².

3.4. Knight shifts

The Knight shifts, *K*, measured for both compounds, are found to be very small, i.e. 0.6 and −1 ppm for YB₆ and YB₄, respectively. The accuracy of the *K* values were estimated to be ±8 ppm, where the uncertainty results from an incomplete reduction of the strong dipolar interaction in the MAS experiment, mainly between the boron nuclei. These values of *K* are much smaller than those observed in MgB₂, where *K*(¹¹B) = 100 ppm [36] and in YNi₂B₂C, where *K*(¹¹B) ≈ 400 ppm [37] (both values are for room temperature). This comparison indicates that the values for the densities of states (DOS) at the Fermi level for the boron sites are much lower than those in the borides mentioned above. Especially the lack of s-type DOS, which is usually the contribution with the largest hyperfine field, reduces significantly the shifts. Indeed, the s-type DOS per boron atom is, in YB₆ [38], over 20 times smaller than in MgB₂ [38]. Also the p-type DOS per B atom is significantly smaller in YB₆ compared to MgB₂. These data are compatible with the present electronic band structure calculations (see next section) which show that s- and p-type boron states are located mainly below the Fermi energy and thus, the contribution to the DOS at *E_F* is small.

4. Electronic structure and chemical bonding

The first theoretical investigation of metal borides of general formula MB₆ has been performed 50 years ago by Longuet-Higgins and Roberts [39] using the tight-binding approximation. According to these authors the octahedral arrangement of the B atoms leads to 10 bonding states which, when filled with the 18 B s and p plus two metal valence electrons, will correspond to an insulator. A metal will be obtained when the hexaboride of a trivalent metal is considered instead of a divalent metal. In their paper, the states below the Fermi level are not only characterized in terms of their bonding or antibonding properties but also as regards their participation in bonds within a single B₆ octahedron or between neighbouring octahedra. Later [40] the higher lying valence and conduction bands of YB₆ have been calculated

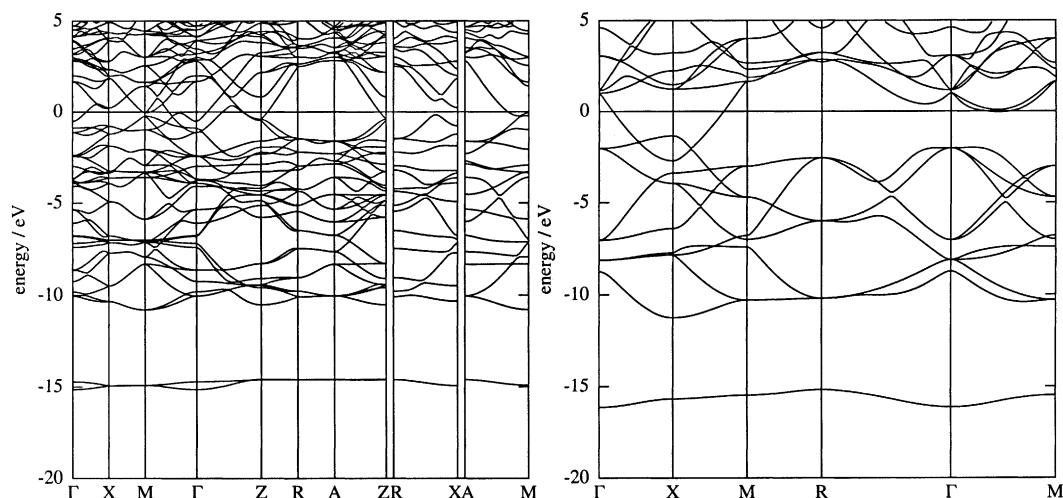


Fig. 2. Electronic band structure for YB_4 (left) and YB_6 (right).

by a discrete variational method in a non-selfconsistent fashion. Recent electronic-structure calculations for YB_6 can be found in Ref. [2] (DOS only) and in Ref. [38] where also the band structure is given. For YB_4 only the DOS has been published so far [2,38]. In both references, however, the lowest B 2s band is not shown although it is of crucial importance for the chemical bonding in both borides as will be argued below. In the case of YB_6 Shein et al. [38] designate it erroneously as “quasi-core B 2s band”—obviously mainly because it is a low-lying band. In Fig. 2 the band structures for YB_4 and YB_6 are presented.

