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Microwave Spectrum of Acetyl Iodide*

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The microwave spectra of CH₃COI and CD₃COI were investigated in the region 8000 to 27 000 Mc/sec. The effects of internal rotation and quadrupole perturbations were found to be essentially independent. The height of the potential barrier hindering the methyl group internal rotation was determined to be 1301 ± 30 cal/mole from measured CH₃COI doublet splittings. Level mixing was found for several pairs of rotational states, analogous to Fermi resonance in vibrational levels. Mixing effects permitted determination of the quadrupole coupling constant χ_{ab} in both isotopic species. The values for quadrupole coupling constants in CH₃COI are $\chi_{aa} = -1563 \pm 2$, $\chi_{bb} = 914 \pm 2$, and $\chi_{ab} = -135.6 \pm 2$ Mc/sec. In CD₅COI the values are $\chi_{aa} = -1541 \pm 3$, $\chi_{bb} = 892 \pm 2$, and $\chi_{ab} = -258.5 \pm 10$ Mc/sec. Diagonalization of each of the above tensors gives $\chi_{\alpha\alpha} = -1569$ and $\chi_{\beta\beta} = 920$ Mc/sec.

I. INTRODUCTION

THIS work is part of a systematic study of molecules **I** with the general formula CH₃COZ, the "acetyl" series.¹⁻³ A primary motive for work on this series is elucidation of the nature of the potential barrier which hinders internal rotation of the CH₃ group about the C-C axis.

The analysis of internal barrier effects in acetyl iodide proceeded in much the same way as for acetyl chloride³ and acetyl bromide.² The height of the hindering barrier was found to be virtually the same in the iodide as in the chloride and bromide.

The quadrupole hyperfine effects were more complicated in the case of the iodide than for the other halides. While first-order perturbation theory was sufficient to account for hyperfine effects in the chloride and bromide, acetyl iodide hyperfine structure (hfs) required use of both first- and second-order perturbation theory. A computer program was written to generate the second-order corrections.

II. EXPERIMENTAL

Both CH₃COI and CD₃COI were prepared by the method of Thiele and Haakh.⁴ A 3-g quantity of red phosphorous was added to 10 cc of acetic anhydride in a 500-cc three-neck flask. A reflux condenser and CaCl₂ drying tube were placed in the center neck of the flask. The other two necks were fitted for later addition of reagents.

The flask was heated for 1 h in a water bath with gradual addition of 28 g of iodine. Gelation occurred and the reflux condenser was replaced by a distilling column packed with glass helices. An additional 1.5 g of phosphorous was then added and the flask was

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heated for several minutes, after which the contents were distilled.

The CH₃COI was collected at 105°C and the CD₃COI at 103.5°C. The yield in each case was about 4 cc. The product was pale orange, and storage at room temperature rapidly turned it dark brown. Samples stored at dry ice temperature remained undecomposed for months.

The spectrometer used was a Stark-effect type with 100-kc/sec square-wave modulation. Frequency measurements were made with multiples of a 5-Mc/sec crystal oscillator, monitored by radio station WWV. Both oscilloscope and recorder display were used, and all runs were made with the Stark cell at dry ice temperature. Observations were made of *a*-type and b-type transitions of CH₃COI and CD₃COI in the frequency range 8000 to 27 000 Mc/sec.

III. OBSERVED SPECTRA

Observed transitions with detailed quadrupole and internal rotation assignments are listed in Tables I and II.

For J > 3 R-branch transitions, the six strongest hyperfine components (the iodine nuclear spin of 5/2gives rise to six F values when J > 3) are described by the selection rule $\Delta F = 1(F \rightarrow F + 1)$. For Q branches involving J values of 4 or higher, the strong sextet is that involving the six $F \rightarrow F$ transitions.

The general transition thus appears as a sextet of hyperfine components, in the absence of resolved internal rotation structure. When both internal rotation and quadrupole perturbation components are fully resolved, 12 distinct lines may be observed for each rigid-rotor transition.

If the quadrupole and internal rotation effects were independent, the transitions would appear as sextets of doublets, with each doublet spacing the same. This was found to be the case for those CH₃COI transitions which were fully resolved.

Many additional intense high-J multiplets have been measured and assigned to the rigid rotator. Details of

^{*} Research supported by the Public Health Service, National Institutes of Health.

¹L. C. Krisher and E. B. Wilson, Jr., J. Chem. Phys. 31, 882 (1959).

 ² L. C. Krisher, J. Chem. Phys. 33, 1237 (1960).
³ K. M. Sinnott, J. Chem. Phys. 34, 851 (1961).
⁴ J. Thiele and H. Haakh, Ann. Chem. 369, 145 (1909).

