

High-Resolution Fourier Transform Infrared Spectrum of the ν_5 Fundamental Band System of Cyanogen, NCCN

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The far-infrared spectrum of the lowest-lying rovibrational band system ν_5 of cyanogen, NCCN, was measured in the wavenumber range from 180 to 280 cm^{-1} . A Fourier transform spectrometer was used with a nominal resolution of 0.0018 cm^{-1} . Transitions within the ν_5 manifold up to $\nu_5 = 4$ were assigned and precise molecular constants for the corresponding states were determined.

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INTRODUCTION

Cyanogen,¹ NCCN, was first synthesized by Gay-Lussac in 1815 by thermolysis of AgCN (1). The problem of the determination of the chemical formula and structure of cyanogen accompanied chemistry from its early days (2, 3). Even now, with investigations by means of high-resolution gas-phase spectroscopy and ab initio calculations at a high level, cyanogen still presents questions about details of its structure and dynamics.

Cyanogen belongs to the point group $D_{\infty h}$ and exhibits five fundamental normal modes, two of which are degenerate. The fundamental rovibrational band systems ν_1 at 2330.5 cm^{-1} , ν_2 at 845.5 cm^{-1} , and ν_4 at 502.8 cm^{-1} are infrared-inactive due to the centrosymmetry of the molecule. The *ungerade* modes ν_3 at 2157.8 cm^{-1} and ν_5 at 233.9 cm^{-1} are infrared-active fundamental band systems.

The most recent work on rovibrational spectroscopy of NCCN was carried out by Wang and Weber on the Raman-active band systems (4). The infrared spectrum of the ν_3 band system was recorded by Picard (5) and the ν_5 band system was observed by Jolma (6). The latter study was made with a resolution of 0.02 cm^{-1} . Due to the lack of a permanent electric dipole moment, pure rotational spectra are observable only as Raman spectra, most recently reported in 1987 (7).

In the early 1980's cyanogen won new interest upon its detection in the atmosphere of the Saturn moon Titan by Voyager 1 (8, 9) and due to the identification of new isomers (10, 11). This resulted in new theoretical investigations of cyanogen and its isotopomers concerning the structure, energy levels, and the intensities of vibrational transitions (12, 13).

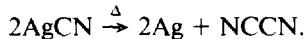
We decided to measure the ν_5 band system, which was first observed by Rubens and von Wartenberg in 1911 (14), with high resolution (0.0018 cm^{-1}) and to characterize the lowest rovibrational energy levels, important for the analysis of all other band systems of cyanogen. Furthermore, we carried out precise intensity measurements, which will be treated in the following paper (15).

¹ IUPAC name since 1970: Ethanenitrile.

EXPERIMENTAL DETAILS

Synthesis

Cyanogen was prepared in two different ways (2, 3). The first method was vapor thermolysis of silver cyanide, AgCN:



Solid AgCN was held under vacuum in a quartz tube with a cross section of $\approx 1 \text{ cm}^2$ at a temperature of 300°C to dry the probe completely. The quartz tube was heated on a length of $\approx 20 \text{ cm}$. After $\approx 1 \text{ hr}$ the temperature was raised to 600°C and the product of the pyrolysis was condensed at liquid nitrogen temperature. The product was used without further purification. The yield is quantitative.

The second preparation uses the oxidation of potassium cyanide, KCN, with copper(II) sulfate, CuSO₄:



An aqueous solution of KCN was dropped onto solid CuSO₄ · 5 H₂O in a dry N₂ atmosphere. The gaseous products were passed through an ice/NaCl-cooled trap, through a tube filled with CaCl₂, and finally condensed in a trap held at -80°C . This crude product was additionally passed through a tube filled with solid NaOH to eliminate the by-product HCN. The overall yield is 38%.

No impurities were observed. Pure cyanogen is stable in a glass cell.

Far-Infrared (FIR) Measurements

The FIR spectra were recorded with the Bruker IFS 120 HR Fourier transform vacuum Michelson interferometer (16, 17).

The glass cell was 10 cm in diameter and 284 cm in length. Wedged polyethylene windows of about 2-mm thickness were used. Cyanogen was sublimed into the cell at room temperature until a sample pressure of 0.25 mbar was reached. The measurement parameters were as follows: source, mercury lamp; aperture, 4 mm; beam splitter, 6 μ mylar; scanner speed, 2.532 cm/sec; optical filters, 0–375 cm⁻¹; detector, Si bolometer, 4.2 K, resolution [1/(maximum optical path difference)], 0.0018 cm⁻¹.

The cyanogen spectrum was recorded in eight blocks each of 25 scans. Since during the measurements the conditions of the spectrometer and sample were stable, all blocks could be coadded.

The spectrum file was divided by a background recorded at lower resolution and post transform zero-filled to match the resolution of the sample spectrum. The resulting transmittance spectrum was further zero-filled to an overall zero-filling factor of 16. The signal-to-noise (S/N) ratio varies between 80 and 100. The peak positions were determined using the available Bruker software.

Calibration was achieved with internal, pure rotational water lines, due to residual water in the spectrometer (not in the sample!). Since the line density of cyanogen increases very rapidly above 215 cm⁻¹ only water lines below 210 cm⁻¹ are used for calibration purposes. In Table I the water lines used for calibration are listed together with the standard deviation of the calibration fit. If a linear calibration curve can be assumed, the accuracy of the line positions is $\pm 7 \times 10^{-5} \text{ cm}^{-1}$ at 180 cm⁻¹ and $\pm 10 \times 10^{-5} \text{ cm}^{-1}$ at 250 cm⁻¹.

TABLE I
Pure Rotational Water Lines Used for Internal Calibration

Measured position/cm ⁻¹	Reference position/cm ⁻¹	Calculated position/cm ⁻¹	Deviation 10 ⁵ (calc-ref)/cm ⁻¹
173.281 172	173.282 07	173.282 0128	-5.724 5
173.354 784	173.355 56	173.355 6251	6.511 1
178.485 051	178.485 89	178.485 9170	2.700 5
179.047 923	179.048 74	179.048 7917	5.173 4
184.564 179	184.565 05	184.565 0745	2.4500
184.770 620	184.771 51	184.771 5165	0.650 3
193.478 370	193.479 32	193.479 3087	-1.124 7
194.321 321	194.322 24	194.322 2638	2.384 1
195.804 561	195.805 63	195.805 5110	-11.895 6
197.085 534	197.086 40	197.086 4903	9.025 3
197.263 671	197.264 72	197.264 6281	-9.188 0
Standard error of measurement: 6.55 × 10 ⁻⁵ cm ⁻¹			

THEORETICAL CONSIDERATIONS

For clarity the notation is briefly explained. We refer to a "state" as a group of energy levels designated by a set of vibrational quantum numbers, in the case of a four atomic linear molecule written as $(v_1 v_2 v_3 v_4 v_5)$, whereby leading quantum numbers may be omitted if they are zero. Here we need only $(v_4 v_5)$. The v_5 band system in absorption includes only transitions with $\Delta v_5 = +1$, e.g., transitions of the vibrational bands

$$(v_1 v_2 v_3 v_4 (v_5 + 1)) \leftarrow (v_1 v_2 v_3 v_4 v_5).$$

If a state involves one or more excited bending modes it splits into two or more substates characterized by the vibrational angular momenta quantum numbers l_i , e.g., $(v_1 v_2 v_3 v_4^l v_5^{l_5})^k$ with $k = l_4 + l_5$. The transitions between substates constitute subbands, e.g., for the perpendicular bands studied here

$$(v_1 v_2 v_3 v_4^l (v_5 + 1)^{l_5})^{k \pm 1} \leftarrow (v_1 v_2 v_3 v_4^{l'} v_5^{l_5})^k.$$

The rotational energy levels of a linear molecule within a vibrational state or substate can be expressed in a power series (ps) in $J(J+1)$:

$$E(J) = G_c + B_{ps}J(J+1) + D_{ps}J^2(J+1)^2 + H_{ps}J^3(J+1)^3. \quad (1)$$

G_c is defined by band centers and thus differs from the spectroscopic term value G_v defined below, which defines band origins. The expression in Eq. (1) cannot describe a complete k -polyade of an excited bending state simultaneously. Therefore the power series coefficients provide only a nearly "model-free" representation of the energy levels of a state with an excited bending mode. They provide a check of the quality of the data and a basis for the vibrational assignments, but are not directly related to a molecular Hamiltonian.

