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# Fractionation Factors for the Aqueous Hydroxide Ion and Solvent Isotope Effects on the Ionisation of 1,8-Bis(dimethyamino)naphthalene (Proton Sponge)

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Isotopic fractionation factors  $\phi_a$  and  $\phi_b$  for the hydroxy hydrogen and hydrogen-bonded water hydrogens of the solvated hydroxide ion are important in controlling solvent isotope effects upon reactions involving the hydroxide ion, and were required for a vibrational analysis of the solvated ion. The product  $\phi_a \phi_b^3 = 0.434$  is accurately available from e.m.f. measurements corrected for free energies of ion transfer between H<sub>2</sub>O and D<sub>2</sub>O, but separation of  $\phi_a$  and  $\phi_b$ , which requires measurements in H<sub>2</sub>O-D<sub>2</sub>O mixtures, is known to be subject to considerable uncertainty. Thus careful measurements with 1,8-bis(dimethylamino)naphthalene gave  $K_{D_{10}}/K_{H_{10}} = 0.420 \pm 0.006$  for the ratio of basic ionisation constants in H<sub>2</sub>O-D<sub>2</sub>O gave an ionisation constant too small to be consistent with any reasonable fractionation factor model for the hydroxide ion. Alternative methods of dissecting  $\phi_a$  and  $\phi_b$ , from measurements of isotope separation factors between hydroxide solutions and water vapour and autoprotolysis constants of H<sub>2</sub>O-D<sub>2</sub>O mixtures, are critically reviewed and optimum values are assessed. The results are shown to be sensitive to experimental error and to medium effects but not to departures from the Rule of the Geometric Mean.

SOLVENT isotope effects offer a valuable tool for the investigation of acid- and base-catalysed reactions.<sup>1-7</sup> However, their interpretation requires an understanding of the isotopic fractionation of the hydronium ion and hydroxide ion, and while for the hydronium ion this understanding has been largely achieved,<sup>7-11</sup> for the hydroxide ion in important respects it is still lacking. In 1967 Gold and Lowe made the useful suggestion that contributions to hydroxide isotope effects should be considered as arising both from the hydrogen of hydroxide itself and from three hydrogens hydrogen-bonded in its



primary solvation shell (1).<sup>12</sup> Writing fractionation factors for these hydrogens  $\phi_a$  and  $\phi_b$ , where  $\phi$  denotes the D: H ratio at the hydrogen site relative to that of the bulk solvent in mixed isotopic solutions, the net contributions to kinetic and equilibrium isotope effects involving the hydroxide ion become  $\phi_a \phi_b^3$  in D<sub>2</sub>O and  $(1 - x + x \phi_a)(1 - x + x \phi_b)^3$  in a H<sub>2</sub>O-D<sub>2</sub>O mixture of atom fraction x.

In principle  $\phi_a$  and  $\phi_b$  may be determined by combining suitable measurements in pure and mixed isotopic solvents; for example, the autoprotolysis constants of H<sub>2</sub>O, D<sub>2</sub>O, and H<sub>2</sub>O-D<sub>2</sub>O mixtures corrected for isotopic fractionation of the hydronium ion.<sup>6,12,13</sup> In practice separation of  $\phi_a$  and  $\phi_b$  is subject to certain difficulties which have been discussed by Gold and Grist <sup>13</sup> and by Taylor and Tomlinson.<sup>14</sup> On the one hand the separation is highly sensitive to errors; on the other, for a given value of  $\phi_a \phi_b^3$ , two solutions for  $\phi_a$  and  $\phi_b$  are obtained.<sup>13-15</sup>

The first difficulty is the subject of this paper. Existing data for evaluating  $\phi_a$  and  $\phi_b$  are analysed, and experimental measurements of the ionisation of 1,8-bis-(dimethylamino)naphthalene <sup>16</sup> [equation (1)] in H<sub>2</sub>O, D<sub>2</sub>O, and 1: 1 H<sub>2</sub>O-D<sub>2</sub>O are described. The measurements were undertaken with the object of providing new values of  $\phi_a$  and  $\phi_b$ , although, as will be seen, they serve to underline the problems of effecting a separation. The second difficulty is examined in the accompanying paper,<sup>17</sup> where an attempt is made to distinguish alternative solutions using calculations based upon vibrational analyses of a model for the solvated hydroxide ion.



EXPERIMENTAL

Materials.—1,8-Bis(dimethylamino)naphthalene (Aldrich Chemical Co.) was purified by sublimation. Deionized water was purified further by distillation from alkaline permanganate;  $D_2O$  (Merck; 99.7 atom % D) was used as received. Both  $H_2O$  and  $D_2O$  were made  $CO_2$ -free just prior to use by boiling for a few minutes followed by cooling under protection by Ascarite. Sodium hydroxide stock solutions (ca. 0.1M) were prepared from NaOH and either  $H_2O$ ,  $D_2O$ , or  $1:1H_2O-D_2O$ ; the latter was made by mixing equal volumes of  $H_2O$  and  $D_2O$ . Exact hydroxide ion concentrations of these stock solutions were determined by acidimetric titration. More dilute sodium hydroxide solutions were prepared by diluting stock solutions by weight.