27	7	Q
52		0

TABLE I. Observed spectra of CH₃COI.^a

Transition	$F \rightarrow F'$	σ	ν_{obs} (Mc/sec)	Transition	$F \rightarrow F'$	σ	vobs (Mc/sec)
a Type				b Type			
50,5-60,B	7/2-9/2	ь	23 769.83	$5_{0,5}-5_{1,4}$ (Cont)	7/2-7/2	A	11 200 00
- 010 - 010	5/2-7/2	b	23 776.65°		15/2-15/2	Eſ	11 289.88
	9/2-11/2	b	23 777.45			A	11 290.82
	11/2-13/2	b	23 792.33		5/2-5/2	$E \\ A$	11 291.47
	15/2-17/2	b	23 795.52			А	11 292.18°
	13/2-15/2	Ь	23 803.45	61,8-70,7	11/2-13/2	b	22 685.10
				01,8 70,7	13/2 - 15/2	b	22 686.98
51,4-61,5	7/2-9/2	Ь	25 226.12		9/2-11/2	b	22 697.10
	9/2-11/2	Ъ	25 227.88		15/2-17/2	b	22 701.07
	11/2 - 13/2	b	25 239.91		7/2-9/2	b	22 723.66
	5/2-7/2	b			17/2-19/2	b	22 726.95
	13/2-15/2	b	25 253.32			5	22 /20//0
	15/2-17/2	b	25 255.18	70,7-71,6	15/2-15/2	E	14 537.61
b Type						A	14 539.07
00,0-1,1	5/2-3/2	b	11 839.75		13/2-13/2	E	14 541.86
-,,-	5/2-7/2	b	11 923.31			A	14 543.40
	5/2-5/2	b	12 117.86		17/2-17/2	E∫	
	210 510	L	15 269 50			<i>A</i>	14 544.96
$1_{0,1} - 2_{1,2}$	3/2-5/2	b L	15 368.50 15 469.61		11/2-11/2	E	14 553.32
	3/2-3/2	b b	15 482.72			A	14 554.77
	7/2-7/2	b h	15 542.72		19/2–19/2	E	14 561.89
	3/2-1/2	b r	15 600.22			A	14 563.35
	7/2-9/2	b b	15 809.89		9/2-9/2	E	14 568.24
	5/2-7/2	b	15 839.47			\boldsymbol{A}	14 569.72
	5/2-5/2 5/2-3/2	b	15 940.35	80,8-81,7	17/2-17/2	E	16 722.45
	3/2-3/2	D	15 910.05	00,8 01,1	10/2 10/2	\widetilde{A}	16 724.38
20.2-31.3	9/2-11/2	ь	19 087.37		15/2-15/2	E	16 727.32
-,,-	5/2-7/2	b	19 115.06			A	16 729.19
	3/23/2	b	19 135.86		19/2-19/2	E	16 730.54
	7/2-9/2	Ь	19 201.36		,,-	Ā	16 732.38
$3_{1,2}$ - $3_{2,1}$	11/2-11/2	ь	23 192.91		13/2-13/2	E	16 741.48
51,2-52,1	7/2-7/2	b				\boldsymbol{A}	16 743.41
	9/2-7/2	Ď	23 427.22°		21/2-21/2	E	16 753.30
	9/2-11/2	b	23 428.84			A	16 755.17
	7/2-9/2	b	23 432.70°		11/2-11/2	E	16 760.95
	9/2-9/2	b	23 433.13°			A	16 762.83
4 4	3/2-3/2	Ь	22 555.29	100,10-101,9	21/2-21/2	E	22 251.68
$4_{1,3}$ - $4_{2,2}$	13/2-13/2	b	22 622.77		,, -	A	22 254.64
	5/2-5/2	b	22 640.50		19/2-19/2	E	22 256.83
	11/2-11/2	b	22 767.45			\widetilde{A}	22 259.82
	9/2-9/2	b	22 781.23		23/2-23/2	Ε	22 260.86
						E A	22 263.75
5 _{0,5} -5 _{1,4}	$\frac{11}{2} - \frac{11}{2}$	$\left. \begin{array}{c} E \\ E \end{array} \right\}$	11 286.95°		17/2-17/2	$E \\ A$	22 272.41
	9/2-9/2 11/2-11/2	L) A	11 287.680			A	22 275.39
	13/2-13/2	E)			25/2-25/2	$E \\ A$	22 291.19
	9/2-9/2	$\left. \begin{smallmatrix} E \\ A \end{smallmatrix} \right\}$	11 288.02°		-	A	22 294.20
	7/2-7/2	$\left. \begin{array}{c} E\\ A \end{array} \right\}$	11 288.95		15/2-15/2	E	22 296.72
	13/2-13/2	AJ	11 200.70			A	22 299.70

^a Estimated uncertainty ±0.15 Mc/sec unless otherwise stated. ^b Internal rotation (A-E) splittings not resolved. ^c Unresolved or poorly resolved line.

the hfs for these groups of lines have not been calculated and they are not reported in the tables.

