# Reactions of Tropone Tosylhydrazone Sodium Salt with Anthracene, 1,3-Diphenylisobenzofuran, and Phenylacetylene: [2+2] and [4+2] Type Cycloaddition Reactions of Cycloheptatrienylidene or 1,2,4,6-Cycloheptatetraene

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(Received December 3, 1984)

The reaction of tropone tosylhydrazone sodium salt (1) with anthracene gave a [4+2]-type adduct and the reaction of 1 with 1,3-diphenylisobenzofuran afforded endo- and exo-[4+2]-type adducts as well as a heptafulvene derivative. The reaction of 1 with phenylacetylene yielded a [2+2]-type adduct, which rearranged into 2-phenylindene upon heating. The addition reactions are thought to proceed via the allene intermediate, 1,2,4,6-cycloheptatetraene, which is a valence-bond isomer of the carbene intermediate, cycloheptatrienylidene, initially generated by the pyrolysis of 1. The photoreaction of adduct 3 with a high-pressure mercury lamp afforded a ring-closure product via the photobicyclization reaction of the cycloheptatriene moiety of the adduct. Thermal interconversions between the three products of the reaction of 1 with 1,3-diphenylisobenzofuran were investigated.

It is known that tropone tosylhydrazone sodium salt (1) generates the carbene, cycloheptatrienylidene (3a) accompanied by nitrogen gas and sodium p-toluenesulfinate (2) by pyrolysis or photolysis.1) Cycloheptatrienylidene is recognized to be a nucleophilic singlet carbene, due to the contribution of a canonical formula (3b), which is stabilized by the 6  $\pi$ -electrons aromatic system.2 Actually, 3a preferentially reacts with electron-deficient double bonds.<sup>2)</sup> Recently, Jones et al. suggested the possibility of a valence-bond isomerization between the carbene 3a and an allene, 1,2,4,6-cycloheptatetraene (3c), and proved experimentally that 3c rearranged into 3a.3 However, the reverse isomerization, 3a to 3c, has never been found. We have pyrolyzed 1 in the presence of various olefins and we have evidence which suggests the isomerization of 3a to 3c. Here, we wish to report our findings.

# Results

When 1 was allowed to react with anthracene (4) in anhydrous diglyme at  $120\,^{\circ}$ C for  $15\,\text{min}$ , the [4+2]-type adduct 5 was afforded in a yield of 21%. The reaction of 1 with 1,3-diphenylisobenzofuran (6) under the identical conditions gave two [4+2]-type adducts, 7 and 8, accompanied by the heptafulvene derivative 9, in yields of 28, 3, and 4%, respectively. The analogous reaction of 1 with phenylacetylene (10) afforded a [2+2]-type adduct 11 and 2-phenyl-1H-indene (12)4) in yields of 8 and 5%, respectively.

Compound 5 was thermally stable and was recover-

ed quantitatively after heating at 150°C for 40 h, but turned to polymeric materials upon heating at 180°C for 20 h. No change was observed when 7 and 8 were kept at 120°C for 15 min (the conditions of the pyrolysis of 1), but upon heating at 130°C for 25 h, 7 gave 8 and 9 in yields of 6 and 42%, respectively, as well as a 30% yield of recovered 7. Under conditions analogous to the above, 8 afforded 7, 9, and recovered 8 in yields of 2, 20, and 68%, respectively. Upon heating at 120°C for 1 h, 11 rearranged into 12 in a 55% yield. The red oil 9 was unstable and readily decomposed to a resinous material, but catalytic hydrogenation of 9 over palladium-charcoal resulted in the formation of a colorless oil 13 in 96% yield by absorbing 4 molar equivalents of hydrogen.

The irradiation of a methanol solution of 5 using a high-pressure mercury lamp afforded the ring-closure product 14 in a yield of 88%.