For the full analysis of the transitions we used the effective Hamiltonian for a linear molecule defined by Yamada *et al.* (18). For states within the v_5 manifold (bending mode v_t , $v_t = n$ and $l_t = k$) the diagonal elements in k are

$$E_{k,k} = G_v + x_k k^2 + y_k k^4 + \{B_v + d_{jk} k^2\} f_0(k) - \{D_v + h_{jk} k^2\} f_0(k)^2, \quad (2)$$

and the only off-diagonal elements needed to reproduce the date are given by

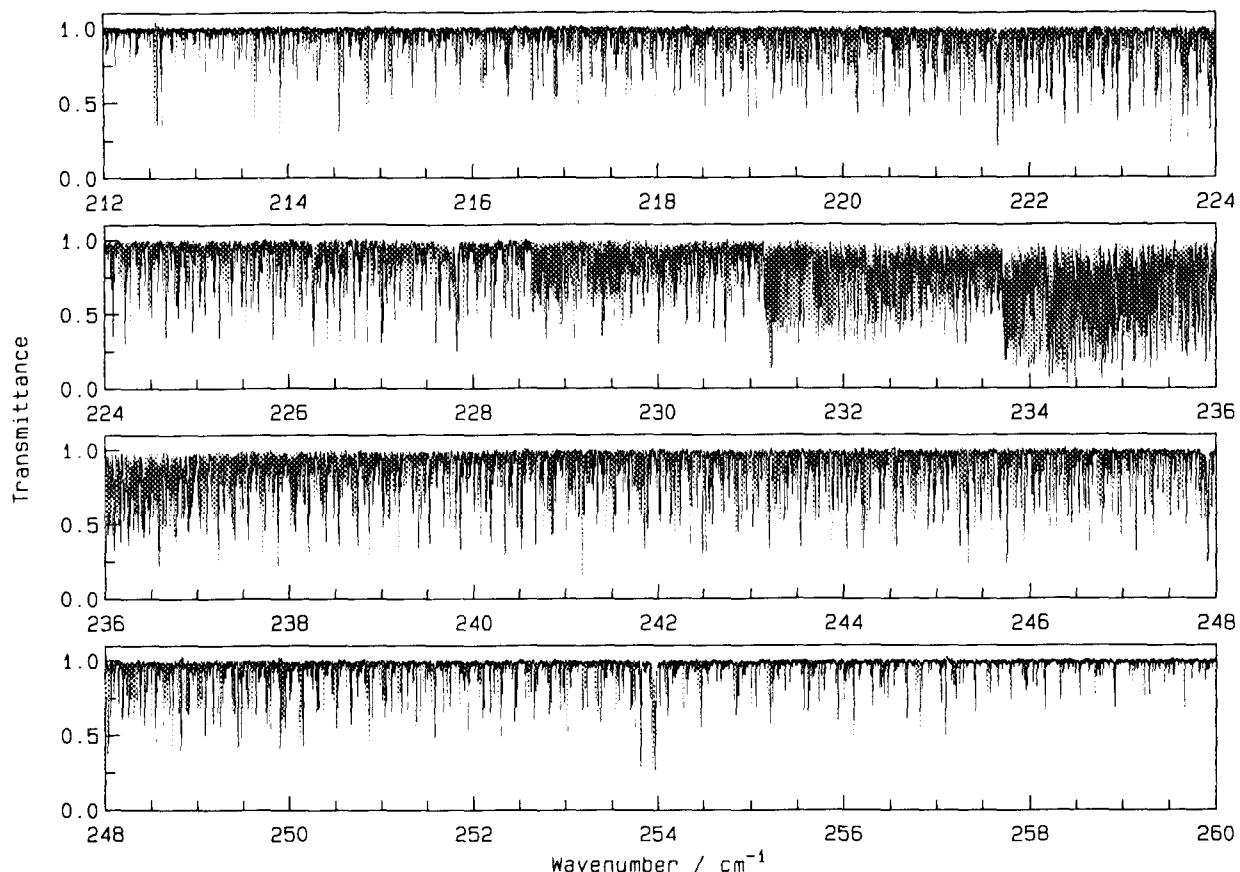


FIG. 1. Overview spectrum of NCCN recorded at 0.25 mbar in a cell 284 cm long at 0.0018 cm^{-1} resolution.

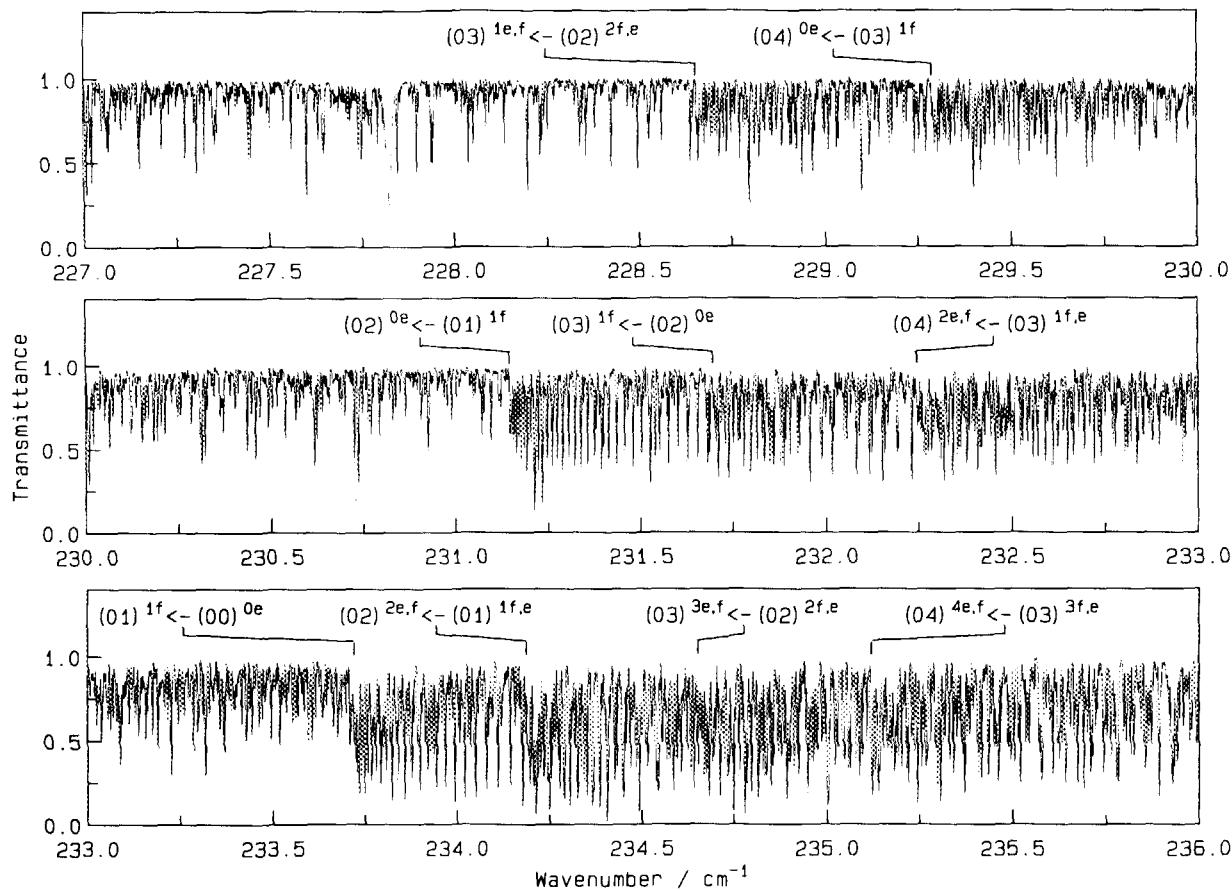


FIG. 2. Q -branch region of the ν_5 band system of NCCN.

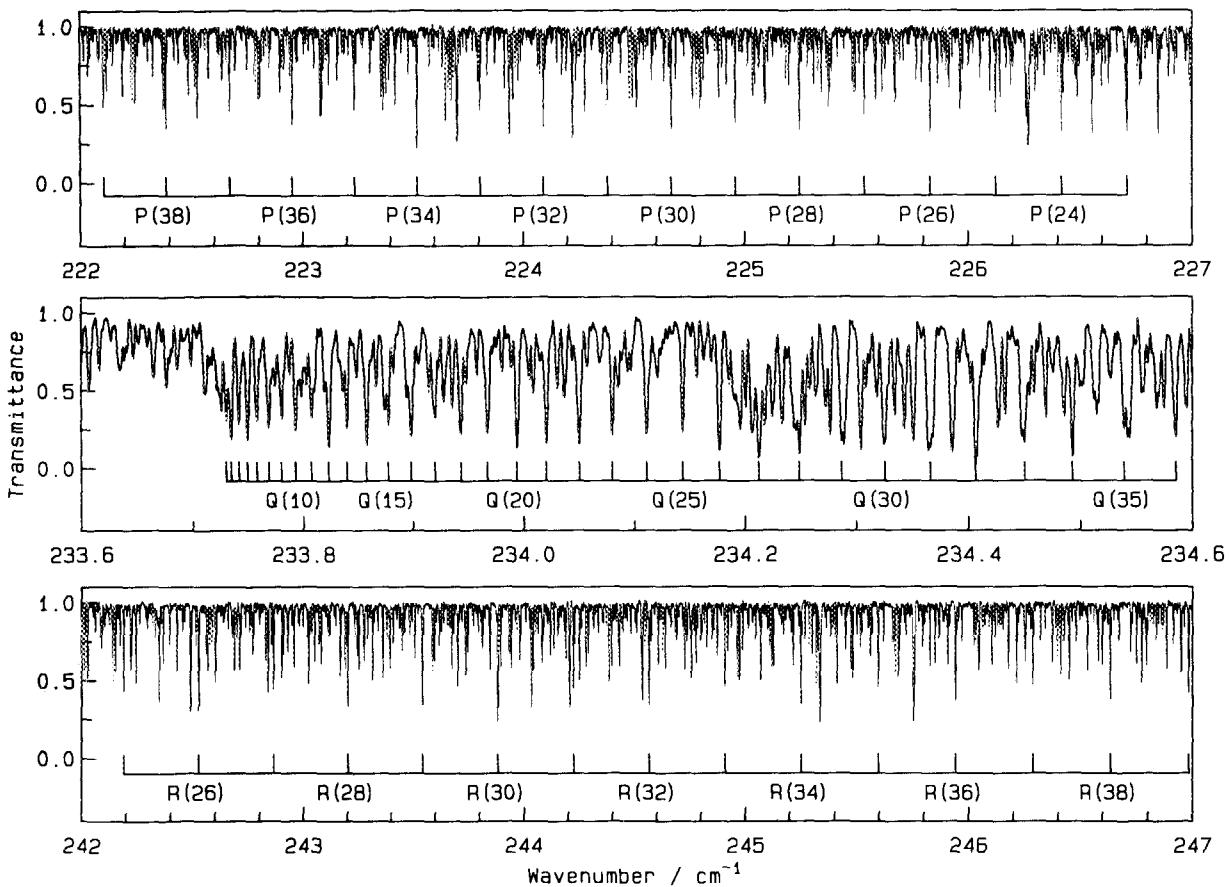


FIG. 3. Excerpts of *P*-, *Q*-, and *R*-branch regions of the ν_5 band system of NCCN. The lines of the fundamental band are indicated with assignment combs.