IV. ROTATIONAL CONSTANTS

In order to determine the molecular rigid rotational constants A. B, C, the observed spectra must be

corrected for quadrupole and internal rotation effects to determine the hypothetical "center" frequencies where rigid-rotor transitions would occur in the absence of these perturbations. Table III compares center frequencies derived from the data with those calculated from A, B, and C.

Transition	$F \rightarrow F'$	$\nu_{\rm obs}$ (Mc/sec)	Transition	$F {\rightarrow} F'$	vobe (Mc/sec)
a-Type			b-Type		
51,4-61,5	7/9-9/2	23 209.40	72,6-81,7	15/2-17/2	15 090.77
	9/2-11/2	23 212.41		17/2-19/2	15 101.60
	5/2-7/2	23 223.38		13/2-15/2	15 105.30°
	11/2-13/2	23 224.91		11/2-13/2	15 136.36
	13/2-15/2	23 234.80		19/2-21/2	15 153.59
	15/2-17/2	23 240.02		9/2-11/2	15 175.23
60.5-70.7	9/2-11/2	25 278.16			
	7/2-9/2	25 281.39	80,8-81,7	15/2-15/2	15 077.64
	11/2-13/2	25 284.60		13/2-13/2	15 082.90
	13/2 - 15/2			17/2-17/2	15 084.82
	17/2-19/2	25 295.18		19/2-19/2	15 098.55
	15/2-17/2	25 301.64		11/2-11/2	15 101.60
b-Type				21/2-21/2	15 106.87
0 _{6.0} -1 _{1.1}	5/2-3/2	10 221.32	101,9-102,8	15/2-15/2	17 356.90
V0,0 -1,1	5/2-7/2	10 302.90	101,9 102,8	25/2-25/2	17 358.81
	5/2-5/2	10 493.10		17/2-17/2	17 365.28
			[23/2-23/2	17 369.69
2 _{0,2} -3 _{1,3}	3/2-5/2	16 780.80		19/2-19/2	17 370.80
	9/2-11/2	16 874.56		$\frac{21}{2-21}$	17 372.85
	5/2-7/2	16 895.84		21/2 21/2	17 072.00
	3/2-3/2	16 901.17	110.11-111.10	23/2-23/2	23 481.11
	7/2-9/2	16 979.28°	110,11 111,10	21/2-21/2	23 485.40
	7/2-7/25 5/2-5/2	16 994.09		25/2-25/2	23 490.28
	5/2-5/2	10 994.09		19/2-19/2	23 500.27
40,4-41,8	13/2-13/2	8 736.89		27/2-27/2	23 518.43
	5/2-5/2	8 738.46		17/2-17/2	23 523.26
	7/2-7/2	8 746.73			20 020120
	11/2-11/2	8 752.68°	289,19-2710,18	51/2-49/2	23 799.04°
	9/2-9/2)		289,20-2710,17	61/2-59/2	23 800.25°
51,5-52,4	5/2-5/2	23 074.53		53/2-51/2	23 821.55
	15/2-15/2	23 097.68		59/2-57/2	23 824.48
	9/2-9/2	23 147.22		55/2-53/2	23 834.00
	13/2-13/2	23 156.81		57/2-55/2	23 835.29
	11/2-11/2	23 166.01			
71,6-72,5	9/2-9/2	17 293.64°	287,21-296,24	57/2-59/2 55/2-57/2	23 447.02°
· .,0 · 2,0	19/2-19/2	17 306.31			23 453.36
	$\frac{13}{2} - \frac{13}{2}$ $\frac{11}{2} - \frac{11}{2}$	17 326.27		59/2-61/2	
	17/2-17/2	17 350.38		53/2-55/2 61/2-63/2	23 454.60
	13/2-13/2	17 351.33	1	51/2-53/2	23 468.60°
	15/2-15/2	17 362.27		<i></i>	

TABLE II. Observed spectra of CD₃COI.^{a,b}

^a Estimated uncertainty ±0.15 Mc/sec unless otherwise indicated. ^b No internal rotor splittings were resolved. ^c Unresolved or poorly resolved line.

No internal rotation doublets were observed in the CD₃COI spectrum due to the increased I_{α} of the deuterated methyl group. Since the CD₃COI quadrupole and rigid-rotor problems could be solved without internal rotation complications, this species was analyzed first.