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 $pK_a$  Determinations.—These were carried out spectrophotometrically by making measurements at 335 nm where the free base, 1,8-bis(dimethylamino)naphthalene, absorbs strongly and its conjugate acid does not absorb at all. A Cary model 118C spectrometer was used, and its cell block was thermostatted at  $25.0 + 0.1^{\circ}$  despite the fact that changes in temperature of as much as 1° were found to have no perceptible effect on absorbance. Measurements were made in 1 cm cuvettes; the very limited solubility of 1,8bis(dimethylamino)naphthalene in water required use of the 0-0.1 spectrometer absorbance scale, but readings could nevertheless easily be made to 0.001 absorbance unit or better

In a typical experiment, 3 ml of sodium hydroxide solution of the appropriate concentration was pipetted into the cell. After this had come to temperature equilibrum with the spectrometer cell compartment, the base line was adjusted and a fixed amount, usually 100  $\lambda$ , of stock 1,8bis(dimethylamino)naphthalene solution (H<sub>2</sub>O, D<sub>2</sub>O, or  $H_2O-D_2O$ ) was added. The resulting mixture was shaken and an absorbance reading was taken. This procedure was repeated three times for each sodium hydroxide concentration.

The ratio of unprotonated to protonated 1,8-bis(dimethylamino)naphthalene was calculated using the relationship  $[B]/[BH^+] = (A - A_{BH^+})/(A_B - A); A_B$  was measured in concentrated (1.3M) sodium hydroxide solution and  $A_{\rm BH^+}$ was taken to be zero.

#### RESULTS

The determinations were made at ionic strengths fixed by the sodium hydroxide concentrations, which were both appreciable and variable (see Table 1). The data were therefore extrapolated to infinite dilution; this was done as follows.

The thermodynamic or infinite dilution ionization constant for reaction (2) under investigation is given by

$$B + L_2 O \longrightarrow BL^+ + LO^-$$
(2)

equation (3) in which parentheses denote molar activities,

$$K_{\rm b} = \frac{({\rm BL}^+)({\rm LO}^-)}{({\rm B})} = \frac{[{\rm BL}^+][{\rm LO}^-]_{y^+y^-}}{[{\rm B}]}$$
(3)

square brackets denote molar concentrations, and  $y^+$  and  $y^{-}$  are the molar activity coefficients of the BH<sup>+</sup> and LO<sup>-</sup> ions respectively. (The symbol L is used to signify either H or D.) The activity coefficient of the neutral base was taken to be unity, while those of the ions were assumed to depend on ionic strength,  $\mu$ , in the manner shown by equation (4) where  $B_{\pm}$  are specific ion interaction constants.

$$\log y_{\pm} = \frac{-0.5\sqrt{I}}{1+\sqrt{I}} + B_{\pm}I$$
 (4)

Combination of equations (3) and (4) gives an expression. which upon taking logarithms and making the substitutions  $pK_e = -\log[BL^+][OL^-]/[B]$  and  $pK_b = -\log K_b$  leads to equation (5). This expression shows that  $pK_b$  may be

$$pK_{c} + \frac{\sqrt{I}}{1 + \sqrt{I}} = pK_{b} + (B_{+} + B_{-})I$$
 (5)

obtained as the intercept of a linear plot of  $[pK_e + \sqrt{I}]$  $(1 + \sqrt{I})$ ] versus  $\sqrt{I}$ .

Least-squares analysis of the data listed in Table 1 gave

#### TABLE 1

Ionization constant measurements for 1,8-bis(dimethylamino)naphthalene in aqueous solution at 25°

0.

the following results,  $pK_b$  1.973  $\pm$  0.003 in H<sub>2</sub>O, 2.395  $\pm$ 0.005 in  $D_2O_1$ , and 2.181  $\pm$  0.006 in 1 : 1  $H_2O_2O_2$ . These translate into the following thermodynamic basicity constants,  $K_{\rm H_{2}O}$  (1.064 ± 0.007) × 10<sup>-2</sup>,  $K_{\rm D_{2}O}$  (0.403 ± 0.005) × 10<sup>-2</sup>, and  $K_{\rm HDO}$  (0.659 ± 0.009) × 10<sup>-2</sup> mol l<sup>-1</sup>, and give the following isotope effects,  $K_{\rm H_2O}/K_{\rm D_2O}$  2.64  $\pm$  0.04 and  $K_{\rm H_{*}O}/K_{\rm HDO}$  1.61  $\pm$  0.03.

The value  $pK_{\rm b}$  1.97 for H<sub>2</sub>O solution may be converted into  $pK_a$  12.03 by subtraction from  $pK_w$  (=14.00). The result obtained is in good agreement with  $pK_{a}' 12.1 \pm 0.1$ measured at an ionic strength of 0.1M,<sup>18</sup> and is consistent with  $pK_a$  12.34 reported for an unspecified ionic strength.<sup>16</sup>

Fractionation Factor Determination.-The D: H fractionation factor for the acidic hydrogen of monoprotonated 1,8bis(dimethylamino)naphthalene was determined by dissolving the unprotonated substrate in an acidic (0.2Mhydrochloric acid) H<sub>2</sub>O-D<sub>2</sub>O solution of known deuterium content and then measuring the area of the n.m.r. signal from the acidic proton located at  $\delta$  19.5. (Under these conditions, exchange of this hydrogen with the solvent is slow on the n.m.r. time scale.) This signal area was

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translated into protium content by comparison with the area of the nearest other n.m.r. signal of the protonated substrate, that from the six non-exchanging aromatic hydrogens located at about  $\delta$  8. Since these two signals were still more than 10 p.p.m. apart, the comparison was done stepwise using glacial acetic acid as an external reference, *i.e.* the area of the substrate acidic hydrogen signal was compared with that of the hydroxy-group signal from acetic acid and the area of the substrate aromatic hydrogens signal was compared with that from the methyl group of acetic acid reference, which added to the hydroxy-group signal, was taken into account by determining the ratio of hydroxy to methyl group signal areas separately. The results, summarized in Table 2, give  $\phi_{\rm P}$  0.901  $\pm$  0.014.