TABLE II

Band Centers $\nu_c = (G'_c - G''_c)$ Derived from Fits to the Power Series in Eq. (1) of the Subbands in the v_i Band System of NCCN. σ is the Standard Deviation of the Fit (the Numbers in Parentheses Give One Standard Deviation in Units of the Last Digits Given)

Subband	$\bar{\nu}_c/\text{cm}^{-1}$	$10^4 \sigma/\text{cm}^{-1}$
(01) ^{1e} \leftarrow (00) ^{0e}	233.721 478 (16)	1.01
(01) ^{1f} \leftarrow (00) ^{0e}	233.721 36 (10)	3.56
(02) ^{2e} \leftarrow (01) ^{1e}	234.187 781 (41)	1.76
(02) ^{2f} \leftarrow (01) ^{1f}	234.187 537 (26)	1.31
(02) ^{0e} \leftarrow (00) ^{1e}	231.144 702 (36)	1.69
(02) ^{0e} \leftarrow (01) ^{1f}	231.145 93 (23)	9.58
(03) ^{3e} \leftarrow (02) ^{2e}	234.653 37 (18)	8.01
(03) ^{3f} \leftarrow (02) ^{2f}	234.653 572 (53)	2.50
(03) ^{1e} \leftarrow (02) ^{0e}	231.696 458 (47)	2.16
(03) ^{1f} \leftarrow (02) ^{0e}	231.696 07 (13)	3.69
(03) ^{1e} \leftarrow (02) ^{2e}	228.653 543 (72)	1.76
(03) ^{1f} \leftarrow (02) ^{2f}	228.640 37 (14)	1.70
(04) ^{4e} \leftarrow (03) ^{3e}	235.119 681 (68)	2.28
(04) ^{4f} \leftarrow (03) ^{3f}	235.119 484 (44)	1.38
(04) ^{2e} \leftarrow (03) ^{1e}	232.242 26 (25)	4.83
(04) ^{2f} \leftarrow (03) ^{1f}	232.243 42 (15)	4.01
(04) ^{0e} \leftarrow (03) ^{1e}	229.287 51 (13)	3.75
(04) ^{0e} \leftarrow (03) ^{1f}	229.287 94 (38)	6.12

$$U_{k,k+2}^S = U_{k-2,k}^S = \frac{1}{4} \{ q_i + q_{IJ} J(J+1) \} \sqrt{(n-k+1)(n+k+1)} f_2(k). \quad (3)$$

The superscript S indicates that this matrix element is defined for the excitation of only one bending mode. The $f_i(k)$ are given by

$$f_0(k) = J(J+1) - k^2 \text{ and}$$

$$f_2(k) = \sqrt{[J(J+1) - k(k+1)][J(J+1) - (k+1)(k+2)]}. \quad (4)$$

With Eqs. (2) and (3) all substates in k of a bending state v_i can be described with one set of parameters.

TABLE III

Power Series (ps) Rotational Constants Obtained from the FIR Spectrum of NCCN (the Numbers in Parentheses Give One Standard Deviation in Units of the Last Digits Given)

Level	from Subband	$B_{\text{ps}}/\text{cm}^{-1}$	$10^8 D_{\text{ps}}/\text{cm}^{-1}$	$10^{13} H_{\text{ps}}/\text{cm}^{-1}$
(00) ^{0e}	(01) ^{1e} \leftarrow (00) ^{0e}	0.157 088 07 (19)	2.116 3 (18)	
(01) ^{1e}	(01) ^{1e} \leftarrow (00) ^{0e}	0.157 515 66 (19)	2.180 3 (18)	
(01) ^{1f}	(01) ^{1f} \leftarrow (00) ^{0e}	0.157 738 56 (25)	2.243 2 (54)	
(02) ^{2e}	(02) ^{2e} \leftarrow (01) ^{1e}	0.158 160 54 (58)	5.30 (13)	-6.365 (59)
(02) ^{2f}	(02) ^{2f} \leftarrow (01) ^{1f}	0.158 161 64 (30)	2.302 9 (37)	
(02) ^{0e}	(02) ^{0e} \leftarrow (01) ^{1e}	0.158 164 85 (39)	4.074 1 (54)	6.442 (20)
(03) ^{3e}	(03) ^{3e} \leftarrow (02) ^{2e}	0.158 708 5 (50)	4.28 (35)	1.164 (91)
(03) ^{3f}	(03) ^{3f} \leftarrow (02) ^{2f}	0.158 689 70 (67)	1.636 (11)	
(03) ^{1e}	(03) ^{1e} \leftarrow (02) ^{0e}	0.158 469 13 (54)	2.759 1 (76)	
(03) ^{1f}	(03) ^{1f} \leftarrow (02) ^{2f}	0.158 384 8 (40)	4.25 (28)	
(04) ^{4e}	(04) ^{4e} \leftarrow (03) ^{3e}	0.159 219 91 (87)	1.983 (19)	
(04) ^{4f}	(04) ^{4f} \leftarrow (03) ^{3f}	0.159 219 29 (56)	1.993 (14)	
(04) ^{2e}	(04) ^{2e} \leftarrow (03) ^{1e}	0.159 215 2 (32)	2.91 (15)	
(04) ^{2f}	(04) ^{2f} \leftarrow (03) ^{1f}	0.159 241 8 (19)	3.62 (12)	8.0 (16)
(04) ^{0e}	(04) ^{0e} \leftarrow (03) ^{1e}	0.159 224 9 (36)	7.37 (24)	-18.4 (50)

TABLE IV

Spectroscopic Constants of NCCN in the Effective Hamiltonian (the Numbers in Parentheses Give One Standard Deviation in Units of the Last Digits Given)

Vibrational constants				
State	G_v / cm^{-1}	x_k / cm^{-1}	$10^5 y_k / \text{cm}^{-1}$	
(00)	0.0			
(01)	233.879 144 (23) ^a			
(02)	464.866 405 (35)	0.918 829 6 (90)		
(03)	695.812 505 (46)	0.908 716 7 (64)		
(04)	925.850 387 (51)	0.897 639 0 (11)	6.687 (68)	
Rotational constants				
State	B_v / cm^{-1}	$10^3 (B_v - B_0) / \text{cm}^{-1}$	$10^7 d_{JK} / \text{cm}^{-1}$	
(00)	0.157 087 69 (14)	0.0		
(01)	0.157 626 63 (14) ^a	0.538 94 (20)		
(02)	0.158 163 80 (14)	1.076 11 (20)	-5.29 (13)	
(03)	0.158 698 47 (15)	1.610 78 (21)	-6.74 (10)	
(04)	0.159 230 77 (6)	2.143 08 (15)	-7.67 (5)	
State	$10^8 D_v / \text{cm}^{-1}$	$10^{11} h_{JK} / \text{cm}^{-1}$	$10^4 q_S / \text{cm}^{-1}$	$10^{10} q_{SJ} / \text{cm}^{-1}$
(00)	2.110 6 (16)			
(01)	2.205 1 (17) ^a		2.228 24 (23)	6.114 (80)
(02)	2.299 5 (19)	1.82 (38)	2.232 95 (48)	5.978 (97)
(03)	2.397 8 (29)	2.76 (37)	2.240 88 (31)	6.14 (14)
(04)	2.475 1 (16)	5.00 (17)	2.246 25 (87)	4.10 (34)

^aFor determination of the ν_5 -dependence of G_v , B_v , and D_v , extrapolated values of x_k , d_{JK} , and h_{JK} were subtracted from these values.

An intensity alternation of spectral transitions arising from the spin statistics of adjacent rotational levels is characteristic for molecules with symmetrically equivalent atoms. The spin statistics for NCCN are derived by considering the symmetry representation (Γ) with respect to the exchange of equivalent atoms. Following the Born–Oppenheimer approximation the total wavefunction describing the state of the molecule can be written as

$$\Psi_{\text{tot}} = \Psi_{\text{el}} \Psi_{\text{vib}} \Psi_{\text{rot}} \Psi_{\text{ns}}. \quad (5)$$

Bosons with integer values for nuclear spin quantum number I have symmetric Ψ_{tot} [$\Gamma(\Psi_{\text{tot}}) = A_1$], fermions with half integer values of I have antisymmetric Ψ_{tot} [$\Gamma(\Psi_{\text{tot}}) = B_2$]. In general there are $(2I + 1)^2$ possible Ψ_{ns} , of which $(2I + 1)(I + 1)$ are symmetric and $(2I + 1)I$ are antisymmetric. NCCN has two sets of equivalent atoms, but since $I(^{12}\text{C}) = 0$ the carbon atoms have no influence on spin statistics. Since $I(^{14}\text{N}) = 1$ the molecule NCCN is a boson, and the product function Ψ_{tot} has to be symmetric. The electronic ground state Ψ_{el} is symmetric. If we consider the ground vibrational state, $\Gamma(\Psi_{\text{vib}}) = A_1$. Thus $\Gamma(\Psi_{\text{rot}}) = A_1$ must be combined with $\Gamma(\Psi_{\text{ns}}) = A_1$, and $\Gamma(\Psi_{\text{rot}}) = B_2$ with $\Gamma(\Psi_{\text{ns}}) = B_2$. The molecule NCCN exhibits six symmetric and three antisymmetric Ψ_{ns} . Since $\Gamma(\Psi_{\text{rot}}) = A_1$ for even J and $\Gamma(\Psi_{\text{rot}}) = B_2$ for odd J , transitions from states with even J have a statistical weight of six and odd J of three. The first excited bending states $(01)^{1e}$ and $(01)^{1f}$ have B_2 and A_1 symmetry, respectively. Therefore the rotational levels of the $(01)^{1e}$ substate with even J have a statistical weight of three and odd J of six, and vice versa for the $(01)^{1f}$ substate.