Preliminary analysis on the Q-branch spectrum of CH₃COI determined approximate values of $\frac{1}{2}(A-C)$ and $\kappa = (2B-A-C)/(A-C)$. It was then possible to find a rigid-rotor structure which fits these two parameters. This was done by using the "acetyl" structure determined by Sinnott³ for acetyl chloride and adjusting the position of the iodine mass. This structure was used, replacing deuterium for normal hydrogen,

to predict a spectrum for CD_3COI from which the Q-branch study of that species began.

After κ was established from the Q-branch lines, $\frac{1}{2}(A+C)$ was determined from R-branch transitions. Low-J transitions were used for the final determination of the constants listed in Table IV. The moments of inertia in this table were derived from the rotational constants using the conversion factor 505 531 amu·Å²· Mc/sec.

V. BARRIER TO INTERNAL ROTATION

The interaction of internal and over-all rotation produced observable doublets in certain high-J transi-

Transition	CH3COI Experimental ^a	Calculated ^b	Transition	CD ₈ COI Experimental•	Calculated ^b
00,0-11,1	11 968.59	11 968.70	00,0-11,1	10 346.96	10 346.97
10,1-21,2	15 631.78	15 631.66	20,2-31,8	16 897.93	16 897.84
20,2-31,3	19 111.93	19 111.93	40,4-41,3	8 745.10	8 744.97
31,2-32,1	23 300.94	23 300.80	51,5,-52,4	23 129.60	23 129.72
41,3-42,2	22 695.89	22 695.86	51,4-61,5	23 230.21	23 230.10
40.4-41.8	10 154.58	10 154.52	60,6-70,7	25 292.96	25 292.91
50,5-51,4	11 289.17	11 289.06	71,8-72,5	17 333.36	17 333.70
50,5-60,6	23 791.40	23 791.33	72,8-81,7	15 125.94	15 125.58
51,4-61,5	25 245.13	25 244.94	80,8-81,7	15 092.97	15 093.00
61,6-70,7	22 705.57	22 705.31	101,9-102,8	17 365.79	17 366.56
70,7-71,8	14 550.79	14 550.67	110,11-111,10	23 499.81	23 500.99
8 _{0,8} -8 _{1,7} 10 _{0,10} -10 _{1,9}	16 738.85 22 272.61	16 738.77 22 272.97	$28_{9,19}-27_{10,18}$ $28_{9,20}-27_{10,17}$	23 819.13	23 827.02 23 827.16
			287,21-296,24	23 456.50	23 468.13

TABLE III. Experimental^a and calculated^b rigid-rotor transition frequencies in acetyl iodide (megacycles per second).

^a Derived from observed spectra by correcting for hyperfine and internal rotation effects. ^b Calculated from rotational constants in Table IV.

tions of CH₃COI. The height of the barrier hindering internal rotation of the CH₃ group about the C-C axis was determined from measured doublet splittings using the theory of Kilb, Lin, and Wilson⁵ and Herschbach.⁶

The theory assumes a potential-energy barrier of the form $V = \frac{1}{2}V_3(1 - \cos 3\alpha)$, where α is the angle of internal rotation.

The "high-barrier approximation" is applicable to acetyl iodide, i.e., only second-order perturbations are observable. The perturbation effects give rise to slightly different effective, or pseudorigid, rotational constants for the two types of torsional levels. Transitions between the A (nondegenerate) and E (doubly degenerate) torsional levels are forbidden because the molecular dipole moment is independent of the internal rotation angle. The resulting spectrum is thus doublets of nearby A and E pseudorigid-rotor transitions.

TABLE IV. Rotational constants and moments of inertia.^a

	CH₃COI	CD ⁸ COI
A	10 137.22 Mc/sec	8 666.38
В	2 206.97	2 034.23
С	1 831.48	1 680.59
Ia	49.8688 amu•Ų	58.3324
I_b	229.0611	248.5122
I.	276.0232	300.8057

* Estimated uncertainty ± 0.10 Mc/sec.

⁵ R. W. Kilb, C. C. Lin, and E. B. Wilson, Jr., J. Chem. Phys. 26, 1695 (1957). ⁶ D. R. Herschbach, J. Chem. Phys. 31, 91 (1959).