#### TABLE 2

Measurements of the fractionation factor  $\phi_P$  for the N-H<sup>+</sup> hydrogen of protonated 1,8-bis(dimethylamino)naphthalene

| [Substrate]/M | D : H atom ratio |           |                   |  |
|---------------|------------------|-----------|-------------------|--|
|               | Solvent          | Substrate | φ <sub>P</sub>    |  |
| 0.73          | 0:908            | 0.779     | 0.858             |  |
| 0.53          | 0.933            | 0.894     | 0.959             |  |
| 0.43          | 0.944            | 0.845     | 0.896             |  |
| 0.28          | 0.963            | 0.852     | 0.885             |  |
| 0.20          | 0.973            | 0.869     | 0.893             |  |
| 0.20          | 0.973            | 0.890     | 0.915             |  |
|               |                  | Average   | $0.901 \pm 0.014$ |  |

#### DISCUSSION

Measurements in  $D_2O$ .—In evaluating fractionation factors for the hydroxide ion it is convenient to consider measurements in  $D_2O$  and  $H_2O-D_2O$  mixtures in turn. In pure isotopic solvents the ratios  $K_{D_2O}/K_{H_2O}$  for equilibria involving hydroxide ion yield products of fractionation factors: in terms of model (1),  $\phi_a\phi_b^3$ , or, more generally,  $\prod \phi_i$ . The general expression makes no

assumption about the number of fractionating hydrogens and includes a term for medium effects, denoted  $\Phi_{\rm s}$  by Albery,<sup>6</sup> representing fractionation effects too small to distinguish individually and commonly associated with ionic solvation; this term may also be considered as the activity coefficient counterpart of free energies of transfer between H<sub>2</sub>O and D<sub>2</sub>O.<sup>15,19</sup> In this paper the results are discussed in terms of model (1) with alternative possibilities noted as appropriate.

(a) Autoprotolysis and electrochemical measurements. Before considering the measurements for 1,8-bis(dimethylamino)naphthalene it is pertinent to consider previous determinations of  $\phi_a \phi_b^3$ , and most importantly those from measurements of the ratio of autoprotolysis constants of H<sub>2</sub>O and D<sub>2</sub>O,  $K_W H_{2}O/K_W D_{2}O.12, 20-23$  The ratio of autoprotolysis constants may be considered as an effective equilibrium constant for the isotope exchange (6), and  $\phi_a \phi_b^3$  may be obtained from  $(K_W D_{2}O)$ 

$$\begin{array}{c} {\rm H_{3}O^{+} + HO^{-}(H_{2}O)_{3} + 5D_{2}O \clubsuit} \\ {\rm D_{3}O^{+} + DO^{-}(D_{2}O)_{3} + 5H_{2}O} \end{array} \tag{6}$$

 $K_{\rm W}^{\rm H_{4}O}/l^3$ , where *l* is the fractionation factor for the hydronium ion, that is  $L^{-1/6}$  where in turn *L* is the

equilibrium constant for the exchange reaction (7). Determination of  $\phi_a \phi_b^3$  thus requires a knowledge of L.

$$2D_3O^+ + 3H_2O \implies 2H_3O^+ + 3D_2O$$
 (7)

What is probably the best method of evaluating L has been summarised by Salomaa and Aalto.<sup>7</sup> E.m.f. data for the electrochemical cells comprising hydrogen and silver-silver chloride electrodes in H<sub>2</sub>O and D<sub>2</sub>O are combined to give  $\Delta \bar{G}^0$  for reaction (8). Further combination with measurements of the equilibrium constant

$$\frac{1}{2}D_2 + HCl(H_2O) \Longrightarrow \frac{1}{2}H_2 + DCl(D_2O) \quad (8)$$

of reaction (9) and the free energy of transfer of chloride

$$D_2 + H_2O(l) \Longrightarrow H_2 + D_2O(l)$$
(9)

ions between  $H_2O$  and  $D_2O$  [reaction (10)], yields L.

$$D_2O + Cl^-(H_2O) \Longrightarrow Cl^-(D_2O) + H_2O \quad (10)$$

Of the data used by Salomaa and Aalto the e.m.f. values of Gary *et al.*<sup>24</sup> are still applicable, but improved measurements for reactions (9) and (10) are now available. For the isotope exchange between hydrogen gas and water (9), Rolston, *et al.* have made measurements at low atom fractions of deuterium <sup>25</sup> to obtain 3.81 as equilibrium constant at 25° for the exchange (11), which, when combined with K 3.26 for the disproportionation constant of HD (12), calculated from Bron

$$HD + H_2O(l) \rightleftharpoons H_2 + HDO(l) \qquad (11)$$
$$2HD \rightleftharpoons H_2 + D_2 \qquad (12)$$

et al.'s convenient tabulation of isotopic partition function ratios and their temperature dependence,<sup>26</sup> and 3.80 for the disproportionation constant of HDO (13), based on the average of gas phase measurements<sup>27</sup>

$$2HDO \Longrightarrow H_2O + D_2O \tag{13}$$

corrected to the liquid state,<sup>28</sup> gives an equilibrium constant for (9) of 12.39.

Taking Voice's measurement of 172 cal mol<sup>-1</sup> for sodium chloride as the molar transfer free energy of the chloride ion <sup>29</sup> gives L 9.85, which differs little from Salomaa and Aalto's original value of 9.0 and agrees well with Gold's n.m.r. determination <sup>9</sup> of 9.7 and Heinzinger and Weston's <sup>7,10,30</sup> value of 9.6 from measurements of isotope separation factors between aqueous perchloric acid solutions and water vapour, although the last value is for 13.5 °C and would be smaller (*ca.* 9.0) at 25°. The data also allow calculation of the temperature dependence of L between 0 and 50° as equation (14), where

$$\Delta \bar{G}^0 = -3\,126 - 14.08T + .02724T^2 \quad (14)$$

 $\Delta \bar{G}^0$  is the standard molar free energy change for reaction (7) in cal mol<sup>-1</sup> and T is in degrees Kelvin.

