

A preliminary exploration of the mechanism for the occurrence of two types of various magnetic structures in the magnetotail

JIN Shuping¹, HU Xianpeng¹, CUI Hailong¹,
LIU Zhenxing², PU Zuyin³ & B. Wilken⁴

1. Department of Earth and Space Science, University of Science and Technology of China, Hefei 230026, China;
2. Center for Space Sciences and Application Research, Chinese Academy of Sciences, Beijing 100080, China;
3. Department of Geophysics, Peking University, Beijing 100871, China;
4. Max-Planck Institut fuer Aeronomie, D-37191 Katlanburg-Lindau, Germany

Abstract As well known, the magnetic cross-tail component B_y in the magnetotail is in direct proportion to the in-

terplanetary magnetic field (IMF) B_y component. And the polarity of IMF and plasmoid / flux rope B_y components do indeed agree. This results indicate that the IMF B_y penetrates plasmoids and the magnetic structures must therefore be three-dimensional. In this note, the dynamical processes of magnetotail in the course of a substorm are studied using a MHD code with two-dimensions and three components on the basis of two types of initial equilibrium solutions of the quiet magnetotail. The numerical results of two cases illustrate various features of time evolution of B_y component that correspond to two kinds of plasmoid-like structures: one is associated with a flux rope core and the other resembles a "closed loop" plasmoid. Therefore, the occurrence of various magnetic structures in the magnetotail might be related to nonsteady driven reconnection with different distributions of the B_y component.

Keywords: magnetospheric substorm, magnetic cross-tail component B_y , plasmoid-like structures, nonsteady magnetic reconnection.

Observations of magnetic structures in the magnetotail have frequently shown bipolar perturbations in the B_z component of the magnetic field. These are thought to be

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created by reconnection processes. In addition, the existence of significant B_y component across the tail, which is proportional to the IMF B_y , is a well-known fact^[1, 2]. Based on magnetic field measurements over a large fraction of the magnetotail, an approximate expression B_y (magnetotail) $\sim 0.13 B_y$ (IMF) was found^[1]. Moreover, a comparison of B_y observations within plasmoids with simultaneous upstream IMF B_y data^[3] indicates that the polarity of the IMF B_y is in agreement with that in the plasmoid. Consequently, a plasmoid should be considered as a three-dimensional structure. Five plasmoid-like structures associated with five energetic ion bursts were identified by Geotail observations in the deep tail ($x = -96R_E$) during an isolated substorm on January 15, 1994. Ref. [4] shows Geotail particle and magnetic field data, in which the five plasmoid events are marked P₁ to P₅. Ref. [4] indicates that in the P₂ event the B_y and B_z components show bipolar signatures; but in the third event P₃ the bipolar waveforms can be observed only in the B_z component and in coincidence with the inflection point of the B_z bipolar signatures, the B_y component shows a peak value. However, the P₁, P₄ and P₅ events do not show any indication for bipolar signatures in the B_z component.

In this note, taking aim at an exploration of the mechanism for the occurrence of various magnetic structures, MHD equations are numerically resolved. The simulation space is in rectangular plane (x, z), in which the x coordinate is in the anti-earth direction, the z coordinate is perpendicular (northward) to the plasmoid sheet, and the y coordinate is consistent with a right-handed coordinate system of x and z . A magnetic flux function $A(t, x, z)$ being related to the magnetic field is introduced by the equation

$$\mathbf{B} = \nabla \times (A \mathbf{e}_y) + B_y \mathbf{e}_y. \quad (1)$$

The MHD equations of two-dimension and three-component including the resistivity are written in a dimensionless form:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0, \quad (2)$$

$$\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} + \frac{1}{\rho} \nabla \left(\rho T + \frac{F}{2} B_y^2 \right) + \frac{F}{\rho} \Delta A \nabla A + \frac{F}{\rho} \nabla A \times \nabla B_y = 0, \quad (3)$$

$$\frac{\partial A}{\partial t} + \mathbf{v} \cdot \nabla A - \chi_m \Delta A = 0, \quad (4)$$

$$\frac{\partial B_y}{\partial t} + \nabla \cdot (B_y \mathbf{v}) - (\nabla \mathbf{v}_y \times \nabla A) \cdot \mathbf{e}_y - \chi_m \Delta B_y = 0, \quad (5)$$

$$\frac{\partial T}{\partial t} + \mathbf{v} \cdot \nabla T + (\gamma - 1) T \nabla \cdot \mathbf{v} = 0, \quad (6)$$

where

$$\chi_m = \frac{\eta_m}{v_0 l_0}, \quad F = \frac{A_0^2}{\rho_0 l_0^2 v_0^2}, \quad v_0 = \sqrt{RT_0}. \quad (7)$$

The length, magnetic field strength, density, temperature, magnetic flux function and velocity are expressed in units of l_0 ($= L_z = 20R_E$, the half-length of simulation box in the z direction), B_∞ (the initial value of B_x at $x = 0, z = L_z$), ρ_∞ (the initial plasma density on the boundary of magnetotail $z = L_z$), T_0 (the initial temperature), $A_0 = B_\infty l_0$, $v_0 = \sqrt{RT_0}$ (R is the gas constant), respectively.