SPECTRUM AND ASSIGNMENTS

An overview of the ν_5 band system is given in Fig. 1. The most striking property of the spectrum is the very high line density, due to the small rotational constant B , the

TABLE V

Measured and Assigned Line Positions of the ν_5 Band System of NCCN

P -branch J''	P -branch ν/cm^{-1}		Q -branch ν/cm^{-1}		$(o-c)$		R -branch ν/cm^{-1}		$(o-c)$		P -branch J''	P -branch ν/cm^{-1}		Q -branch ν/cm^{-1}		$(o-c)$		R -branch ν/cm^{-1}		$(o-c)$			
	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$		ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^6/\text{cm}^{-1}$		
	(01) ^a * - (100) ^b *											(01) ^a * - (100) ^b *											
0	(233 407 543)	233 725 631*	817	234 350 719*	-1714	234 350 719*	-1714	234 350 719*	-1714	235 453 314	-14	235 733 448*	-1394	253 020 466	14								
1	(233 093 003)	120	233 725 498	518	234 350 719*	-1714	234 350 719*	-1714	235 187 471	-22	235 856 597*	-1468	253 382 774	-135									
2	232 781 514	-45	233 725 841	518	234 986 862	97	234 986 862	97	235 658 186	-22	236 008 205	-50	254 110 060	-121									
4	232 469 812	-140	233 734 384	-141	235 305 880*	669	235 305 880*	669	236 394 810	-20	236 085 549	326	254 475 062	32									
6	232 449 251	270	233 725 266	201	233 944 567	-97	233 944 567	-97	236 167 323	-15	236 160 050*	-3386	254 840 680	59									
7	(231 540 276)	233 757 666	-270	236 265 849	189	236 265 849	189	235 610 616*	688	236 243 152	-20	236 243 152	-20	255 574 231	-24								
8	231 327 629	579	233 768 346	6	236 587 127*	-1657	236 587 127*	-1657	234 350 920	13	235 942 556	-25	255 942 556	-3									
9	231 297 147	103	233 725 334	-88	234 350 719*	57	234 350 719*	57	234 833 776	36	235 860 014	-19	255 860 014	-19									
10	230 618 245	-80	233 793 095	39	237 732 944*	-819	237 732 944*	-819	235 575 396	7	235 050 949	-52	257 050 949	-52									
11	230 320 525	-74	233 807 403	55	237 538 007	-156	237 538 007	-156	234 318 918	24	237 422 029	-44	257 422 029	-44									
12	230 068 218	736	233 823 137	188	237 883 586	178	237 883 586	178	235 732 959	59	235 732 959	-13	255 732 959	-13									
13	229 801 166	77	233 823 137	187	237 883 586	179	237 883 586	179	234 350 862	12	235 557 140	-70	255 557 140	-70									
14	229 740 188	97	233 857 649	349	238 536 364	-81	238 536 364	-81	231 808 480	14	235 166 720	-85	255 166 720	-85									
15	229 099 196	262	233 877 579	38	238 662 574*	-1657	238 662 574*	-1657	231 554 581	48	238 540 595	-7	255 540 595	-7									
16	228 999 196	262	233 877 579	38	238 662 574*	-1657	238 662 574*	-1657	231 554 581	48	238 540 595	-7	255 540 595	-7									
17	228 497 101	-103	233 823 137	-88	234 350 719*	57	234 350 719*	57	231 043 755	30	235 860 014	-40	255 860 014	-40									
18	228 197 477	-154	233 943 578	-729	239 852 539	-118	239 852 539	-118	231 797 809	-39	235 665 053*	-403	255 665 053*	-403									
19	228 098 648	-73	233 943 578	-1137	240 183 849	31	240 183 849	31	232 514 505	31	232 514 505	-56	255 514 505	-56									
20	227 940 166	77	233 823 137	187	237 883 586	-57	237 883 586	-57	231 043 816	-89	231 043 816	-89	255 073 174	-76	255 073 174	-76							
21	227 301 998	-87	234 021 124*	-610	240 848 713	67	240 848 713	67	231 043 816	-9	231 043 816	-9	260 797 543	-118	260 797 543	-118							
22	227 007 145	-135	234 080 068	-162	241 181 960	-360	241 181 960	-360	211 808 662	12	211 808 662	12	261 176 229	-52	261 176 229	-52							
23	226 711 365*	-135	234 080 068	-162	241 516 848	-26	241 516 848	-26	211 808 662	12	211 808 662	12	261 556 144	-14	261 556 144	-14							
24	226 711 365	135	234 080 068	-162	241 516 848	-26	241 516 848	-26	211 808 662	12	211 808 662	12	261 556 144	-14	261 556 144	-14							
25	226 124 123	-43	234 143 734	-15	242 188 567	-59	242 188 567	-59	211 062 054	41	211 062 054	41	262 317 598	-208	262 317 598	-208							
26	225 832 008	86	234 176 808*	-672	242 188 567	-136	242 188 567	-136	210 817 501	73	210 817 501	73	262 699 767	-182	262 699 767	-182							
27	225 832 008	86	234 176 808*	-672	242 188 567	-136	242 188 567	-136	210 817 501	73	210 817 501	73	262 699 767	-182	262 699 767	-182							
28	224 249 111	-150	234 249 111	-150	242 201 980	-70	242 201 980	-70	210 817 501	73	210 817 501	73	262 699 767	-182	262 699 767	-182							
29	224 955 911*	-343	234 286 682	266	243 541 505	-83	243 541 505	-83	210 817 501	73	210 817 501	73	263 465 537	-46	263 465 537	-46							
30	224 669 872	-169	234 325 285	-20	243 882 063	-109	243 882 063	-109	210 817 501	73	210 817 501	73	263 850 009	-114	263 850 009	-114							
31	224 669 872	-169	234 325 285	-20	243 882 063	-109	243 882 063	-109	210 817 501	73	210 817 501	73	264 235 142	-76	264 235 142	-76							
32	224 054 117	-19	234 406 547	-395	244 565 139	-65	244 565 139	-65	209 367 801	150	209 367 801	150	265 007 387	-74	265 007 387	-74							
33	223 807 490	-86	234 450 182	-154	244 908 055	-15	244 908 055	-15	209 367 801	150	209 367 801	150	265 394 127	-131	265 394 127	-131							
34	223 523 292	-51	234 523 292	-51	240 761 635	-49	240 761 635	-49	209 367 801	150	209 367 801	150	265 782 331	131	265 782 331	131							
35	223 523 292	-51	234 523 292	-51	240 761 635	-49	240 761 635	-49	209 367 801	150	209 367 801	150	265 782 331	131	265 782 331	131							
36	222 273 880	-43	234 583 778	-67	240 140 794	-136	240 140 794	-136	207 311 255	450	207 311 255	450	260 166 797	54	260 166 797	54							
37	222 273 880	-43	234 583 778	-67	240 140 794	-136	240 140 794	-136	207 311 255	450	207 311 255	450	261 035 428*	-415	261 035 428*	-415							
38	222 273 880	-43	234 583 778	-67	240 140 794	-136	240 140 794	-136	207 311 255	450	207 311 255	450	261 442 950	-137	261 442 950	-137							
39	222 897 059	-121	234 823 383	217	235 378 207*	-121	235 378 207*	-121	207 311 255	450	207 311 255	450	261 839 031	-409	261 839 031	-409							
40	222 636 573	140	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 067 117	-250	261 067 117	-250							
41	222 377 289	34	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
42	222 377 289	34	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
43	221 863 725	35	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
44	221 669 491	207	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
45	221 669 491	207	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
46	221 920 467	17	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
47	221 920 467	17	234 250 286	-254	240 862 650	-63	240 862 650	-63	207 311 255	450	207 311 255	450	261 407 117	-250	261 407 117	-250							
48	220 855 734	-168	234 250 286	-254	240 862																		