The value of  $L^{1/2}$  may now be combined with one of the recent measurements of  $K_W^{H_2O}/K_W^{D_2O}$ ,  $^{12,20-23}$  of which those of Gold and Lowe  $^{12}$  and Covington *et al.*<sup>20</sup> are perhaps the most satisfactory.<sup>31</sup> From Gold and Lowe's value of 7.28 at 25° one obtains  $\phi_a \phi_b^3$  0.431. A similar combination using the value of Covington *et al.*  however, leads to a cancellation of redundant terms because common e.m.f. data are used for the calculations of  $K_{W}^{H_{2}O}/K_{W}^{D_{2}O}$  and L. Most directly  $\phi_{a}\phi_{b}^{3}$  is obtained from e.m.f. measurements for the cell H<sub>2</sub>,NaOH,NaCl-(H<sub>2</sub>O),AgCl;Ag<sup>32</sup> and its D<sub>2</sub>-D<sub>2</sub>O counterpart.<sup>20</sup> E.m.f.s corresponding to the net reaction (15) have been

$$\frac{1}{2}D_2 + \text{NaOD}(D_2O) + \text{NaCl}(H_2O) + H_2O = \frac{1}{2}H_2 + \text{NaOH}(H_2O) + \text{NaCl}(D_2O) + D_2O \quad (15)$$

listed by Goldblatt and Jones,<sup>21</sup> and combination with  $\Delta \bar{G}^0$  for the D<sub>2</sub>-water exchange (8) and the transfer free energy of chloride ions (10) yields at 25°  $\phi_a \phi_b^3 0.434$ , which compares satisfactorily with Goldblatt and Jones's own measurement at 25° giving  $\phi_a \phi_b^3 0.444$ . It should be noted that these values contain a, probably very small, contribution from the transfer free energy of sodium ions.

From the e.m.f. measurements <sup>21,23</sup> the temperature dependence of  $\phi_a \phi_b{}^3$  may be calculated as equation (16),

$$\Delta \bar{G}^0 = -820 - 0.456T + 0.000\ 56T^2 \quad (16)$$

where  $\Delta \bar{G}^0 = 2RT \ln (\phi_a \phi_b^3)$  [or, more generally,  $2RT \ln (\prod_i \phi_i)$ ] is the standard molar free energy change for reaction (17) in which the hydroxide ion is written

$$2\mathrm{DO}^{-} + \mathrm{H}_{2}\mathrm{O} \Longrightarrow 2\mathrm{HO}^{-} + \mathrm{D}_{2}\mathrm{O} \qquad (17)$$

formally without its solvation shell. At  $25^{\circ}$  the equilibrium constant for this reaction is 5.31.

(b) Ionisation of 1,8 bis(dimethylamino)naphthalene. For 1,8-bis(dimethylamino)naphthalene the ratio of basic ionisation constants in  $D_2O$  and  $H_2O$  may be written in terms of fractionation factors as equation (18), where  $\phi_P$  refers to the ionising hydrogen of the protonated

$$K_{\mathrm{D}_{a}\mathrm{O}}/K_{\mathrm{H}_{a}\mathrm{O}} = \phi_{a}\phi_{b}{}^{3}\phi_{\mathrm{P}}\Phi_{\mathrm{S}} \tag{18}$$

base [cf. equation (1)] and  $\Phi_{\rm S}$  is the contribution of medium effects arising from transfer of free and protonated base from H<sub>2</sub>O to D<sub>2</sub>O.<sup>6</sup> Since ionisation occurs at concentrations of hydroxide ion (0.1-0.001M) determinable by titration or dilution no correction is required for the difference of pH from pD. The measured values of  $K_{\rm H_2O}/K_{\rm D_2O}$  and  $\phi_{\rm P}$  were 2.64  $\pm$  0.04 and 0.901  $\pm$  0.014, respectively

Because  $\Phi_8$  is unknown  $\phi_a \phi_b^3$  cannot in this case be determined directly. However, with  $\phi_a \phi_b^3 0.434$ , we obtain  $\phi_8 1.03$ , and it becomes possible to make transfer corrections and derive values of  $\phi_a$  and  $\phi_b$  from measurements in H<sub>2</sub>O-D<sub>2</sub>O mixtures. The nearness of  $\Phi_8$  to 1.0 suggests cancellation of transfer free energies between free and pronated base (plausibly because hydrogen bonding between the ionising species and solvent is weak), and this small correction for medium effects should be an advantage in evaluating  $\phi_a$  and  $\phi_b$ .

Measurements in  $H_2O-D_2O$  Mixtures.—To obtain  $\phi_a$ and  $\phi_b$  separately the value of  $\phi_a \phi_b{}^3$  must be combined with suitable measurements in  $H_2O-D_2O$  mixtures. Again, previous measurements may be reviewed before considering results for 1,8-bis(dimethylamino)naphthalene.

