# Equilibrium Vapor Composition in the Pb–I<sub>2</sub> System

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**Abstract**—The equilibrium vapor composition in the Pb–I<sub>2</sub> system at temperatures from 400 to 2000 K and total pressures from  $10^2$  to  $10^5$  Pa was assessed by thermodynamic analysis. The results show that the dominant vapor species is PbI<sub>2</sub>. PbI<sub>2</sub> dissociation is significant starting at 1000–1300 K, depending on the total pressure in the system.

# INTRODUCTION

 $PbI_2$  crystals are potentially attractive as materials for optical information recording systems, nonlinear optical devices, and x-ray and gamma detectors [1, 2]. The known techniques for melt growth of large  $PbI_2$ crystals are incapable of ensuring the desired structural perfection of the crystals, which reflects on the engineering performance of  $PbI_2$ -based devices. Large, stoichiometric  $PbI_2$  single crystals with a low dislocation density can be grown from the vapor phase in the presence of excess iodine [3]. This process, however, has not yet been studied in sufficient detail.

In this context, it is of interest to analyze the equilibrium vapor composition in a closed system. Information about the temperature-dependent compositions of the vapor and condensed phases helps to clarify the mechanism of mass transport in the growth system and optimize the growth procedure. By varying the process parameters, one can control the quality of the growing crystal.

#### **EXPERIMENTAL**

The equilibrium pressures of vapor species can be determined either experimentally or by thermodynamic calculations.

We used Knudsen cell mass spectrometric measurements to study the sublimation and thermal dissociation of  $PbI_2$  in the temperature range 300–873 K. The mass spectra of saturated vapor over  $PbI_2$  crystals showed the presence of  $PbI_2$  molecules and minor amounts of iodine and lead.

# CALCULATIONAL APPROACH

Although crystal growth from the vapor phase is a nonequilibrium process, it can be analyzed, to a reasonable approximation, with the use of equilibrium thermodynamics since knowledge of the equilibrium characteristics of the reactions involved makes it possible to draw a number of conclusions about the key features of the process as a whole, such as the reaction path, deviations from equilibrium, and the influence of individual reactions on the overall process.

To assess the vapor composition over  $PbI_2$  in the temperature range 400–2000 K at total pressures of  $10^2$ ,  $10^3$ ,  $10^4$ , and  $10^5$  Pa, we carried out thermodynamic analysis of the Pb–I<sub>2</sub> system. The vapor species included in our analysis were I, I<sub>2</sub>, Pb, PbI, and PbI<sub>2</sub>. The corresponding vapor-phase equilibria are

$$I_2(g) \Longrightarrow 2I(g),$$
 (1)

$$PbI_2(g) \Longrightarrow PbI(g) + I(g),$$
 (2)

$$\operatorname{PbI}_2(g) \Longrightarrow \operatorname{Pb}(g) + \operatorname{I}_2(g).$$
 (3)

Depending on their melting and boiling points, the reactants may be in different states of aggregation, producing different vapor pressures. The equilibrium constants of independent reactions in the range 300–2000 K were calculated using the reported thermodynamic functions of the substances involved [4, 5] (table).

In terms of the partial pressures  $p_1 = p(I)$ ,  $p_2 = p(I_2)$ ,  $p_3 = p(Pb)$ ,  $p_4 = p(PbI)$ , and  $p_5 = p(PbI_2)$ , the equilibrium constants for reactions (1)–(3) have the form

$$K_1 = p_1^2 / p_2, (4)$$

$$K_2 = p_1 p_4 / p_5, (5)$$

$$K_3 = p_2 p_3 / p_5. (6)$$

In addition,

$$p_1 + 2p_2 + p_4 + 2p_5 = 2(p_3 + p_4 + p_5)$$
(7)

(the amount of iodine atoms per unit volume is twice as



**Fig. 1.** Calculated temperature-dependent partial pressures in the Pb–I<sub>2</sub> system at total pressures of (a)  $10^2$ , (b)  $10^3$ , (c)  $10^4$ , and (d)  $10^5$  Pa;  $p_1-p_5$  have the same meaning as in text.

large as that of lead atoms),

$$p = p_1 + p_2 + p_4 + p_4 + p_5 \tag{8}$$

(Dalton Law).