The structures of **5**, **7**, and **8** were deduced on the basis of their physical properties and confirmed by a comparison of these properties with those of analogous compounds.<sup>5)</sup> The stereochemistries of **7** (endoadduct) and **8** (exo-adduct) were deduced on the basis of the following arguments. According to Dreiding models,  $H_a$  of **8** ( $\delta$  2.60) and  $H_b$  of **7** ( $\delta$  4.75) are expected to appear in a higher field in the NMR spectra compared to  $H_a$  of **7** ( $\delta$  3.68) and  $H_b$  of **8** ( $\delta$  5.15), because of the diamagnetic anisotropic effects from the o-disubstituted benzene moiety. Furthermore, the chemical shifts of  $H_a$  of **7** ( $\delta$  3.68) and **8** ( $\delta$  2.60) are

Fig. 1.

Fig. 4.

consistent with that of the bridge-head proton of the endo-adduct of **6** with cycloheptatriene ( $\delta$  3.88)<sup>5d)</sup> and that of H<sub>a</sub> of **5** ( $\delta$  2.46), respectively, indicating that each pair of protons is located in nearly the same chemical environment.

The structure of **9** was deduced mainly from its UV spectrum, which is characteristic of heptafulvene derivatives, <sup>6)</sup> and its IR spectrum, which shows a carbonyl band in the same region as that of benzophenone. The absorbing of 4 molar equivalents of hydrogen by **9** to give a stable colorless oil **13** seems to support the structure of **9**. <sup>6d)</sup>

The structure of the photoproduct 14 was deduced

on the basis of the physical properties and confirmed by a comparison of the physical properties with those of the analogous compounds.<sup>7</sup>

### **Discussion**

The mechanism for the formation of 9 from 7 and 8 initially involves the cleavage of the bond at 7-position of the cycloheptatriene moiety of 7 and 8 to give a tropylium cation (15a) or a tropylium radical intermediate (15b), which in turn affords 9 via an ether bond cleavage as shown in Fig. 5. The stability of the tropylium cation and/or the tropylium radical<sup>8)</sup> and

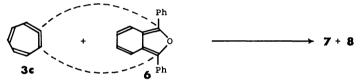




Fig. 6.

the formation of the stable benzophenone moiety can be regarded as the driving force for this reaction.

The isomerization mechanism of 11 to 12 may be explained as follows. The valence-bond isomerization of the cycloheptatriene moiety of 11 gives rise to the norcaradiene structure (16),9) which rearranges to 12 via a hydrogen shift. The analogous reaction mechanism has been proposed for the formation of indane derivatives in the thermal reactions of spiro[2.6]nona-4,6,8-triene derivatives. The photochemical formation of 14 proceeds via the well known 4  $\pi$ -electrons photo-allowed disrotatory cyclization process. 7,11)

Two possible mechanisms may be considered for the reaction of 1 with 4, 6, and 10. Pathway A involves an allene intermediate 3c followed by a [4+2] or [2+2] addition reaction of the allenic double bond of 3c with the appropriate moieties of 4, 6, and 10 to give the corresponding adducts. Pathway B involves the carbene intermediate 3a, which reacts with 4, 6, and 10 to afford the tropylium cation intermediates 17a, 15a, and

18a, respectively, or the tropylium radical intermediates 17b, 15b, and 18b, respectively. Subsequent cyclization reactions of these intermediates lead to the formation of the corresponding products.

A closer examination into pathway B reveals two facts which do not adequately explain the observed products. First, intermediate 3a is a nucleophilic carbene; therefore, the addition of this carbene to 4, 6, and 10 is not favored since these compounds do not contain any electron-defficient double bonds. Second, the yield of the endo-adduct 7 is higher than that of the exo-adduct 8. According to Dreiding model, there is no obvious difference between the steric repulsions in the formation of 7 and 8 from 15. On this basis, 7 and 8 are expected to be formed in an equal yield from 15. The fairly large difference between the yield of 7 and 8 would suggest that the reaction does not proceed via 15. On the other hand, several advantages are envisioned regarding pathway A. Compounds 4 and **6** are known to react readily as  $4\pi$ -components

Fig. 7.

in [4+2]-type addition reactions.<sup>12)</sup> Oda has reported that a cyclic conjugated allene derivative has been allowed to react with **6** to give *endo* and *exo* [4+2]-type adducts in a yield ratio of 5:1, without defining the stereochemistry of the adducts.<sup>13)</sup> The major formation of the *endo*-adduct **7** can be explained as the result of the secondary orbital interaction in the transition state.<sup>11)</sup>