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(a) Liquid-vapour isotope separation factors. Weston and Heinzinger measured the fractionation of H and D isotopes between liquid water and aqueous hydroxide solutions and water vapour.<sup>33</sup> Their measurements yield  $(1 - \phi_a) + 3(1 - \phi_b)$  or, in model independent terms,  $\sum_{i} (1 - \phi_i)$ , where again the  $\phi_i$  may include a contribution from a medium effect  $\Phi_s$ . The relationship of

fractionation factors to experimentally measured parameters is expressed by equation (19) where N is the mole

$$\sum_{i} (1 - \phi_i) - \ln \Phi_{\rm S} = \frac{2 - N}{N} (1 - \alpha_{\rm B}/\alpha_{\rm W}) \quad (19)$$

fraction of NaOH or KOH,  $\alpha_{\rm B}$  and  $\alpha_{\rm W}$  are the liquidvapour D-H separation factors for base solution and pure water respectively, and  $-\ln \Phi_{\rm S}$  separates medium from specific fractionation effects.\* The separation factors are defined by  $\alpha = x_{\rm V}(1 - x_{\rm L})/x_{\rm L}(1 - x_{\rm V})$  where x is the atom fraction of deuterium and the subscripts L and V denote liquid and vapour. Values of  $\sum_{i} (1 - \phi_i)$ are shown in Table 3.

TABLE 3

 $\sum_{i} (1 - \phi_i)^{a}$  for the hydroxide ion from Heinzinger and Weston's isotope separation measurements <sup>b</sup>

| Base |       | $(1 - \phi_i)^d$                      |             |                    |       |  |
|------|-------|---------------------------------------|-------------|--------------------|-------|--|
|      | N     | $\alpha_{\rm B}/\alpha_{\rm W}^{\ c}$ | Uncorrected | Corrected <i>f</i> | σε    |  |
| NaOH | 7.84  | 0.9638                                | 0.442       | 0.442              | 0.021 |  |
| NaOH | 10.20 | 0.9567                                | 0.480       | 0.480              | 0.010 |  |
| NaOH | 12.12 | 0.9472                                | 0.486       | 0.486              | 0.014 |  |
| КОН  | 6.99  | 0.9626                                | 0.573       | 0.519              | 0.011 |  |
| КОН  | 10.30 | 0.9456                                | 0.543       | 0.489              | 0.008 |  |

<sup>*a*</sup> For model (1),  $4 - \phi_a - 3\phi_b$ . <sup>*b*</sup> Ref. 33. <sup>*c*</sup> Ratio of isotope separation factors between base solution and water vapour  $(\alpha_B)$  and liquid water and water vapour  $(\alpha_W)$ . <sup>*d*</sup>  $(2-N)(1-\alpha_B/\alpha_W)/N$ . <sup>*d*</sup> Average deviation. <sup>*f*</sup> The measurements for KOH are corrected for the difference in free energies of transfer of Na<sup>+</sup> and K<sup>+</sup> ions.

Measurements were made for KOH and NaOH solutions, and their comparison requires a correction to be made for the difference in transfer free energies between potassium and sodium ions,  $\Delta \bar{G}_i^0$ , which from Voice's measurements<sup>29</sup> amounts to 31 cal mol<sup>-1</sup>. Taking  $\ln \Phi_{\rm S} = \Delta \bar{G}_i^0/RT$  and subtracting from  $\sum_i (1 - \phi_i)$  for KOH gives the corrected values shown in the right hand column of Table 3. Agreement between KOH and NaOH measurements is significantly improved.

In a later discussion of the results, Gold and Grist <sup>13</sup> noted that a trend in Heinzinger and Weston's measurements with concentration of base could perhaps be discerned, and suggested extrapolation to zero base concentration. They made no correction, however, for the difference in free energies of transfer of Na<sup>+</sup> and K<sup>+</sup> ions and a linear extrapolation leads to a significantly higher value of  $(1 - \phi_a) + 3(1 - \phi_b)$  without the correction (0.561) than with it (0.490  $\pm$  0.064). Indeed Grist and Gold considered a higher value still (0.656) not inconsistent with the result.

<sup>\*</sup> In terms of fractionation,  $\Phi_{\rm S} = \phi^n$ , where *n* is large and  $\phi \rightarrow 1.0$ . The contribution to  $\sum_i (1 - \phi)$  is thus  $n (1 - \phi) \cong -n \ln \phi = -\ln \Phi_{\rm S}$ .

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Further corrections may be made because the measurements were made at  $13.5^{\circ}$  rather than  $25^{\circ}$  and to take account of departures from the Rule of the Geometric Mean.<sup>6,27</sup> In practise these were found to be so small (2%) as to be sensibly neglected.

Values of  $\phi_a$  and  $\phi_b$  may be obtained by combining Heinzinger and Weston's measurements with  $\phi_a \phi_b{}^3 = 0.434$ . The sensitivity of the values to the precision of the measurements is best shown by plotting  $(1 - \phi_a) + 3(1 - \phi_b)$  against a range of values of  $\phi_a$  with  $\phi_b = \sqrt[3]{0.434/\phi_a}$  as in Figure 1. A smooth curve is obtained



FIGURE 1 Full curve, plot of  $4 - \phi - 3\phi_b$  versus  $\phi_a$  with  $\phi_a \phi_b^3$  0.434. Dashed curve, the same including a medium effect  $\phi$  1.3. The patched area shows an experimental value and standard deviation based on the data of ref. 35. The upper line shows a value from the same data derived by Gold and Grist

with a maximum at  $\phi_a = \phi_b$ , as shown by the full line in Figure 1. The 'observed' value of  $(1 - \phi_a) +$  $3(1 - \phi_b) = 0.490$ , extrapolated to infinite dilution and corrected to 25°, is shown as the horizontal line, with the limits of the standard deviation of its mean indicated by cross hatching. Also shown, as an extreme comparison, is the value favoured by Gold and Grist,<sup>13</sup> which lacks corrections for the difference in transfer free energies of Na<sup>+</sup> and K<sup>+</sup>.