TABLE V—Continued

<i>J''</i>	<i>P</i> -branch	(o-c)	<i>R</i> -branch	(o-c)	<i>J''</i>	<i>P</i> -branch	(o-c)	<i>R</i> -branch	(o-c)	<i>J''</i>	<i>P</i> -branch	(o-c)	<i>R</i> -branch	(o-c)		
	ν/cm^{-1}	$\times 10^4/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^4/\text{cm}^{-1}$		ν/cm^{-1}	$\times 10^4/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^4/\text{cm}^{-1}$		ν/cm^{-1}	$\times 10^4/\text{cm}^{-1}$	ν/cm^{-1}	$\times 10^4/\text{cm}^{-1}$		
50	219 459 006	77	251 383 601	-252	17	225 964 920	17	231 273 482	-92	237 034 688	6					
51	219 186 148	-51	251 743 265	37	18	225 671 727	68	231 288 212	-294	237 373 995	208					
52	218 914 192	-51	251 101 563	37	19	225 671 727	93	231 320 689	-137	237 373 995	171					
53	218 643 431	251	252 461 434	-120	20	225 008 859	-29	231 320 688	-18	238 055 602	-8					
54	218 372 671	-29	253 134 163	46	21	224 799 271	58	231 337 176*	-784	238 397 676	-434					
55	218 103 605	-26	253 546 382	171	22	224 511 107	79	231 355 864	-108	238 741 196*	-991					
56	217 835 077	-26	253 546 382	-12	23	224 511 107	415	231 355 864	-173	238 741 196*	-175					
57	217 566 302	-145	253 546 382	265	24	224 393 362	367	231 394 312	77	239 433 291	-157					
58	217 298 013	-101	254 373 540	-265	25	223 653 164	-140	231 413 489*	-978	239 700 667	-139					
59	217 034 647	-41	254 636 377	44	26	223 653 164	34	231 413 489*	-240	240 478 921	86					
60	216 769 883	296	255 003 864	1	27	223 087 426	-2	231 457 072	-12	240 478 921	-2					
61	216 503 339	-17	255 134 033	-1	28	222 006 239	-4	231 479 509	61	240 829 661						
62	216 241 915	-8	255 737 324	-5	29	222 526 271	58	231 502 254	-248	241 181 900	491					
63	215 979 403	42	256 105 296	75	30	222 526 271	135	231 502 254	-247	241 181 900	54					
64	215 717 454	-202	256 136 868		31	221 969 141*	-435	231 550 877	193	241 888 498	62					
65	215 454 921	-9	256 841 362	-56	32	221 692 709	-237	231 575 660	-29	242 243 129	-379					
66	215 196 771	-9	257 213 465	-94	33	221 417 365	-58	231 661 248	-140	242 599 635	55					
67	214 937 620	9	257 584 742	189	34	221 417 365	125	231 661 248	-102	242 599 635	55					
68	214 670 875	-2	257 584 742	-24	35	220 869 706	123	231 654 308	-361	243 314 927	-57					
69	214 427 051	240	258 328 933	72	36	220 597 406	-9	231 682 115	-112	243 674 268	85					
70	214 165 138	-40	258 702 009	-144	37	220 597 406	-40	231 708 214	33	243 737 332	33					
71	213 165 170	281	259 134 033	173	38	220 556 122	58	231 738 561*	-550	244 395 649	48					
72	213 084 564	-17	259 134 033	-174	39	219 766 904	-57	231 768 333	-80	244 757 754	44					
73	213 400 269	-70	259 826 649	4	40	219 518 270	-155	231 796 927*	-1343	245 120 642	-174					
74	213 146 955	-123	260 202 595	-43	41	219 518 270	125	231 826 649	-247	245 120 642	-166					
75	(212 270 771)	271	260 202 595	-136	42	219 884 971*	-749	231 859 718	120	245 849 868	34					
76	(212 242 890)	-187	260 557 936	-56	43	218 720 538	-88	231 891 025	-18	246 215 619	-100					
77	(212 199 327)	220	(216 336 606)		44	218 720 538	104	231 891 025	-25	246 215 619	-300					
78	212 142 385	-51	261 716 058	74	45	218 193 379	8	231 955 878	450	246 948 212*	-174					
79	-	(212 199 327)	220	261 716 058		46	217 669 774	-51	231 021 683	-37	247 688 072	-22				
80	-	(212 199 327)	220	261 716 058		47	217 669 774	-103	231 055 352	-16	248 058 271	-55				
81	-	(212 199 327)	220	261 716 058		48	217 669 774	-103	231 055 352	-27	248 058 271	-166				
82	-	(212 199 327)	220	261 716 058		49	218 691 475	65	231 124 301	-205	248 801 188	-72				
83	-	(212 199 327)	220	261 716 058		50	218 691 475	65	231 124 301	-205	248 801 188	-72				
1	230 829 673	-182	231 146 159	422	(231 778 837)		51	218 633 688	-25	232 159 423	-188	249 173 867	-67			
2	230 516 109	-13	231 147 669	230	(232 097 874)	119	52	215 105 251	-58	232 379 127*	875	251 426 061	-9			
3	230 203 767	80	231 150 114	122	231 428 408*	442	53	214 851 556	-1872	251 415 633	-291	251 803 950	-44			
4	229 282 238*	-131	231 150 114	-94	231 428 408*	-130	54	214 660 321	-12	251 812 575						
5	229 028 175	-65	231 150 114	33	231 428 408*	-130	55	214 660 321	-11	251 812 575						
6	229 273 529*	-63	231 162 768	31	231 386 243	-91	56	214 660 321	-11	251 812 575						
7	228 967 311*	400	231 168 708	34	(237 711 691)		57	214 660 321	-11	251 812 575						
8	228 745 745	-263	231 168 708	58	(237 711 691)		58	214 660 321	-11	251 812 575						
9	228 556 745	-460	231 168 708	69	234 366 234		59	213 111 704	-12	251 812 575						
10	228 252 722	-174	231 191 151	-361	(236 695 410)		60	216 865 866	9	252 277 813*	-493	254 851 949	59			
11	227 750 980	185	231 200 783	-5	(235 025 850)		61	216 865 866	129	252 277 813*	-493	254 851 949	59			
12	227 447 255	28	231 211 628*	73	(235 025 850)		62	216 865 866	129	252 277 813*	-493	254 851 949	59			
13	227 250 949	31	231 211 628*	47	(235 025 850)		63	216 865 866	-843	252 277 813*	-135	256 005 453	-46			
14	226 851 325*	-829	231 232 529*	-915	(236 024 693)		64	216 889 717		252 277 813*	-222	256 391 289	22			
15	226 555 387	242	231 245 977	-110	236 360 109	-18	65	216 889 717	50	252 931 300*	-66	256 777 590	-51			
16	226 259 918*	571	231 259 319	-113	236 696 969	176	66	216 405 513	15	252 972 749*	-877	257 164 643				
1	(234 022 066)		(235 608 993)				67	216 405 513		252 972 749*						
3	(233 707 868)		(235 929 560)				68	216 405 513		252 972 749*						
4	(233 394 155)	-578	(235 251 165)	-174			69	216 405 513		252 972 749*						
5	(233 081 049)	-174	(235 251 165)	-174			70	216 405 513		252 972 749*						
6	(232 191 197)	-263	(235 251 165)	-98			71	216 405 513		252 972 749*						
7	(232 462 012)	283	(237 222 587)	143			72	216 405 513		252 972 749*						
8	(232 153 406)	551	(237 227 587)	-45			73	216 405 513		252 972 749*						
9	(232 153 407)	-65	(237 227 587)	-240			74	216 405 513		252 972 749*						
10	(231 538 802)	475	(238 201 038)	-219			75	216 405 513		252 972 749*						
11	(231 232 629)	-44	(238 332 542)	-79			76	216 405 513		252 972 749*						
12	(231 232 627)	-163	(238 332 542)	-154			77	216 405 513		252 972 749*						
13	(230 624 318)	-571	(239 129 520)	-174			78	216 405 513		252 972 749*						
14	(230 320 528)*	-577	(239 525 368)*	-540			79	216 405 513		252 972 749*						
15	(230 070 210)	-611	(239 525 368)*	-567			80	216 405 513		252 972 749*						
16	(230 227 587)	-103	(239 525 368)*	-562			81	216 405 513		252 972 749*						
17	(230 420 503)*	883	(240 527 924)*	-1139			82	216 405 513		252 972 749*						
18	(229 123 766)	466	(241 884 061)	-1598			83	216 405 513		252 972 749*						
21	(228 235 392)	-194	(242 881 664)	-96			84	216 405 513		252 972 749*						
22	(227 294 635)	-262	(242 881 664)	97			85	216 405 513		252 972 749*						
23	(227 294 635)	-262	(242 881 664)	-19			86	216 405 513		252 972 749*						
24	(227 357 821)	-16	(242 881 664)	-64			87	216 405 513		252 972 749*						
25	(227 067 384)	-38	(243 516 965)	-15			88	216 405 513		252 972 749*						
26	(226 778 118)	-38	(243 516 965)	-15			89	216 405 513		252 972 749*						
27	(226 544 256)	-163	(244 290 742)	63			90	216 405 513		252 972 749*						
28	(226 203 008)	-204	(244 290 742)	63			91	216 405 513		252 972 749*						
29	(225 916 849)	-236	(244 369 149)	-49			92	216 405 513		252 972 749*						
30	(225 633 522)	-164	(244 369 149)	-50			93	216 405 513		252 972 749*						
31	(224 784 8															