A particular doublet splitting can be written⁷

$$-\nu_E = \Delta \nu_{J,\tau \to J',\tau'}$$
$$= \Delta A \frac{\partial \Delta E}{\partial A} + \Delta B \frac{\partial \Delta E}{\partial B} + \Delta C \frac{\partial \Delta E}{\partial C},$$

where $\Delta E = E_{J',\tau'} - E_{J,\tau}$ is the rigid-rotor transition frequency and $\Delta A = \Delta W^{(2)} (I_{\alpha}^{2} \lambda_{a}^{2} / I_{a}^{2}) F$. For acetyl iodide this becomes

$$\Delta \nu_{J,\tau \to J',\tau'} = I_a{}^2 F \Delta W^{(2)} \left(\frac{\lambda_a{}^2}{I_a{}^2} \frac{\partial}{\partial A} \Delta E + \frac{\lambda_b{}^2}{I_b{}^2} \frac{\partial}{\partial B} \Delta E \right).$$

The quantity $\Delta W^{(2)}$ is tabulated⁸ in terms of a parameter s which is related to the barrier height by

$$V_3 = \frac{9}{4}Fs.$$

The notation is that of Ref. 6.

 ν_A

This set of relations determines V_3 for the measured $\nu_A - \nu_E$, with given values for the structural parameters λ_a , λ_b , and I_a . If acetyl iodide were a classical rigid body, it would be true that

$$I_{a} = I_{a} + I_{b} - I_{c}.$$

Since vibration and rotation are not separable, this relation is not exact for the moments of inertia derived from microwave data. An "inertial defect"⁹ must be added to the right-hand side when the I's in Table IV are used. A reasonable value of the inertial defect for the acetyl series is² 0.2 amu·Å² and gives $I_{\alpha}=3.11$

⁹ V. W. Laurie, J. Chem. Phys. 28, 704 (1958).

⁷ J. D. Swalen and D. R. Herschbach, J. Chem. Phys. 27, 100 (1957). ⁸ Reference 6, Appendix C.

amu \cdot Å² for acetyl iodide. This is close to the conventional value of 3.14 amu \cdot Å² which was used in the V₃ calculation. The barrier height is sensitive to I_{α} . The I_{α} value is not precisely known, however, because of this inertial defect which gives rise to the major uncertainty in V_3 . The assumed structural constants are uncertain also, but their effect on V_3 is less direct. The structural values in Table V are based on the CH₃CO structure from acetyl chloride,³ with an iodine position adjusted to fit the rotational constants in Table IV.

VI. QUADRUPOLE COUPLING CONSTANTS

The energies associated with the quadrupole moment of the iodine nucleus required the use of second-order perturbation theory to obtain accurate hfs predictions. The diagonal quadrupole coupling constants¹⁰ $\chi_{gg} =$ $eQ(\partial^2 V/\partial g^2)$ (where g=a, b, c, the molecule principal axes), were obtained graphically after correcting the observed spectra for second-order effects.

Two computer programs were used to calculate the second-order quadrupole corrections. One of them used the matrix elements of Van Vleck," and the other employed those of Bragg,12 and King, Hainer, and Cross.¹³ After adjustment for phase differences in the two schemes, the programs agreed to better than 0.01 Mc/sec for all predictions.

There were several pairs of levels, however, for which these perturbation techniques gave incorrect results: $(1_{1,0} \text{ and } 2_{0,2})$ in CH₃COI; $(1_{1,0} \text{ and } 2_{0,2})$, $(4_{2,2})$ and $5_{1,4}$), and $(7_{2,6}$ and $8_{0,8}$) in CD₃COI. These pairs of levels were all less than 600 Mc/sec apart and $c_{12}^{(1)} = V_{21}/(E_1^0 - E_2^0)$, where V_{21} is a matrix element of the quadrupole Hamiltonian, was found to be large, due to the small energy denominator, so that some

TABLE V. Internal barrier and assumed structural constants.

F	1.64841×10 ⁵ Mc/sec
λα	0.44177
λ_b	0.89713
Ια	3.14 amu•Å ²
V ₃ from 7 _{0,7} -7 _{1,6}	1305 cal/mole
V3 from 80,8-81,7	1301
V3 from 100,10-101,9	1296
V_{3}	1301 ± 30

¹⁰ C. H. Townes and A. L. Schawlow, Microwave Spectroscopy (McGraw-Hill Book Co., Inc., New York, 1955), Chap. 6.
¹¹ J. H. Van Vleck, Rev. Mod. Phys. 23, 213 (1951).
¹² J. K. Bragg, Phys. Rev. 74, 533 (1948).
¹³ P. C. Cross, R. M. Hainer, and G. W. King, J. Chem. Phys. 23, 210 (1944). modification was required. A perturbed wavefunction was written

$$\psi_1 = a_1 \psi_1^0 + b_1 \psi_2^0 + \sum_{m; m \neq 1, 2} c_{1m} \psi_m^0,$$

where a_1 , b_1 are zero order in the smallness parameter λ , and $c_{1m} = \lambda c_{1m}^{(1)} + \lambda^2 c_{1m}^{(2)} + \cdots (m \neq 1, 2)$. The time-independent Schrödinger equation then became

$$(H^{0}+\lambda V) (a_{1}\psi_{1}^{0}+b^{1}\psi_{2}^{0}+\sum_{m;m\neq 1,2}C_{1m}\psi_{m}^{0})$$