The DOS curves for YB_4 and YB_6 are given in Fig. 3 together with the local partial DOS components. For both borides the states at energies of approximately -15 eV are dominated by B 2s character with a considerable amount of B 2p character. Such states appear for all B atoms constituting the B_6 octahedra, but not for B(2), which belongs to the B_2 unit of which each B atom is linked to two different octahedra. In this energy range hybrid orbitals are formed which lead to strong covalent σ bonds between the boron atoms within a B_6 unit which can be seen from the corresponding electron densities shown in Fig. 4.

After an energy gap of about 3.7 eV a complex of bands appears in both compounds where in the lower energy range B s states prevail with an admixture of B p states except for the B(2) atoms. These states correspond mainly to bonds between different B_6 octahedra and s–s σ bonds in the B_2 units of YB_4 . At higher energies below the Fermi level B p states are predominant apart from a relatively small B s and a considerable Y d contribution. Also in this energy range the inter-octahedral bonds are dominant except for the region very near the Fermi level in YB_6 where the intraoctahedral B–B bonds again become important.

In YB_6 the Y d states have mostly e_g character which can be seen from the valence electron densities in Fig. 5. This Figure also shows that this is not the case for YB_4 although near the Fermi level e_g -like character, i.e. $(d_{z^2}, d_{x^2-y^2})$ character, is predominant.

Our results for YB_6 are in very good agreement with the detailed semiempirical tight-binding investigation by Longuet-Higgins and Roberts [39]. In order to make the comparison we performed crystal-field splittings for the B p (and Y d) states. We thus obtained the distinction between

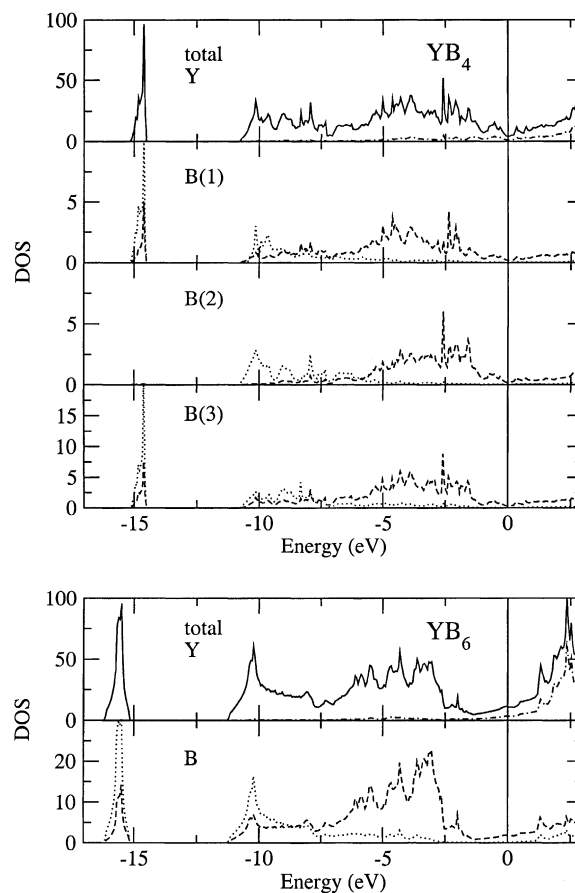


Fig. 3. Total DOS (full line) and local partial DOS components (B s: dotted line; B p: dashed line; Y d: dash-dotted line) for YB_4 (top) and YB_6 (bottom) in units of states per Rydberg and per formula unit.

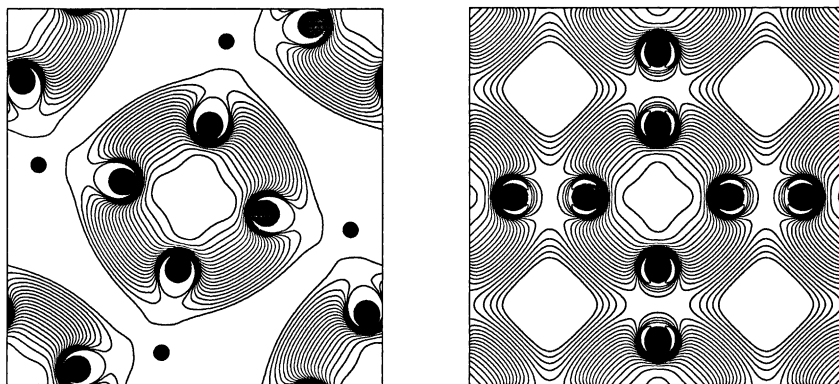


Fig. 4. Electron densities in the (001) plane through the B atoms for the lowest valence bands at approximately -15 eV. Left: YB_4 , right: YB_6 . A logarithmic grid of contour lines has been used ($x_i = x_0 2^{i/3}$). For YB_4 the B(2) atoms appear as black bullets without a surrounding electron density.