TABLE V—Continued

<i>P</i> -branch <i>J'</i>	<i>v</i> /cm ⁻¹	(o-c) $\times 10^4/\text{cm}^{-1}$	<i>R</i> -branch <i>J''</i>	(o-c) $\times 10^4/\text{cm}^{-1}$	<i>P</i> -branch <i>J'</i>	<i>v</i> /cm ⁻¹	(o-c) $\times 10^4/\text{cm}^{-1}$	<i>R</i> -branch <i>J''</i>	(o-c) $\times 10^4/\text{cm}^{-1}$
(03) ^a — (02) ^b					(03) ^a — (02) ^b				
15 230 020 210	328	239 658 672	377		71	—	—	—	—
16 229 719 521	168	240 192 694	273		72	—	(259 319 822)	260 299 527 ^c	1008
17 229 420 503 ^d	647	240 527 924	351						
18 228 842 070	137	241 201 453	328		3 230 179 441 ^e	—	—	—	—
19 228 842 076	137	241 201 405 ^f	506		4 230 443 660	-1552	231 701 699 ^g	580	233 286 926
20 228 526 883 ^d	627	241 319 207	140		5 230 465 420	765	231 701 699 ^g	147	233 286 926
21 228 321 199 ^d	896	241 877 465 ^f	-765		6 230 467 549	61	231 728 192	221	233 297 950
22 227 644 725	141	242 201 453	48		7 230 495 629	626	231 738 561	-36	234 248 992
23 227 351 896	442	242 559 529	14		8 229 182 985	25	231 750 651	-87	234 570 530
24 227 059 392	21	242 901 451	-174		9 228 560 966	100	231 779 536	-116	234 864 587
25 226 769 327	-80	243 188 702	3		10 228 560 990	71	231 779 536	-165	235 215 667 ^h
26 226 480 574	5	243 933 642	-92		11 228 560 990	58	231 966 927 ⁱ	587	235 540 682
27 226 182 057	-27	244 279 645	-30		12 227 374 664	-234	231 834 253 ^j	-102	235 864 587
28 226 182 057	36	244 279 645	-40		13 227 374 664	-234	231 834 253 ^j	-129	235 864 587
29 225 617 820	-179	244 974 425	66		14 227 374 664	-31	231 855 775	72	236 515 420
31 225 332 362	-21	245 323 678 ^k	592		15 227 017 435	182	231 878 435	-127	236 840 822 ^h
32 225 048 618	83	245 672 708	-18		16 226 404 461	895	231 955 678	-52	236 840 822 ^h
33 224 184 467	608	246 201 453	7		17 226 498 091	113	231 928 280	-672	237 496 472
34 224 481 105 ^d	-49	246 374 681	-26		18 226 553 219	-23	231 955 678	-513	237 824 398
35 224 199 052	-204	246 727 132	102		19 226 553 219	55	231 985 424	-238	238 153 643
36 224 199 052	241	246 727 132	-29		20 226 553 219	126	231 985 424	-282	238 153 643
37 223 638 338	160	247 414 404	115		21 225 186 637	37	232 048 141	-30	238 813 068
38 223 359 119	138	247 789 367	154		22 224 883 873	1	232 048 505	-376	239 143 816
39 223 062 118 ^d	1451	248 144 936	-50		23 224 883 873	1	232 116 804	-352	239 143 816
40 222 756 777	394	248 144 936	21		24 224 883 873	1	232 116 804	-352	239 143 816
41 222 526 271	-381	248 859 079	65		25 224 883 873	1	232 116 804	-352	239 143 816
42 222 250 716	-217	249 217 271	11		26 224 883 873	1	232 116 804	-352	239 143 816
43 221 217 271	249	249 217 271	107		27 224 883 873	1	232 116 804	-352	239 143 816
44 221 701 876	-104	249 336 117	-45		28 224 883 873	1	232 116 804	-352	239 143 816
45 221 428 889	63	250 196 734	-63		29 224 883 873	1	232 116 804	-352	239 143 816
46 221 156 539	95	250 658 209	0		30 224 883 873	1	232 116 804	-352	239 143 816
47 220 842 065 ^d	-508	251 336 166 ^k	15		31 224 883 873	1	232 116 804	-352	239 143 816
48 220 614 202 ^d	96	251 363 601 ^k	280		32 224 883 873	1	232 116 804	-352	239 143 816
49 220 344 216 ^d	82	251 747 147 ^f	145		33 224 883 873	1	232 116 804	-352	239 143 816
50 220 074 789 ^d	-158	252 111 174	158		34 224 883 873	1	232 116 804	-352	239 143 816
51 220 074 789 ^d	250	252 111 174	35		35 224 883 873	1	232 116 804	-352	239 143 816
52 219 359 024 ^d	124	252 842 657 ^k	228		36 224 883 873	1	232 116 804	-352	239 143 816
53 219 272 024 ^d	0	253 209 431 ^k	430		37 224 883 873	1	232 116 804	-352	239 143 816
54 218 217 024	180	253 376 166 ^k	326		38 224 883 873	1	232 116 804	-352	239 143 816
55 218 140 743 ^d	217	254 336 166 ^k	-72		39 224 883 873	1	232 116 804	-352	239 143 816
56 218 767 160 ^d	269	254 313 108	223		40 224 883 873	1	232 116 804	-352	239 143 816
57 218 212 549 ^d	560	254 682 587 ^k	379		41 224 883 873	1	232 116 804	-352	239 143 816
58 217 949 213 ^d	400	254 682 587 ^k	-123		42 224 883 873	1	232 116 804	-352	239 143 816
59 215 833 770	83	254 906 941 ^k	-166		43 224 883 873	1	232 116 804	-352	239 143 816
60 215 723 335	72	254 906 941 ^k	-467		44 224 883 873	1	232 116 804	-352	239 143 816
61 215 506 178	7	255 794 520 ^k	371		45 224 883 873	1	232 116 804	-352	239 143 816
62 215 166 376	280	256 174 404	-53		46 224 883 873	1	232 116 804	-352	239 143 816
63 215 166 376	531	256 174 404	-531		47 224 883 873	1	232 116 804	-352	239 143 816
64 215 262 454	705	256 912 596 ^k	693		48 224 883 873	1	232 116 804	-352	239 143 816
65 215 661 070	852	256 912 596 ^k	-852		49 224 883 873	1	232 116 804	-352	239 143 816
66 215 262 309	349	256 912 596 ^k	706		50 224 883 873	1	232 116 804	-352	239 143 816
67 215 217 309	258 411 561 ^k	561			51 224 883 873	1	232 116 804	-352	239 143 816
68 215 217 309	258 788 153 ^k	849			52 224 883 873	1	232 116 804	-352	239 143 816
69 215 217 309	-259 164 212 ^k	1099			53 224 883 873	1	232 116 804	-352	239 143 816

TABLE V—Continued

<i>P</i> -branch <i>J'</i>	<i>v</i> /cm ⁻¹	(o-c) $\times 10^4/\text{cm}^{-1}$	<i>Q</i> -branch <i>J''</i>	<i>v</i> /cm ⁻¹	<i>P</i> -branch <i>J'</i>	<i>v</i> /cm ⁻¹	(o-c) $\times 10^4/\text{cm}^{-1}$	<i>R</i> -branch <i>J''</i>	<i>v</i> /cm ⁻¹	(o-c) $\times 10^4/\text{cm}^{-1}$
(03) ^a — (02) ^b					(03) ^a — (02) ^b					
50 216 716 775	6	233 576 905 ^k	494	248 698 792	20	51 216 453 691	-36	(232 641 064)		
51 216 435 691	561	233 576 905 ^k	556	249 640 424	34	52 216 443 341	-45	(232 641 064)		
52 216 157 994	-57	233 839 770	318	249 640 424	34	53 216 443 341	-45	(232 641 064)		
53 216 157 994	52	233 839 770	318	249 640 424	34	54 216 443 341	-46	(232 641 064)		
54 216 603 724	64	234 008 677	-407	250 114 699	263	55 216 623 166	-54	(232 641 064)		
55 215 327 791	58	234 096 941 ^k	573	250 470 069	89	56 215 327 791	-54	(232 641 064)		
56 215 327 791	83	234 096 941 ^k	-121	250 470 069	89	57 215 327 791	-54	(232 641 064)		
58 215 703 335	72	251 443 509	-121	251 443 509	25	59 215 703 335	-86	(232 641 064)		
59 214 234 308	7	251 443 509	25	251 443 509	25	60 214 234 308	-94	(232 641 064)		
60 214 234 308	-57	251 443 509	51	251 443 509	51	61 214 234 308	-94	(232 641 064)		
61 213 693 088	-80	252 111 174	128	252 125 137	128	62 213 693 088	-94	(232 641 064)		
62 213 693 088	143	252 111 174	-237	252 866 720 ^k	-595	63 213 693 088	-94	(232 641 064)		
63 213 156 106	61	252 111 174	111	252 714 872	181	64 213 156 106	-94	(232 641 064)		
64 213 156 106	-3	252 111 174	-3	254 445 745	145	65 213 156 106	-94	(232 641 064)		
65 212 232 099	28	255 180 712	9	255 180 712	9	66 212 232 099	-106	(232 641 064)		
66 212 232 099	127	255 180 712	-121	255 180 712	-121	67 212 232 099	-106	(232 641 064)		
67 212 232 099	127	255 180 712	9	255 180 712	9	68 212 232 099	-106	(232 641 064)		
68 212 232 099	4	255 180 712	-121	255 180 712	-121	69 212 232 099	-106	(232 641 064)		
69 212 232 099	126	255 180 712	9	255 180 712	9	70 212 232 099	-106	(232 641 064)		
70 212 232 099	-14	255 180 712	9	255 180 712	9	71 212 232 099	-106	(232 641 064)		
72 210 787 965	-8	256 688 990	32	256 660 421	69	73 210 787 965	-106	(232 641 064)		
73 210 529 754	-76	257 032 648	-118	257 032 648	-118	74 210 529 754	-106	(232 641 064)		
74 210 529 754	129	257 032 648	-118	257 032 648	-118	75 210 529 754	-106	(232 641 064)		
75 210 016 377	-154	257 779 649	-370	257 779 649	-370	76 210 016 377	-106	(232 641 064)		
76 209 761 313	-50	258 155 189	136	258 155 189	136	77 209 761 313	-106	(232 641 064)		
78 209 602 099	82	258 155 189	-101	260 784 209 ^k	-678	79 209 602 099	-106	(232 641 064)		
79 209 602 099	145	258 155 189	-124	260 784 209 ^k	-678	80 209 602 099	-106	(232 641 064)		
80 208 928 380	232	259 665 053 ^k	870	259 665 053 ^k	-39	81 208 928 380	-106	(232 641 064)		
81 208 928 380	141	259 665 053 ^k	-39	259 665 053 ^k	-39	82 208 928 380	-106	(