Figure 1 illustrates the two solutions <sup>13,15</sup> associated with measurements of  $(1 - \phi_a) + 3(1 - \phi_b)$ , and Table 4 lists pairs of values of  $\phi_a$  and  $\phi_b$ . The vulnerability of  $\phi_a$  and  $\phi_b$  to errors is indicated by the difference between the values of  $\phi_a$  of 0.39 or 1.54 obtained using the fully corrected results and of  $\phi_a = 0.5$  or 1.24 considered possible by Gold and Grist.<sup>12</sup> While it is now clear that the latter values have a poorer experimental basis, their lesser divergence from 1.0 makes them more consistent with measurements of other OH fractionation factors.<sup>34</sup>

TABLE 4

Fraction factors for the hydroxide ion <sup>a</sup>

| Method<br>Vapour-liquid | Medium<br>effect <sup>δ</sup><br>Φ <sub>8</sub> | Solution 1 |          | Solution 2     |        |
|-------------------------|---|------------|----------|----------------|--------|
|                         |   | - ¢a       | φ        | φ <sub>a</sub> | фь     |
| isotope separation      | 1.0   | 0.39       | 1.04     | 1.54           | 0.26   |
|                         | 1.3   | 0.39       | 0.95     | 1.37           | 0.63   |
|                         | 1.0   | (0.50) *   | (0.95) ° | (1.24) °       | (0.70) |
| Autoprotolysis          |   |            |          |                | • /    |
| constant                | 1.0   | 0.55       | 0.92     | 1.15           | 0.72   |
|                         | 1.3   | 0.58       | 0.83     | 1.00           | 0.69   |

<sup>a</sup> Corrections for deviations from the Rule of the Mean are not included. Normally these amount to <3%. <sup>b</sup> When  $\Phi_8 = 1.0$ , there is no medium effect. <sup>c</sup> Values in parentheses are those suggested by Gold and Grist <sup>13</sup> (see text)

(b) Autoprotolysis measurements. The second source of results suitable for determining  $\phi_a$  and  $\phi_b$  are Gold and Lowe's measurements of the autoprotolysis constant of water in H<sub>2</sub>O-D<sub>2</sub>O mixtures.<sup>12</sup> If  $K_W^x$  is the autoprotolysis constant for a solvent of deuterium atom fraction x,  $K_W^x/K_W^{H_3O}$  may be expressed in terms of fractionation factors as equation (20). Following Albery

$$K_{W}^{x}/K_{W}^{\Pi_{2}O} = (1 - x + xl)^{3}(1 - x + x\phi_{b})^{3}$$

$$(1 - x + x\phi_{a}) \quad (20)$$

and Davies,<sup>35</sup> this expression may be rearranged to a function  $y_x$  isolating terms in  $\phi_a$  and  $\phi_b$  (21). Focusing

$$y_x = \frac{K_W^x / K_W^{H_s O}}{(1 - x + xl)^3} = (1 - x + x\phi_b)^3 (1 - x + x\phi_a) \quad (21)$$

on  $y_x$  at  $x = \frac{1}{2}$  one obtains for  $y_1$  equation (22), or, if a

$$y_{\frac{1}{2}} = \frac{K_{W}^{\frac{1}{2}}}{K_{W}^{H_{2}O}} \frac{8}{(1+l)^{3}} = \frac{(1+\phi_{b})^{3}(1+\phi_{a})}{16} \quad (22)$$

specific model for the hydroxide ion is not used,  $y_{\frac{1}{2}}$  takes the general form of (23).

$$y_{\pm} = \prod (1 + \phi_i)/2$$
 (23)

Solutions of  $\phi_a$  and  $\phi_b$  are obtained as before by plotting  $y_{\frac{1}{2}}$  as a function of  $\phi_a$  for  $\phi_a \phi_b{}^3 = 0.434$  and reading off values of  $\phi_a$  and  $\phi_b$  corresponding to the measured  $y_{\frac{1}{2}}$ . In practice what is plotted in Figure 2 is not  $y_{\frac{1}{2}}$  but the 'percentage curvature' c, representing the deviation from linearity of a plot of  $K_W x/K_W H_{*0}$  against x at x = 0.5, defined by (24) where  $y_1$  is the value of y in pure

$$%c = \left\{1 - \frac{2y_{\frac{1}{2}}}{(1+y_{1})}\right\} \times 100$$
 (24)

 $D_2O$ , *i.e.*  $\phi_a\phi_b^3$  (=0.434). Expressed in this form the precision required of the measurements to define the fractionation factors is directly indicated.

Although Gold and Lowe did not measure  $K_W$  at x = 0.5 directly, the value can be interpolated from their measurements at other values of x. The derived curvature is shown as the horizontal line aa' in Figure 2 and it is apparent that again two solutions exist. The values of  $\phi_a$  and  $\phi_b$  are also listed in Table 4, and it can be seen that compared with Heinzinger and Weston's measurements  $\phi_a$  (0.55 or 1.15) is significantly closer to unity.