= $E_{1}(a_{1}\psi_{1}^{0}+b_{1}\psi_{2}^{0}+\sum_{m;m\neq 1,2}C_{1m}\psi_{m}^{0}),$

where $E_1 = E_1^0 + \lambda E_1^{(1)} + \lambda^2 E_1^{(2)} + \cdots$. This equation was solved to first order in λ for the constants a_1 and b_1 , the constants being determined from the pair of homogeneous equations, $a_1(W_{11}-\varepsilon)+b_1V_{12}=0$ and $a_1V_{21}+$ $b_1(W_{22}-\hat{\varepsilon})=0$, where $\varepsilon = E_1^0 + \lambda E_1^{(1)}$. These equations lead to the same secular equation for \mathcal{E} as is found for the eigenvalues when $\psi_{\pm} = a^{\pm}\psi_1^0 + b_{\pm}\psi_2^0$ are sought as eigenfunctions of the total Hamiltonian. The mixed energies have the usual 2×2 form

$$E_{\pm} = \frac{1}{2} (W_{11} + W_{22}) \pm \left[\frac{1}{2} (W_{11} - W_{22})^2 + |W_{12}|^2\right]^{\frac{1}{2}},$$

where

$$W_{\alpha\beta} = \int d\tau \psi_{\alpha}^{*} (H^{0} + \lambda V) \psi_{\beta}.$$

A simple way to utilize the usual perturbation formulas is to then use ψ_{\pm} instead of ψ_1^0 and ψ_2^0 in the set of basis functions. Since the effect of $(H^0+\lambda V)$ on ψ_{\pm} is known, one may define $H_{++}^{0} = E_{+}, H_{--}^{0} = E_{-},$ and $V_{++} = V_{--} = V_{+-} = V_{-+} = 0$. This formally treats V as part of the unperturbed Hamiltonian for mixed level matrix elements. Now, the standard perturbation results apply, with all other matrix elements defined in the usual way.

The second-order correction to a mixed level becomes

$$E_{\pm}^{(2)} = |a_{\pm}|^{2} E_{1}^{(2)} + |b_{\pm}|^{2} E_{2}^{(2)} + 2 \operatorname{Re} a_{\pm}^{*} b_{\pm} \sum_{k; k \neq 1, 2} \frac{V_{1k} V_{k2}}{E_{\pm} - E^{k0}}$$

These mixed level second-order corrections were found to be noticeably different from unmixed level corrections in some low-J levels, or where large mixing occurred. The cross term is always real, and in a few cases was 0.1 or 0.2 Mc/sec in size. It might be thought that the cross terms could be used to determine the sign of χ_{ab} , but all terms, including cross terms, depend on the square of χ_{ab} .

As a check on the modified theory, one should observe that this correction goes over to the usual unmixed form as the energy separation of the mixed pair increases. If $W_{11} > W_{22}$, as the levels separate, $|a_+|^2 \rightarrow 1$

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^{12, 210 (1944).}

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and $|b_+|^2 \rightarrow 0$, so we find

$$E_{+}^{(2)} \longrightarrow \sum_{n; n \neq 1, 2} \frac{|V_{1n}|^{2}}{E_{1}^{0} + V_{11} - E_{n}^{0}}$$
$$\simeq \sum_{n; n \neq 1, 2} \frac{|V_{1n}|^{2}}{E_{1}^{0} - E_{n}^{0}} - V_{11} \sum_{n; n \neq 1, 2} \frac{|V_{1n}|^{2}}{(E_{1}^{0} - E_{n}^{0})^{2}}$$

The last term is third order in smallness and is essentially that which disappears from the $E_{+}^{(3)}$ expression when V_{++} is formally set to zero. The $|V_{12}|^2/(E_1^0-E_2^0)$ term, missing above, occurs in the expanded square root of E_+ .

Another effect investigated was the extent to which the mixing of two levels affected any third level. All cases of interest were such that the approximation

$$(E_{1^{0}}+V_{11}-E_{n^{0}})^{-1} \simeq (E_{1^{0}}-E_{n^{0}})^{-1} \times \{1-[V_{11}/(E_{1^{0}}-E_{n^{0}})]\}$$

was valid. It was found that mixing at such energy separations produced small third-order effects, and it was sufficient to consider only the second-order effects produced by the unmixed levels.