TABLE V—Continued

<i>J'</i>	<i>P</i> -branch ν / cm^{-1}	<i>R</i> -branch ν / cm^{-1}	(o-c) $\times 10^6 / \text{cm}^{-1}$	<i>P</i> -branch ν / cm^{-1}	<i>R</i> -branch ν / cm^{-1}	(o-c) $\times 10^6 / \text{cm}^{-1}$	<i>P</i> -branch ν / cm^{-1}	<i>R</i> -branch ν / cm^{-1}	(o-c) $\times 10^6 / \text{cm}^{-1}$	<i>P</i> -branch ν / cm^{-1}	<i>R</i> -branch ν / cm^{-1}	(o-c) $\times 10^6 / \text{cm}^{-1}$
(03) ^a — (03) ^b												
15	223 973 056	-21	-233 786 192									
16	223 666 270	-24	-234 110 790									
17	223 359 119	-27	-234 435 862									
18	223 053 145	29	-234 761 410									
19	222 737 070	33	-234 987 317									
20	222 442 443	35	-235 413 948									
21	222 138 011	-37	-235 740 944									
22	221 834 049	40	-236 092 933									
23	221 529 075	-43	-236 428 015									
24	221 227 358	-45	-236 753 863	-29								
25	220 924 973	45	-237 083 554	30								
26	220 622 861	50	-237 416 438	33								
27	220 319 790	53	-237 750 273	35								
28	220 202 041	-55	-238 080 999	-37								
29	219 719 144	57	-238 411 070	360								
30	219 411 251	59	-238 741 917	-382								
31	218 118 979	61	-239 079 417	41								
32	218 189 209	-62	-239 412 802	-42								
33	218 510 280	-64	-239 747 021	-43								
34	218 202 051	65	-240 080 737	43								
35	217 927 283	-67	-240 415 676	44								
36	217 624 542	67	-240 750 551	-451								
37	217 326 837	68	-241 085 781	452								
38	217 124 554	-68	-241 420 915	45								
39	216 731 907	68	-241 712 325									
40	(216 367 465)		-242 092 098	43								
41	216 138 126	67	-242 385 751									
42	216 125 597	68	-242 720 851	41								
43	215 543 891	63	-243 100 634	-40								
44	215 248 927	63	-243 437 057	38								
45	214 953 068	-61	-243 773 010	35								
46	-	244 110 045	-	-33								
47	-	244 466 211	-	30								
48	-	244 783 742	-	-27								
(04) ^a — (03) ^b												
3	(234 170 554)		-236 389 953	339								
4	233 856 329		-236 721 923	-336								
5	(233 543 152)		-237 045 837	-113								
6	(233 231 040)		-237 369 888*	-804								
7	(232 919 978)		-237 696 544	62								
8	(232 599 998)		-238 023 010	115								
9	(231 360 017)		-238 351 277	77								
10	(231 993 119)		-238 680 376	191								
11	(231 686 175)		-239 010 026	-85								
12	(231 380 487)		-239 341 785	-158								
13	(231 186 688)		-239 673 114	-42								
14	230 771 547	-529	-240 006 397	99								
15	230 469 048	-405	(240 340 444)									
16	230 168 035	151	(240 675 630)									
17	229 876 726	-148	-241 037 402	23								
18	229 568 040	160	-241 349 142	24								
19	229 269 378	-179	-241 687 417	-1								
20	(228 972 156)		-242 026 915	162								
21	228 618 998	88	-242 367 915	53								
22	228 360 346	-211	-242 708 347	-120								
23	228 086 174	77	-243 050 918									
24	227 793 753*	560	-243 394 379	50								
25	227 501 193	109	-243 738 581	-218								
26	227 200 990	68	-244 080 201									
27	226 920 125	119	-244 430 933	133								
28	226 631 211	138	-244 778 411	76								
29	226 340 055	138	-245 126 735	173								
30	226 056 311	90	-245 476 476	31								
31	225 770 571	195	-245 827 277	260								
32	225 465 578	9	-246 178 178	150								
33	225 172 772	174	-246 524 410	265								
34	224 919 266	193	-246 864 988	215								
35	224 637 742	382	-247 239 537	176								
36	224 351 511	224	-247 604 551	509								
37	224 077 658*	616	-248 591 794									
38	223 799 022	606	-249 306 350	261								
39	223 521 792*	468	-249 660 314*	674								
40	223 230 900	180	-249 907 247	174								
41	222 969 106*	422	-249 887 666	-16								
42	222 694 418	283	-249 749 386	221								
43	222 424 594	-2	(249 705 013)	-16								
44	222 148 111	79	-249 475 014	-16								
45	221 876 533	2	-249 389 483	80								
46	221 605 547*	-456	-250 204 754	24								
47	221 321 070	124	-250 573 832	-411								
48	221 067 822	-42	-251 938 048	-174								
49	220 860 30	-206	-252 306 489	114								
50	220 513 827	40	-252 675 381	-79								
51	220 227 000	132	-253 024 644	70								
52	219 004 300*	815	-253 416 444	50								
53	219 739 854	55	-253 788 442	215								
54	219 477 056	-13	-254 134 739	151								
55	-	254 354 779	173									
56	-	254 909 123	-7									
57	-	255 284 378	-411									
58	-	255 632 832	-174									
59	-	256 037 692	-255									
60	-	256 416 277	331									
61	-	256 770 207	421									
62	-	257 174 698	236									
63	-	257 555 036	72									
64	-	257 936 241	-42									
(04) ^a — (03) ^b												
1	228 971 834*	934	-									
2	228 656 565*	1096	-229 289 793	93								
3	228 411 756	206	-									
4	228 151 612*	-102	-229 184 003*	807								
5	227 718 196	195	-229 294 839	-340								
6	227 408 954	91	-229 299 990*	-759								
7	227 100 701	-278	-229 303 662*	-1352								
8	226 794 341	-246	-229 309 992	126								
9	226 437 814	162	-229 313 211	-46								
10	226 186 555	150	-229 321 305	-10								
11	225 884 371	55	-229 326 704*	-1152								
12	225 584 036	209	-229 347 534	-66								
13	225 287 011	-86	-229 352 445	-110								
14	225 000 668	17	-229 359 415	-114								
15	224 991 215	213	-229 359 417	-114								
16	224 794 855*	-1375	-229 368 556	-17								
17	224 102 964	115	-229 377 894	-302								
18	223 800 400	-42	-229 387 310	-10								
19	223 521 292*	106	-229 401 184*	2402								
20	223 230 903	23	-229 409 963	249								
21	222 942 895	5	-									
22	222 642 811	-1	-									
23	222 370 755	-20	-									
24	222 086 608	0	-									
25	221 806 668	17	-									
26	221 521 655	-14	-									
27	221 241 438	51	-									
28	220 961 568	133	-									
29	220 680 740	124	-									
30	220 405 737	178	-									
31	220 130 248*	-532	-									
32	219 846 75	-43	-									
33	219 541 302	-111	-									
34	219 308 455	66	-									

TABLE V-Continued

<i>J'</i>	P-branch		R-branch		Q-branch	
	ν / cm^{-1}	$\times 10^3 / \text{cm}^{-1}$	ν / cm^{-1}	$\times 10^3 / \text{cm}^{-1}$	ν / cm^{-1}	$\times 10^3 / \text{cm}^{-1}$
6	230 361 518*	-2009	-	(04) ^{1e} - (03) ^{1f}	-	
7	230 054 969	-719	-			
8	229 749 778	389	-			
9	229 446 460	-7	-			
10	229 140 708*	-736	-			
11	228 838 715*	-1106	236 164 036*	-527		
12	228 539 635	-146	236 501 723	217		
13	228 234 167	17	-			
14	227 944 140	-366	237 180 065	-170		
15	227 648 958	-344	237 521 998	-56		
16	227 354 577	-306	237 862 432	-100		
17	227 058 542	-306	238 209 606*	-99		
18	226 773 187	-449	238 557 758	211		
19	226 485 707*	579	238 905 853	-273		
20	226 187 777	-1106	239 252 919	9		
21	225 881 415	104	239 608 563	29		
22	225 628 725*	-1123	239 962 293	-113		
23	225 348 556	-25	240 318 036	-61		
24	225 051 531	-52	240 354 444	-89		
25	224 791 169	31	241 034 866	-70		
26	224 514 818	-397	241 396 325	-3		
27	224 239 471*	-1722	241 759 834	292		
28	224 042 167	-1642	241 805 253	-86		
29	223 699 478*	509	242 491 844	3		
30	223 430 784	-40				
31	223 164 582	-113	243 211 973	-187		
32	222 870 610	-245	243 605 371	-25		
33	222 638 610	3	243 980 956	23		
34	222 377 289*	-1417	244 357 738	-430		
35	222 180 767	-1138	244 726 151	-113		
36	221 863 725*	-1813	245 120 642	1128		
37	-		245 503 181	-293		
38	-		245 889 141	-513		
39	-		246 274 104	-434		
40	-		246 668 106*	-684		
41	-		247 061 193	-597		
42	-		247 454 165	-607		
43	-		247 854 533	-279		
44	-		248 254 578	-197		
45	-		248 656 259*	-90		
		(04) ^{1f} - (03) ^{1f}				
15	227 530 000	-475	-			
16	227 230 924	-71	-			
17	226 923 058	-6	-			
18	226 615 853	105	238 397 876*	805		
19	226 318 660	-40	238 788 299	250		
20	226 022 924	-75	239 057 785	198		
21	225 597 684	115	239 388 808	64		
22	225 393 160	392	239 720 556	57		
23	225 193 920	9	240 113 111*	-1029		
24	224 784 838	-275	240 386 152	347		
25	224 481 105*	-1055	240 719 432	77		
26	224 284 165	-117	241 038 213	10		
27	223 678 317	55	241 388 217	-31		
28	223 577 244	-25	241 723 624	33		
		(04) ^{1f} - (03) ^{1f}				
29	223 276 883	-32	242 059 323	-208		
30	223 192 355	132	242 733 497	148		
31	222 676 265	-	243 071 068	129		
32	-		243 474 156	-110		
33	-		243 748 815	-103		
34	221 784 815	19	243 748 815	15		
35	221 488 364	49	244 088 356*	621		
36	221 192 350	-136	244 418 489*	623		
37	220 896 355	71	244 748 489	296		
38	220 602 824	31	245 095 970	37		
39	220 309 660*	726	245 451 504	-367		
40	220 015 721	184	245 794 692	280		
41	219 717 197	142	246 048 236	205		
42	219 431 620	280	246 481 236	-87		
43	219 140 365	219	246 825 859	183		
44	218 836 297	297	247 170 599	-53		
45	218 559 929	145				
46	218 270 533	-85	247 862 929*	495		
47	217 987 185	46	248 209 393	142		
48	217 694 634	286	248 444 944	127		
49	217 304 915	171				
50	217 120 996	148	249 253 342	-85		
51	216 836 297	-97	249 491 317	784		
52	216 550 302	151	250 325 705	36		
53	216 266 097	231	250 303 662	406		
54	215 987 403	104	250 654 360	159		
55	215 708 177	41	251 358 891	-511		
56	215 417 433	106	251 358 891	148		
57	215 136 072	136	251 711 391*	-597		
58	215 065 808	513				
59	214 775 396	16	252 036 909*	637		
60	214 296 357	132	252 775 524	113		
61	214 018 202	378	253 131 533	313		
62	213 736 168	53	253 177 577	170		
63	213 463 335	1	253 444 897	19		
64	213 187 745	-8	254 202 750	13		
65	212 910 561*	-198	254 450 232*	-1060		
66	212 620 476	-120	254 920 476	-1213		
67	212 363 786	73				
68	212 090 573	-306	255 641 472	279		
69	211 813 147*	-667	256 356 800*	-1083		
70	-		256 364 800	99		
71	-		256 727 371	-246		
72	-		257 091 309	69		
73	-					
74	-		257 820 794	41		
75	-		258 185 491*	-1178		
76	-		258 444 897	72		
77	-		258 521 230*	300		
78	-		259 289 589*	472		
79	-		259 658 112	-87		

assignment and the *J* assignment are confirmed or if necessary corrected by the use of the combination differences.