It should be mentioned that these results have previously been analysed by Albery's  $\gamma$  method to give  $\gamma$   $0.43\pm0.14.^6$ 

(c) 1,8-Bis(dimethylamino)naphthalene. Ionisation of 1,8-bis(dimethylamino)naphthalene was studied in the expectation that one or other of the previous measurements might be confirmed. The ratio of ionisation constants in 1:1 H<sub>2</sub>O-D<sub>2</sub>O and pure H<sub>2</sub>O,  $K_{\frac{1}{2}}/K_{\text{H}_{4}\text{O}}$  may be written in terms of  $\phi_a$ ,  $\phi_b$ , the fractionation factor of the exchangeable hydrogen of the protonated base,  $\phi_{\text{P}}$ , and a correction ( $\Phi_{\text{S}}$ )<sup> $\frac{1}{2}$ </sup> for the small net medium effect upon transferring free and protonated base from



FIGURE 2 Full curve, percentage deviation from linearity (%c) of a plot of  $(1 - x + x \phi_a)(1 - x + x \phi_b)^3$  versus x at x = 0.5for various  $\phi_a$  with  $\phi_a \phi_b{}^3 0.434$ . Dashed curves, the same including medium effects,  $\Phi 0.434$  (upper curve) or 1.3 (lower curve). The lines represent experimental measurements from autoprotolysis constants (aa') and from the ionisation of proton sponge (bb')

pure  $H_2O$  to the mixed isotopic solvents, as in equation (25). Rearrangement then gives the same expression

$$\frac{K_{\frac{1}{2}}}{K_{\mathrm{H},0}} = \frac{(1+\phi_a)(1+\phi_b)^3(1+\phi_{\mathrm{P}})\Phi_{\mathrm{S}}^{\frac{1}{2}}}{32} \quad (25)$$

for  $y_{\frac{1}{2}}$  in terms of fractionation factors  $\phi_a$  and  $\phi_b$  as from the autoprotolysis measurements, *i.e.* equation (26). It

$$y_{\pm} = \frac{K_{\pm}}{K_{\rm H_4O}} \times \frac{2}{(1+\phi_{\rm P})\Phi_{\rm S}^{\pm}} = \frac{(1+\phi_b)^3(1+\phi_a)}{16} \quad (26)$$

follows that if the curvature,  $\frac{6}{6}c$ , is calculated  $\phi_a$  and  $\phi_b$  may be read from Figure 2, as before.

For the observed values of  $K_{\rm H_2O}/K_{\rm 2}$  1.61<sub>5</sub>,  $\phi_{\rm P}$  0.90 and  $\Phi_{\rm S}$  1.03, the curvature for  $y_1$  0.434 is 7.7  $\pm$  1.6%,

and this is included in Figure 2 as the line bb'. Thus, far from confirming previous values of  $\phi_a$  and  $\phi_b$  the departure of  $K_x/K_{\rm II}$  from a linear dependence upon the atom fraction of deuterium x at x 0.5 actually exceeds the maximum theoretical value of 6.1% consistent with our model (1) for the hydroxide ion!

In view of the small range of allowed curvatures for 1,8-bis(dimethylamino)naphthalene we may ask whether the measurements are sensitive to small corrections hitherto neglected. It is shown in an Appendix that there is little influence from deviations from the Rule of the Mean, but the measured curvature can be reproduced if the fractionation model for the hydroxide ion is modified to include a sufficiently large medium effect. Thus if the effect of transferring a hydroxide ion from  $H_2O$  to  $D_2O$  is denoted  $\Phi_8^{OH}$  we can write  $\phi_a\phi_b{}^{3}\Phi_8^{OH}$  0.434 and equation (22) as (27). Maximum positive

$$y_{\frac{1}{2}} = \frac{(1+\phi_b)^3(1+\phi_a)(\Phi_{\rm S}^{\rm OH})^{\frac{1}{2}}}{16}$$
(27)

curvature results when the isotope effect is entirely a medium effect, and this is shown in the upper dashed curve of Figure 2, for which  $\Phi_{\rm S}^{\rm OH} = 0.434$ . However, values consistent with the experimental measurement, represented by the line bb' are only just achieved and since the medium effect accounts only for fractionation effects beyond the four innermost hydrogens of the solvated hydroxide ion it is unlikely to be as strong as would be required.\*

Conclusions.—Almost certainly the discrepancy for 1,8-bis(dimethylamino)naphthalene, and indeed between Gold and Grist's and Heinzinger and Weston's measurements, reflects an intrinsic difficulty in separating sets of fractionation factors from measurements of the curvature of plots of  $K_x/K_{\rm H}$  against x when solutions occur in an insensitive range, even when, as here, the measurements are made with considerable care. This is particularly true when a plot of curvature as a function of  $\phi$  has an extremum close to its solutions as in Figure 2. Thus despite the large difference in solutions of  $\phi_a$  and  $\phi_b$  implied, the values of  $y_{\frac{1}{2}}$  on which the curvatures of the autoprotolysis measurements and ionisation of proton sponge are based differ by only 5%.

Probably the most reliable values of  $\phi_a$  and  $\phi_b$  are those based on Heinzinger and Weston's measurements,<sup>33</sup> *i.e.*  $\phi_a 0.39$  and  $\phi_b 1.04$  or  $\phi_a 1.54$  and  $\phi_b 0.66$ , but the more moderate values from Gold and Lowe's autoprotolysis measurements <sup>12</sup> appear more reasonable.<sup>†</sup> Our own results may add weight to values of  $\phi_a$  close to unity, but Taylor and Tomlinson's n.m.r. measurements of hydroxide solutions in H<sub>2</sub>O-D<sub>2</sub>O mixtures, while not yielding values of  $\phi_a$  and  $\phi_b$  directly, suggest the contrary.<sup>14</sup> The combined measurements reflect the recognised uncertainty of the individual values of  $\phi_a$  and  $\phi_b$ .

Nevertheless, 'moderate' solutions for  $\phi_a$  and  $\phi_b$  are implied by the calculations of the following paper, and it is worth examining further the sensitivity of the

† The more limited autoprotolysis data in  $H_2O-D_2O$  mixtures of Pentz and Thornton <sup>22</sup> give  $\phi_a$  0.44 or 1.45.