Normally, the second-order perturbation of nearby levels produced a repulsion between them, i.e., a perturbation which couples them will mix the levels, and increase the energy separation between them, if one disregards perturbation effects of other levels on the pair. If the unperturbed levels are separated by less than a typical first-order perturbation energy, it is possible for the quadrupole perturbation to "invert" the ordering of levels. When $H^{0}_{11} > H^{0}_{22}$, but $(H^{0}_{11} +$ V_{11} < (H^{0}_{22} + V_{22}), the modified theory predicts that ψ_+ will be dominated by ψ_2^0 , $(|a_+/b_+|^2 \ll 1)$ instead of by $\psi^{0_{1}}$ as would "normally" be expected.

The $7_{2,6}$ and $8_{0,8}$ levels in CD₃COI offered an example of this behavior. The 80,8 unperturbed rigid-rotor level is about 33 Mc/sec higher than the unperturbed $7_{2,6}$ level. Addition of first-order quadrupole energies to these levels placed the $7_{2,6}$ state higher for F = 17/2 and F = 19/2 and leaves the $8_{0,8}$ level higher for the 11/2, 13/2, and 15/2 F values. Measurement of the $7_{2,6}-8_{1,7}$ and $8_{0,8} - 8_{1,7}$ transitions near 15 000 Mc/sec permitted a check of the theory. It also provided a good value for the unperturbed energy separation, which was iterated into the calculations as the hyperfine analysis progressed. Predictions based on the above theory agreed with the measured lines to experimental accuracy.

This form of perturbation theory correctly predicted the hfs of all transitions involving one level of a mixed pair. As a result, the value of χ_{ab} for each isotopic species was determined. In the absence of level mixing, energies associated with χ_{ab} are so small that no precise determination of its value can be made.

The signs of the diagonal χ 's were determined from first-order theory. The χ_{ab} sign was inferred from the probable geometry of the molecule and the change in

principal-axis systems for a CH₃ to CD₃ methyl-group substitution, assuming the χ tensor to be diagonal along the C-I bond.

When χ_{aa} , χ_{bb} , and χ_{ab} are determined, one may then make the transformation

$$R\begin{pmatrix} \chi_{aa} & \chi_{ab} & 0\\ \chi_{ba} & \chi_{bb} & 0\\ 0 & 0 & \chi_{cc} \end{pmatrix} = \begin{pmatrix} \chi_{\alpha\alpha} & 0 & 0\\ 0 & \chi_{\beta\beta} & 0\\ 0 & 0 & \chi_{\gamma\gamma} = \chi_{cc} \end{pmatrix},$$

where R is a rotation matrix. This requires no structural assumptions, and we have explicitly

$$\left. \begin{array}{l} \chi_{aa} \\ \chi_{\beta\beta} \end{array} \right\} = \frac{1}{2} (\chi_{aa} + \chi_{bb}) \mp \left[\frac{1}{2} (\chi_{aa} - \chi_{bb})^2 + |\chi_{ab}|^2 \right]^{\frac{1}{2}}.$$

The quadrupole coupling constants for CD₃COI and CH₃COI in both systems are given in Table VI.

At low J, some third-order quadrupole effects were observable. Exact calculations were not undertaken, except for the $0_{0,0}$ level, but inclusion of approximate third-order corrections definitely improved the hyperfine analysis, as Table VII indicates.

VII. DISCUSSION

The assumed iodine position which fit the rotational constants to a few megacycles per second involved a C-I distance of about 2.19 Å, and a CCI angle of 113°. This distance is longer than would be predicted from pure single bonding, and suggests ionic character in the bond, in addition to whatever double bonding may exist. Nothing more concrete can be stated, because the limited isotopic data in no way determined the iodine position, and because models like those discussed in Ref. 14 have not had complete success in correlating molecular properties.¹⁵

In acetyl iodide, the angle θ in the rotation matrix R is given by

$$\tan 2\theta = 2\chi_{ab}/(\chi_{aa}-\chi_{bb}).$$

If the χ tensor is diagonal along the C-I bond, this value of θ should agree with the angle between the

TABLE VI. Quadrupole coupling constants.

	CH3COI (Mc/sec)	CD3COI (Mc/sec)
χ_aa	-1563 ± 2	-1541 ± 3
Хьь	914 ± 2	892±2
Xcc	649 ± 2	649±2
Xab	-135.6 ± 2	-258.5 ± 10
χαα	-1570	-1568
χββ	921	919
χγγ	649	649

 ¹⁴ Reference 10, Chap. 9.
¹⁵ L. C. Krisher, thesis, Harvard University, Cambridge, Mass., 1959.