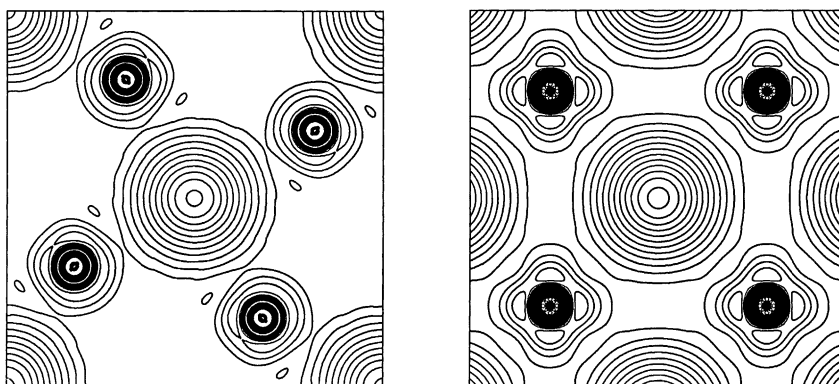


Fig. 5. Valence electron densities in the (001) plane through the Y atoms. Left: YB_4 , right: YB_6 . A logarithmic grid of contour lines has been used ($x_i = x_0 2^{i/3}$).

their radial (p_z) and tangential orbitals (p_x, p_y). Together with electron-density plots for certain energy ranges, the regions for the different site orbitals for the B_6 octahedron could be identified. We obtained the following order (increasing energy): a_{1g} (band at approximately -15 eV), a'_{1g} , t_{1u} , e'_g , and t_{2g} (the nomenclature is taken from Ref. [39] and refers to the irreducible representations for the whole octahedron).

In Fig. 6 the valence electron densities in the (001) plane through the B atoms in YB_4 and YB_6 are displayed. Apart from the structural differences between both borides (irregular heptagonal arrangement of the B atoms outside the octahedra in YB_4 compared to an almost regular octagon in YB_6) the slightly higher valence electron densities between the B atoms outside the octahedra in both compounds can be seen as well as the deep density minima which designate

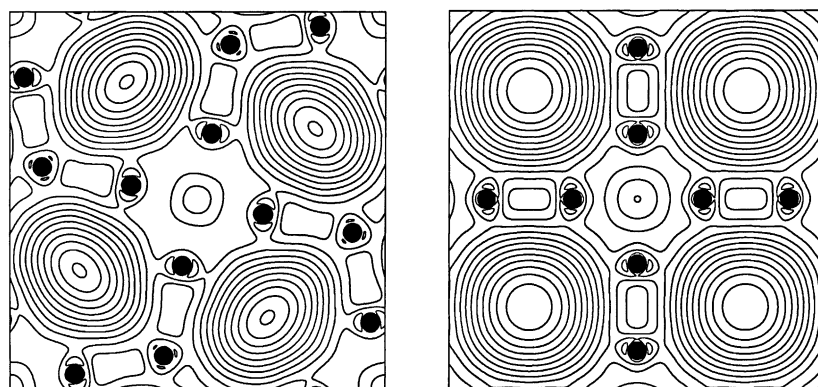


Fig. 6. Valence electron densities in the (001) plane through the B atoms. Left: YB_4 , right: YB_6 . A logarithmic grid of contour lines has been used ($x_i = x_0 2^{i/3}$).

the much weaker covalent Y–Y bonds perpendicular to the (001) plane.

5. Summary

For YB₄ and YB₆ we have performed electric-field gradient and Knight shift measurements for the B sites. The aim of the paper has been a comparison of the NMR results and the available structural data with the results of accurate first-principles calculations. We have, therefore, optimized the structures by atomic forces and stress–tensor minimization. For the optimized structures EFG calculations have been performed. Perfect agreement was found between the experimental and calculated structural parameters and electric-field gradients, thus confirming the structure models available in the literature. Based on calculated total and local partial DOS as well as electron-density plots, we analyse the bonding situation in both compounds and conclude that the lowest valence bands are of particular importance for the stability of both yttrium borides.

Acknowledgements

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