<sup>\*</sup> The value of Albery's  $\gamma \simeq -0.3$  also indicates the poor fit to the hydroxide model;  $\gamma = 0$  corresponds to the whole isotope effect being a medium effect.

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measurements to medium effects. The dashed curve of Figure 1 and the lower dashed curve of Figure 2 incorporate mild medium effects of  $\Phi_{s}^{OH}$  1.3, and it can be seen from the Figures and from Table 4 that for the solution with  $\phi_a > 1.0$ ,  $\phi_a$  is significantly reduced: for the isotope separation measurements, from 1.54 to 1.37. A similar effect is produced by a minor fractionation contribution from the three outer hydrogens of the water molecules in the hydroxide solvation shell (1), *i.e.* with  $\phi^3$  1.3.

With  $\Phi_{s}^{OH}$  1.3 the medium effect on  $\phi_a$  for the second solution of  $\phi_a$  and  $\phi_b$  is small. This solution is sensitive to additional fractionation but more so to a single fractionation site than to a medium effect which, in terms of a structural model, seems less likely.

It is perhaps regrettable that a more precise dissection of  $\phi_a$  and  $\phi_b$  and potential medium effects is not possible. How critical this is to the interpretation of kinetic measurements in H<sub>2</sub>O-D<sub>2</sub>O mixtures will be examined in a further paper. For the present the distinction between the two solutions for  $\phi_a$  and  $\phi_b$  is sufficient to offer a basis for the calculations of the following paper.

#### APPENDIX

Deviations from the Rule of the Mean.—Values of  $y_{k}$  for proton sponge may be corrected for deviations from the Rule of the Mean as follows. It is assumed, and the results of the following paper confirm, that corrections for water molecules in the solvation shell of the hydroxide ion cancel with those of solvent water molecules. Corrections then arise only for the hydrogens of OH<sup>-</sup> itself and of the solvent water molecule that in the ionisation equilibrium (1) is the counterpart of the hydroxide ion and the fractionating hydrogen of proton sponge.

Adapting Albery and Davies' procedure,36 the simple expression for  $y_{k}$  of equation (26) is modified by multiplying  $(1 + \phi_b)^3 (1 + \phi_a)/16$  by the term  $[1 - 0.25(3\delta_{ab} - 2\delta_{HDO})]$ , in which the  $\delta$  values are correction factors representing interactions of fractionating hydrogens attached to a common atom 11 which enter as differences of contributions between reactants and product;  $\delta_{\text{HDO}} = 1 - K/4$ , where K is the equilibrium constant for disproportionation of HDO to  $H_2O$  and  $D_2O$  (13), corrects for interaction of the two hydrogens of a water molecule, and  $3\delta_{ab}$ , defined in the following paper,<sup>17</sup> corrects for interaction of the hydroxide hydrogen a with the three neighbouring hydrogens of its solvation shell. For reaction in an H2O-D2O mixture of atom fraction x the corrections enter as  $\delta x(1-x)$  and for 1:1 H<sub>2</sub>O–D<sub>2</sub>O, for which x = 0.5, as  $0.25\delta^{.36}$ 

The magnitudes of the corrections reflect the bending force constants between the bonds to the interacting atoms, and calculations  $^{17}$  suggest that the value of  $\delta_{ab}$  depends on which solution is adopted for  $\phi_a$  and  $\phi_b$ , since larger values of  $\phi_q$  are associated with larger hydrogen bond bending force constants for the hydroxy group. For  $\phi_a$  1.2–1.5,  $3\delta_{ab}$  approaches  $\delta_{\rm HDO}/2$  and the correction largely cancels with that for a water hydrogen, while for  $\phi_a < 0.6 \, \delta_{ab}$  is small and the hydroxy-group is sensibly treated as an isolated fractionating hydrogen  $(\delta_{ab} 0)$ . The latter case leads to the larger correction and with  $\delta_{\text{HDO}}$  0.05,  $v_{k}$  is now given by equation (28). However, the corrected value of

$$y_{\frac{1}{2}} = \frac{K_{\text{HDO}}}{K_{\text{H}_2\text{O}}} \times \frac{1.975}{(1 - \phi_{\text{R}})\Phi_{\text{S}}^{\frac{1}{2}}}$$
 (28)

the curvature is 8.9% which differs little from the uncorrected value of  $7.7\frac{0}{10}$ . The magnitude of the correction is thus quite small, and its direction is such as to increase rather than decrease the discrepancy between observed and allowed values.

Similar correction of the autoprotolysis measurements introduces an interaction term  $\delta_{H,DO}$  for the hydronium ion, as shown in equation (29). From model calculations <sup>37</sup>  $\delta_{\rm H_{*}DO} \simeq \frac{3}{4} \delta_{\rm HDO}$ , which with  $\delta_{\rm HDO}$  0.05, gives a value close to

$$\frac{K_{\rm W}^{1}}{K_{\rm W}^{\rm H_2O}} = (1 + \phi_a)(1 + \phi_b)^3(1 + l)^3 \\ \{1 - 0.25(3\delta_{ab} + 3\delta_{\rm H_2DO} - 2\delta_{\rm HDO})\}$$
(29)

the measured value of  $\delta$  0.03 for NH<sub>3</sub>.<sup>38</sup> For the solution of the hydroxide fractionation factors with  $\phi_a < 1.0$  $(\delta_{ab} = 0)$  the corrections cancel, while for  $\phi_a > 1.0$  the curvature is reduced slightly, from 3.8 to 3.2%. Again the correction is very small.

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