$F \rightarrow F'$	10	20	30 б	ν_{calo}	$\nu_{\mathrm{ob}s}$
$\frac{3}{2}-\frac{5}{2}$	265.19	+ 1.85	+0.08	15 368.59	15 368.50
$\frac{3}{2}$	-172.48	+10.46	-0.21	15 469.62	15 469.61
$\frac{7}{2}$ - $\frac{7}{2}$	-156.96	+ 7.79	+0.08	15 482.76	15 482.72
$\frac{3}{2}$	- 89.03	+ 0.01	+0.01	15 542.84	15 542.77
$\frac{7}{2}$ - $\frac{9}{2}$	- 31.80	+ 0.07	+0.01	15 600.13	15 600.22
$\frac{5}{2}$ $\frac{7}{2}$	171.29	+ 6.84	+0.01	15 809.99	15 809.89
$\frac{5}{2} - \frac{5}{2}$	203.74	+ 3.73	+0.05	15 839.37	15 839.47
$\frac{5}{2} - \frac{3}{2}$	296.45	+12.34	-0.24	15 940.40	15 940.35
		Hypothetical ce	nter 15 631.8	5°	

TABLE VII. Calculated and observed hfs in CH₃COI transition $1_{0,1} \rightarrow 2_{1,2}$ (megacycles per second).^a

* A-E splittings not resolved. ^b Approximate calculations. ^c Not corrected for internal rotation effects.

a axis and the C-I bond direction. In each isotopic species, the agreement between angles was better than 1°, using the assumed structure mentioned above. A related result is that the bond system χ 's given in Table VI, calculated without recourse to an assumed structure, are in good agreement.

Lack of cylindrical symmetry in the electric-field gradient about the C-I bond is taken as a manifestation of double-bond character.¹⁶ The contribution of a double-bonded structure¹⁴ may be discussed in terms of

$$\eta_{\text{bond}} = (\chi_{\beta\beta} - \chi_{\gamma\gamma})/\chi_{\alpha\alpha}$$

or Goldstein's quantity¹⁶

$$\delta = (\chi_{\beta\beta} - \chi_{\gamma\gamma}) / - \frac{3}{2} (eqQ)_{\text{atomic}}.$$

Howe and Goldstein¹⁷ noted that the halogens could be ranked in the order Cl, Br, I with regard to

TABLE VIII. Values of δ for acetyl and vinyl halides.

Z	CH3COZ	C_2H_3Z
³⁵ Cla	0.093 ^d	0.06 ^f
⁷⁹ Br ^b	0.085*	0.04
Ic	0.079	0.03f

^a Using (eqQ)_{atomic}=-109.7 Mc/sec, V. Jaccarino, and J. G. King, Phys. Rev. 83, 471 (1951).

^b Using (eqQ)_{atomic}=770 Mc/sec, J. G. King and V. Jaccarino, Phys. Rev. 94. 1610 (1954).

^c Using (eqQ)_{atomic} = -2293 Mc/sec, V. Jaccarino, J. G. King, R. A. Satten, and H. H. Stroke, 94, 1798 (1954).

e Reference 2.

f Reference 16.

⁴ C. D. Cornwell, J. Chem. Phys. 18, 1118 (1950); see also Ref. 17.

¹⁶ J. H. Goldstein, J. Chem. Phys. 24, 106 (1956).

¹⁷ J. A. Howe and J. H. Goldstein, J. Chem. Phys. 27, 831 (1957).

their capacities for double bonding. This was done by comparing δ values in vinyl halides, and it was further noted that Ingold¹⁸ had made the same ranking on the basis of chemical evidence. Data on the acetyl halides, Table VIII, show that the order of acetyl halide δ values agrees with the order given above. Comparison of η_{bond} values in the acetyl halides gives the same qualitative result.

Table VIII also shows acetyl C-Z bonds to possess roughly twice the double-bond character of C-Z bonds in the vinyl halides. This comparison is interesting² since each type of molecule has a pi-electron system adjacent to the C-Z bond, in the first case "carbonyl," in the second ethylenic.

The value determined for the internal barrier in acetyl iodide is virtually identical with those determined for acetyl bromide² and acetyl chloride.³ This intensifies the already imposing evidence in support of Wilson's¹⁹ statement that the barriers do not arise primarily from either steric repulsions or electrostatic interactions.

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¹⁸ C. K. Ingold, Structure and Mechanism in Organic Chemistry

(Cornell University Press, Ithaca, N.Y., 1953), p. 75. ¹⁹ E. B. Wilson, Jr., Proc. Natl. Acad. Sci. U.S. **43**, 811 (1957).

d Reference 3.