Equilibrium constants of independent reactions in the  $\mbox{Pb}{-}\mbox{I}_2$  system

<i>Т</i> , К	$K_1$	$K_2$	$K_3$
300	$4.2 \times 10^{-25}$	$4.10 \times 10^{-58}$	$1.20 \times 10^{-31}$
400	$1.45\times10^{-14}$	$4.10 \times 10^{-40}$	$7.50 \times 10^{-23}$
500	$2.8  imes 10^{-11}$	$2.20\times10^{-29}$	$7.20 \times 10^{-18}$
600	$1.2  imes 10^{-8}$	$2.86\times10^{-22}$	$8.20 \times 10^{-14}$
700	$1.02 \times 10^{-6}$	$4.00\times10^{-17}$	$6.50 \times 10^{-11}$
800	$2.70 \times 10^{-5}$	$1.40 \times 10^{-13}$	$5.00 \times 10^{-9}$
900	$3.60 \times 10^{-4}$	$7.00\times10^{-11}$	$1.70 \times 10^{-7}$
1000	$4.20 \times 10^{-3}$	$9.00 \times 10^{-9}$	$2.40\times10^{-6}$
1100	$1.50 \times 10^{-2}$	$4.60 \times 10^{-7}$	$1.90 \times 10^{-5}$
1200	$6.20 \times 10^{-2}$	$4.60 \times 10^{-6}$	$6.20 \times 10^{-5}$
1300	0.20	$3.06 \times 10^{-5}$	$1.15 \times 10^{-4}$
1400	0.57	$1.60  imes 10^{-4}$	$2.00 \times 10^{-4}$
1500	1.39	$6.50 \times 10^{-4}$	$3.30 \times 10^{-4}$
1600	3.05	$2.20 \times 10^{-3}$	$5.03 \times 10^{-6}$
1700	6.09	$6.70 \times 10^{-3}$	$7.40 \times 10^{-4}$
1800	11.30	$1.80 \times 10^{-2}$	$1.04 \times 10^{-3}$
1900	19.70	$4.20 \times 10^{-2}$	$1.42 \times 10^{-3}$
2000	32.40	$9.20 \times 10^{-2}$	$1.90 \times 10^{-3}$

The system of nonlinear algebraic equations (4)–(8) can be reduced to an equation of the fourth degree in  $p_1$ :

$$2p_1^4 + (K_1 + 3K_2)p_1^3 + (2K_1K_2 + 4K_1K_3)p_1^2 + (3K_3K_1^2 - pK_1K_2)p_1 - 2K_3K_1^2p = 0.$$
(9)

This equation was solved numerically. Next, using appropriate substitutions, we found  $p_2$ ,  $p_3$ ,  $p_4$ , and  $p_5$ . The calculated partial pressures of vapor species in the Pb–I<sub>2</sub> system at temperatures in the range 300–1700 K and different total pressures are displayed in Fig. 1.

# DISCUSSION

The above results lead us to the following conclusions:

1. At total pressures from  $10^2$  to  $10^5$  Pa and temperatures from 300 to 1000 K, the dominant vapor species is PbI<sub>2</sub>. Its pressure exceeds those of other vapor species by one to five orders of magnitude.

2. PbI<sub>2</sub> dissociation into I, I<sub>2</sub>, Pb, and PbI is significant starting at 1000–1300 K, depending on the total pressure. The main dissociation products are I and Pb. The PbI vapor pressure rises with increasing temperature and total pressure but, in the range 300–1300 K, remains three to five orders of magnitude lower than the PbI<sub>2</sub> pressure. Only above 1500 K is the pressure of PbI vapor comparable to that of PbI<sub>2</sub>, but the net iodide pressure (PbI + PbI<sub>2</sub>) remains three to four orders of magnitude lower than the pressure of the dissociation products (Pb, I, and  $I_2$ ).

3. To a first approximation, the vapor-phase equilibrium in the Pb– $I_2$  system between 300 and 1000 K can be described by scheme (3).

Our experimental and calculation results on the equilibrium vapor composition in the Pb-I2 system provide guidelines for choosing the conditions of PbI<sub>2</sub> growth from the vapor phase. Since the temperature of the growth zone should not exceed 685 K (melting point of PbI<sub>2</sub>), and a temperature gradient of 100–400 K is typically sufficient for vapor transport growth, the highest temperature of the source zone is 1000-1100 K. At temperatures from 700 to 1100 K and total pressures from  $10^3$  to  $10^5$  Pa, the dominant vapor species in the  $Pb-I_2$  system is  $PbI_2$ . The proportion of the dissociation products under these conditions does not exceed 1%. As PbI<sub>2</sub> slightly dissociates in the temperature range in question, which may lead to deposition of nonstoichiometric material, the process should be run at an iodine overpressure no lower than the dissociation pressure  $(10^3 \text{ Pa})$ . The mechanism of mass transport in the growth system depends on the relationship between the total pressure and the difference in the vapor pressures in the source and growth zones.

Note that, in the growth procedure described in [3], the iodine overpressure is substantially higher than the pressure of  $PbI_2$  dissociation at the temperatures of

interest. At the same time, the growth duration is too long for practical applications. In this context, there is a need for theoretical analysis and experimental studies of the effects that the growth conditions and iodine overpressure have on the rate of  $PbI_2$  transport and the morphology of the resulting crystals. Such information is crucial for optimizing the conditions of  $PbI_2$  crystal growth. These issues will be addressed in subsequent communications.

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