As discussed above, it is difficult to decide whether the carbene intermediate  $\bf 3a$  or the allene intermediate  $\bf 3c$  is involved in the addition reactions, but a plausible pathway for the reaction would involve the allene intermediate  $\bf 3c$ . As for the reaction with  $\bf 10$ , pathway B seems to have still some possibility, because pathway A may involve a thermally forbidden  $[\pi 2s + \pi 2s]$  addition process.  $^{\bf 14}$ )

## **Experimental**

The photoreactions were performed with a 400-W high-pressure mercury lamp, UVL-400P of Riko Kagaku Sangyo Ltd. under a nitrogen stream at room temperature. Thermal isomerizations were carried out in sealed ampoules. All melting points are uncorrected. UV and IR spectra were measured with the Hitachi 220A and DS-701G spectrometers, respectively. Mass spectra were measured with the Hitachi M-52 and JMS-DX300 spectrometers, and the NMR spectra were measured with a Hitachi R-20B or a Varian XL 200 spectrometer with tetramethylsilane as an internal standard. Wako Gel C-200 and activated alumina of Wako Pure Chemical Industries Ltd. were used for column chromatography. Wako Gel B5F was used for thin-layer chromatography.

Reaction of 1 with 4. A mixture of 1 (13.50 g, 46 mmol), 4 (25.00 g, 140 mmol) and anhydrous diglyme (120 ml) was heated at 120 °C for 15 min. After evolution of nitrogen gas had ceased (11, 97%), the gray powder of 2 (7.70 g, 95%) was removed by filtration. The filtrate was extracted with benzene, washed with water, and dried over anhydrous sodium sulfate. After filtration, the solvent was removed on a rotary

evaporator to yield black crystals, which were recrystallized from benzene to give crystals of recovered **4** (21.29 g). The filtrate was chromatographed on silica gel to yield recovered **4** (0.85 g) by pet ether–benzene 9:1 and colorless crystals of **5** (2.57 g, 21%) by pet ether–benzene 8:2. The crystals of **5** were purified by recrystallization from benzene–ethanol. **5**: Mp 135—136 °C. Found: C, 93.80; H, 6.03%. Calcd for C<sub>21</sub>H<sub>16</sub>: C, 93.99; H, 6.01%. Mass m/z (rel intensity): 268 (M+, 95), 191 (23), 178 (100). UV (EtOH): 276 nm (log  $\varepsilon$ , 3.53). IR (KBr): 3030, 1600, 1480 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>)  $\delta$ =2.46 (m, H<sub>a</sub>), 4.47 (d, H<sub>b</sub>), 4.63 (dd, H<sub>c</sub>), 4.78 (s, H<sub>d</sub>), 5.86 (m, H<sub>e</sub>), 6.20 (m, H<sub>f</sub>, H<sub>g</sub>, H<sub>h</sub>), 7.0—7.5 (m, 8H, Ph). Coupling constants in Hz:  $J_{ab}$ =3,  $J_{ac}$ =5,  $J_{ce}$ =10,  $J_{ea}$ =2,  $J_{ef}$ =5.