The assignment was almost straightforward since the ground state constants and those of the ν_5 manifold ($0n$) states with *n* up to 2 were already known sufficiently well from the literature (4, 5, 6, 7, 22). Transitions with ν_5 up to 4 were finally assigned. In Fig. 2 the band origins of each subband are indicated.

From the hot band (11) \leftarrow (10) in the ν_5 band system only two of the four subbands could be identified, since only information about the (10)^{1e} substate is available in the literature (4) and the spectrum is too dense to allow assignment of the subbands originating from the (10)^{1f} substate without auxiliary information. Therefore the combination band system $\nu_4 + \nu_5$ will be measured at high resolution to fix the upper states of the missing subbands. Also the ν_5 fundamental of the isotopomer N¹³CCN, which should in principle be detectable with its $\approx 2\%$ natural abundance, could not be assigned unambiguously. An extended investigation of all band systems needed to characterize all the singly excited vibrational states, and the combination state of the two bending modes (11), is in progress. The measurement for the parent cyanogen and various isotopomers are partially completed and will be the topic of a subsequent publication.

MOLECULAR CONSTANTS OF CYANOGEN IN THE ν_5 MANIFOLD

Over 1500 rovibrational lines were collected into 16 different subbands. First, each subband was fitted separately to Eq. (1), yielding the power series molecular constants. The band centers of each subband are given in Table II. Table III contains the power series rotational constants of each sublevel and indicates from which transition the

TABLE VI

Comparison of Experimental Vibrational and Rotational Constants of the ν_5 Band System of NCCN with ab Initio Results (the Numbers in Parentheses Give One Standard Deviation in Units of the Last Digits Given)

Parameter	This work	<i>Ab initio</i>	Ref.	Experimental	Ref.
ω_5	234.2530 (50) ^b	249.0	(22)	234.4	(24)
x_{55}	-0.4697 (70)			-0.4	(24)
$x_{k,\epsilon}$	0.9508 (11) ^a				
$x_{k,5}^{(v)}$	0.01068 (28)				
B_0	0.15708769 (14)			0.157073 (5) (22)	
				0.157115 (20) (5)	
				0.157135 (10) (4)	
				0.157124 (7) (6)	
B_e	0.15654618 (96) ^a	0.15443 (22)			
$10^4 \alpha_5$	5.4291 (73) ^b	4.830 (12)	5.45 (3) (2)		
			5.48 (5) (6)		
$10^6 \gamma_{55}$	1.20 (12)		4.5 (15) (6)		
$10^8 D_0$	2.1106 (16)		2.7 (5) (5)		
			2.50 (8) (4)		
			2.63 (8) (6)		
$10^8 D_e$	2.0211 (67) ^a	2.008 (22)			
		2.003 (24)			
$10^{10} \beta_{55}$	9.22 (20)				
$10^{13} H_e$		1.3 (25)			
$10^4 q_5$	2.22824 (23)		3.19 (4)		
			2.259 (9) (6)		
$10^4 q_{5,\epsilon}$	2.2154 (15) ^a	2.051 (13)			
$10^7 q_5^{(v)}$	6.20 (42)				
$10^{10} q_{5,J}$	6.114 (80)	4.67 (21)			

^aThe estimated contributions of the linear terms (Y_i) in v_i ($i \leq 4$) are larger than the error of this constant (X^*):

$$X^* = X_e + \sum_{i=1}^4 Y_i \frac{d_i}{2}.$$

^bThe estimated contributions of the higher order terms (Z_{15}) in v_i and v_j ($i \leq 4$) are larger than the error of this constant Y_5^* :

$$Y_5^* = Y_5 + \sum_{i=1}^4 Z_{15} \frac{d_i}{2}.$$

constants were derived. At this stage of data reduction the quality of the lines was checked. Overlapped lines were omitted if the differences between observed and calculated transition wavenumber (obs-calc) exceeded $1 \times 10^{-3} \text{ cm}^{-1}$.

The constants given in Tables II and III, also valuable for quick calculations, are used to determine estimates of the constants of the effective Hamiltonian [Eqs. (2-4)], as starting values for fitting these constants to the observed transitions. The program presently allows simultaneous fitting of four states. All lines left in the fit were weighted equally. The transitions were split into two fits. The first contained all transitions within four states up to $v_5 = 3$. The second fit contained the states (03) and (04) where the constants of the (03) state were taken from the first fit and held fixed. The resulting constants are given in Table IV. Over 1500 transitions are represented by only 32 spectroscopic constants. In Table V all lines of every subband are given together with the (obs-calc)-values from the effective Hamiltonian fit.

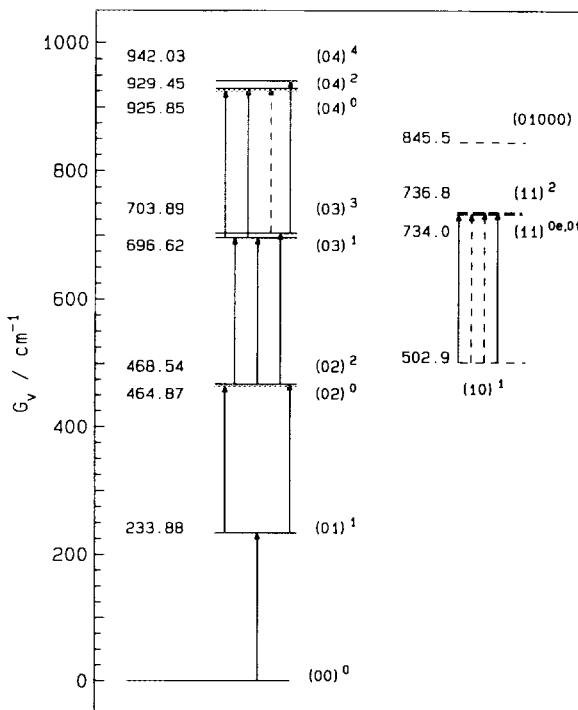


FIG. 4. Vibrational term (G_v) diagram of NCCN. The assigned transitions are indicated with solid arrows. Dashed states are taken from the literature (4). Transitions marked with dashed arrows should be detectable in the spectrum, but could not be assigned.

DISCUSSION

Cyanogen is among the few molecules in which rovibrational transitions may be observed up to a vibrational quantum number of four, without any observable resonance interactions with other normal modes. Therefore it is easy to check the convergence of the expansion of the molecular constants in the vibrational quantum numbers:

$$\begin{aligned}
 G_{v_1, \dots, v_5} &= \sum_i \omega_i \left(v_i + \frac{d_i}{2} \right) + \sum_i \sum_{j \geq i} x_{ij} \left(v_i + \frac{d_i}{2} \right) \left(v_j + \frac{d_j}{2} \right), \\
 B_{v_1, \dots, v_5} &= B_e - \sum_i \alpha_i \left(v_i + \frac{d_i}{2} \right) + \sum_i \sum_{j \geq i} \gamma_{ij} \left(v_i + \frac{d_i}{2} \right) \left(v_j + \frac{d_j}{2} \right), \\
 D_{v_1, \dots, v_5} &= D_e + \sum_i \beta_i \left(v_i + \frac{d_i}{2} \right), \\
 q_{v_1, \dots, v_5} &= q_e + \sum_i q_i^{(v)} \left(v_i + \frac{d_i}{2} \right), \\
 x_{k, v_1, \dots, v_5} &= x_{k,e} + \sum_i x_{i,k}^{(v)} \left(v_i + \frac{d_i}{2} \right). \tag{6}
 \end{aligned}$$

The resulting coefficients are given in Table VI in comparison with experimental and ab initio values in the literature.

The results of ab initio calculations may help to find unassigned experimental transitions. On the other hand the comparison between experimental and calculated values is a touchstone for the theoretical and/or numerical basis of the calculations for species less accessible experimentally. If the difficulties in calculating effects on the order of several Hz for q_{5J} are considered, the comparison between the experimental and calculated values (see Table VI) is remarkable.

The derived molecular constants help us to understand the structure of the ν_5 fundamental band system. The relatively small rotational constant and rotation-vibration interaction constant lead to a high density of lines within one subband. Furthermore a significant population of rotational levels is achieved for J up to ≈ 90 . The small values for the anharmonicity constant x_{55} and the k -dependent part of the vibrational energy causes the origins of each subband within the ν_5 band system to lie very close to the fundamental origin. The origins of all assigned subbands are extended only over a region of $\approx 7 \text{ cm}^{-1}$. The very high line density makes it difficult to assign transitions of NCCN from "dark" infrared states, and from other isotopomers, for which the spectroscopic constants are not sufficiently well known.

The vibrational term diagram is given in Fig. 4. It shows graphically that NCCN is a rather rigid linear molecule. The term values of the k substates within each state increase with increasing k .

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