Reaction of 1 with 6. A mixture of 1 (24.00 g, 80 mmol), 6 (43.00 g, 160 mmol) and anhydrous diglyme (200 ml) was heated at 120°C for 15 min to evolve nitrogen gas (1.71, 96%). After separation of the gray powder of 2 (13.86 g, 96%) by filtration, the filtrate was treated, as usual, to yield a mixture of crystals and an oil. The crystals of recovered 6 (23.60 g) were separated by filtration and the filtrate was chromatographed on alumina to yield colorless crystals 7 (6.20 g) and mixed crystals of 7 and 8 (3.03 g) by pet ether-benzene 3:1 and a red oil 9 (1.15 g, 4%) by ether. The NMR spectrum of the mixed crystals showed that this mixture contained 7 and 8 in a ratio of 2:1. Thus, the yields of 7 and 8 were 8.22 g (28%) and 1.01 g (3%), respectively. Repeated recrystallization from benzene gave pure crystals of 7 and 8. The red oil of 9 was further purified with thin-layer chromatography on silica gel using benzene as a developing solvent  $(R_f=0.60)$ . 7: Mp 189—190°C. Found: C, 90.23; H, 5.43%. Calcd for  $C_{27}H_{20}O$ : C, 89.97; H, 5.59%. Mass m/z (rel intensity): 360 (M+, 100), 255 (87), 105 (82). UV (EtOH): 278 nm  $(\log \varepsilon, 3.44)$ . IR (KBr): 3030, 1600, 1450 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>)  $\delta = 3.68 \, (m, H_a), 4.75 \, (dd, H_b), 5.85 \, (m, H_c), 6.13 \, (m, H_d), 6.20$ (m, H<sub>e</sub>, H<sub>f</sub>), 7.0—7.8 (m, 14H, Ph). Coupling constants in Hz:  $J_{ab}=4$ ,  $J_{ac}=2$ ,  $J_{bc}=10$ ,  $J_{cd}=5$ ,  $J_{de}=11$ . **8**: Mp 177—178 °C. Found: C, 89.62; H, 5.59%. Calcd for C<sub>27</sub>H<sub>20</sub>O: C, 89.97; H, 5.59%. Mass m/z (rel intensity): 360 (M<sup>+</sup>, 45), 255 (100), 105 (55). UV (EtOH): 278 nm ( $\log \varepsilon$ , 3.67). IR (KBr): 3030, 1600, 1450 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>)  $\delta$ =2.60 (m, H<sub>a</sub>), 5.15 (dd, H<sub>b</sub>), 6.05  $(m, H_c), 6.32 (m, H_d), 6.43 (m, H_e, H_f), 7.0-7.8 (m, 14H, Ph).$ 

Coupling constants in Hz:  $J_{ab}$ =4,  $J_{ac}$ =2,  $J_{bc}$ =10,  $J_{cd}$ =5,  $J_{de}$ =11. **9**: Found: C, 90.22; H, 5.61%. Calcd for C<sub>27</sub>H<sub>20</sub>O: C, 89.97; H, 5.59%. Mass m/z (rel intensity): 360 (M<sup>+</sup>, 38), 209 (44), 152 (34), 105 (100). UV (EtOH): 248 nm (log  $\varepsilon$ , 4.32), 332 (3.93). IR (neat): 3030, 1670, 1600 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>)  $\delta$ =5.3—6.5 (m, 6H), 7.0—7.4 (m, 14H, Ph).

Reaction of 1 with 10. A mixture of 1 (5.92 g, 20 mmol), 10 (10.20 g, 100 mmol), and anhydrous diglyme (50 ml) was heated at 120°C for 15 min to evolve nitrogen gas (450 ml, 100%). After separation of the gray powder **2** (3.56 g, 100%), by filtration, the usual workup gave a black oil, which gave recovered 10 (7.69 g) by distillation under a reduced pressure (0.5 Torr<sup>†</sup>, bath temperature 75 °C). The residue was chromatographed on silica gel to give a tarry material (680 mg) by pet ether, which was thin layer chromatographed on silica gel using pet ether as a developing solvent to give crystals of 12 (207 mg, 5%, R<sub>f</sub>=0.45, mp 167—168 °C, lit, 4) 166—167 °C) and a colorless oil of 11 (320 mg, 8%,  $R_1$ =0.40). 11: Found m/z 192.0967. Calcd for C<sub>15</sub>H<sub>12</sub>: 192.0964. Mass m/z(rel intensity): 192 (100), 179 (11), 165 (20), 115 (14). UV (EtOH): 270 nm (log  $\varepsilon$ , 4.23). IR (neat): 3050, 2960, 1660 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>)  $\delta$ =4.71 (m, H<sub>a</sub>), 5.21 (m, H<sub>b</sub>), 5.75 (m, H<sub>c</sub>), 5.8—6.7  $(m, H_d, H_e, H_f), 6.37 (d, H_g), 7.1-7.5 (m, 5H, Ph).$  Coupling constants in Hz:  $J_{ab}=4$ ,  $J_{bc}=10$ ,  $J_{ce}=5$ ,  $J_{gf}=2$ .

Hydrogenation of 9. A solution of 9 (150 mg, 0.42 mmol) in benzene (15 ml) was hydrogenated with palladium–charcoal (30 mg) to absorb hydrogen gas (38 ml, 17 mmol). After filtration, the solvent was removed on a rotary evaporator to yield a colorless oil, which was thin-layer chromatographed on silica gel using benzene as a developing solvent to yield a colorless oil of 13 (146 mg, 96%,  $R_t$ =0.70). 13: Found: C, 87.97; H, 7.43%. Calcd for C<sub>27</sub>H<sub>28</sub>O: C, 88.00; H, 7.66%. Mass m/z (rel intensity): 368 (M<sup>+</sup>, 100), 309 (57), 270 (44), 165 (24). UV (EtOH): 250 nm (log  $\varepsilon$ , 4.31). IR (neat): 3030, 2950, 1673, 1600 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>) δ=1.3—2.4 (two broad peaks, 14H), 7.0—7.4 (m, 14H, Ph).

Thermal Isomerization of 7. A solution of 7 (80 mg) in benzene (0.3 ml) was kept at 130 °C for 25 h in a sealed ampoule. Thin-layer chromatography of the reaction mixture on silica gel using benzene as a developing solvent gave mixed crystals of 7 and 8 (30 mg,  $R_1$ =0.85) and a red oil of 9 (34 mg, 42%,  $R_1$ =0.60). The NMR spectrum of the mixed crystals showed that the crystals contained 7 and 8 in a ratio of 5:1; thus,the yields of 7 and 8 were 25 mg (30%) and 5 mg (6%), respectively.

Thermal Isomerization of 8. A solution of 8 (80 mg) in benzene (0.3 ml) was kept at 130 °C for 25 h. Thin-layer chromatography of the reaction mixture under the same conditions as above gave mixed crystals of 7 and 8 (56 mg) and a red oil of 9 (16 mg, 20%). The NMR spectrum showed that the mixed crystals contained the recovered 7 (54 mg, 68%) and 8 (2 mg, 2%).

Thermal Isomerization of 11. A solution of 11 (40 mg) in benzene (5 ml) was kept at 120 °C for 1 h. After evaporation of the solvent, the reaction mixture was thin-layer chromatographed on silica gel using pet ether as a developing solvent to yield crystals of 12 (22 mg, 55%,  $R_t$ =0.45).

Photoreaction of 5. A solution of 5 (100 mg) in methanol (200 ml) was irradiated with a high-presssure mercury lamp for 2 h. After evaporation of the solvent on a rotary evaporator, the residue was thin-layer chromatographed on

silica gel using pet ether-benzene 8:2 as a developing solvent to yield a colorless oil of **14** (88 mg, 88%,  $R_f$ =0.80). **14**: Found: m/z 268.1227. Calcd for  $C_{21}H_{16}$ : m/z 268.1251. Mass m/z (rel intensity): 268 (14), 178 (100), 151 (7). UV (EtOH) 212 nm (sh, log  $\varepsilon$ , 4.45). IR (neat): 3030, 2980, 1460 cm<sup>-1</sup>. NMR (CDCl<sub>3</sub>)  $\delta$ =2.76 (m,  $H_a$ ), 3.10 (m,  $H_b$ ), 4.19 (s,  $H_c$ ), 4.35 (d,  $H_d$ ), 5.54 (bs,  $H_c$ ,  $H_f$ ), 6.02 (d,  $H_g$ ), 6.28 (d,  $H_h$ ), 7.0—7.3 (m, 8H, Ph). Coupling constants in Hz:  $J_{ab}$ =4,  $J_{ad}$ =3,  $J_{gh}$ =3.

The authors are indebted to Professor Tadashi Sasaki of Nagoya University for his fruitful suggestions. This work was supported by a Scientific Research Grant from the Ministry of Education, Science, and Culture.

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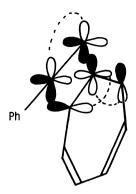


Fig. 8.

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14) It is known that ketenes proceed [2+2]-type concerted addition reactions under thermal conditions, in which ketenes actually react as  $4\pi$  components, forming thermally allowed  $[\pi 4s + \pi 2s]$  addition process. 15) The pathway A for the reaction of 3c with 10 may be considered to be actually a thermally allowed  $[\pi 4s + \pi 2s]$  addition process, in which 3c plays as a  $4\pi$  component in the seemingly [2+2] type addition reaction as shown in Fig. 8.

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