The magnetic Reynolds number is given by

$$R_m = \frac{V_A l_0}{\eta_m} = \frac{V_A}{\chi_m v_0}, \quad (8)$$

where η_m is the resistivity (or magnetic viscosity), $V_A = B_c / \sqrt{4\pi\rho_\infty}$ is the Alfvén speed with B_c which is the initial magnetic field at $x = 100R_E, z = l_0 = 20R_E$ and related to B_∞ by $B_c = 0.5780 B_\infty = 10nT$. In the present study, the resistivity η_m is assumed to be uniform and magnetic Reynolds number is set as: $R_m = 4624$.

We assume the magnetotail to be initially in a static equilibrium state. The equations for $B_y(x, z)$, $P(x, z)$ and $A(x, z)$ can be determined by the equilibrium solution as follows:

$$B_y(x, z) = B_y(A), \quad P(x, z) = P(A),$$

and

$$\nabla^2 A = -4\pi \frac{dP^*(A)}{dA}, \quad (9)$$

where $P^*(A) = P(A) + \frac{B_y^2(A)}{8\pi}$. Assuming $A(x, z)$ weak variations with respect to x , the magnetic flux function can be obtained from eq. (9):

$$A(x, z) = B_\infty L_c \left[\ln \cosh \left(\frac{H(x)z}{L_c} \right) - \ln H(x) \right], \quad (10)$$

where $H(x)$ varies slightly in x and is expressed by

$$H(x) = \left(1.0 + \frac{bx}{vL_c} \right)^{-v}, \quad (11)$$

where we set $b = 0.018, v = 0.6, L_c = 0.1l_0 = 2R_E$.

For the uniform initial temperature T_0 , by using eqs. (9) and (10), two types of $B_y(x, z)$ and $\rho(x, z)$ which are satisfied for the equilibrium condition are given by the following expressions.

Type I.

$$= 2nT, \quad \frac{d}{dA} \left(\frac{B_y^2}{8\pi} \right) = 0, \quad (12)$$

$$\rho(x, z) = \rho_\infty + \rho_c \left[\frac{H(x)}{\cosh\left(\frac{H(x)z}{L_c}\right)} \right]^2. \quad (13)$$

Thus, at $x = 0$ and $z = 0$ the density is $\rho(0,0) = \rho_\infty +$

$$\rho_c, \quad \text{here } \rho_c = \frac{B_\infty^2}{8\pi RT_0}.$$

Type II.

$$B_y(x, z) = \sqrt{(1-\alpha)B_\infty} \frac{H(x)}{\cosh\left(\frac{H(x)z}{L_c}\right)}, \quad (14)$$

$$\rho(x, z) = \rho_\infty + \alpha\rho_c \left[\frac{H(x)}{\cosh\left(\frac{H(x)z}{L_c}\right)} \right]^2, \quad (15)$$

where α is a constant with values $0 < \alpha \leq 1$. It can be found by comparing eqs. (12) and (13) with eqs. (14) and (15) that the distribution of B_y in type II is significantly different from that in type I, but the distribution of the plasma density in type II is similar to that in type I. It can also be seen from eqs. (14) and (15) that ρ increases and B_y decreases with α increasing and $B_y = 0$ when $\alpha = 1.0$. In this study, the case with $\alpha = 0.9$ is investigated. We take $T_0 = 1.66 \times 10^6$ K, $\rho_\infty = 1.67 \times 10^{-25}$ g/cm³ (corresponding to $n_{\text{ion}} = 0.1$ proton/cm³), $B_\infty = 17.3nT$, hence $\rho_c = 4.34 \times 10^{-24}$ g/cm³ (corresponding to $n_{\text{ion}} = 2.6$ proton/cm³), $B_c = 10$ nT, the Alfvén velocity $V_A = B_c / \sqrt{4\pi\rho_\infty} = 690.3$ km/s, and the characteristic time is then given by $\tau_A = l_0/V_A = 184.6$ s. The respective system is then assumed to be initially in a static isothermal state, that is, $v_x = v_y = v_z = 0$ and $T = T_0$. Two types of equilibrium solutions of a quiet magnetotail are used as the initial states of the simulation study. The lengths of the simulation box in the z direction and in the x direction are taken to be $L_z = 20R_E$ and $L_x = 110R_E$ (the unit of length is set as $l_0 = L_z$). The simulation is carried out in the upper half plane, i.e. the computational domain is taken to be $0 \leq x \leq L_x$, $0 \leq z \leq L_z$, since the symmetric boundary conditions are imposed at the bottom boundary ($z = 0$). The computational domains

$0 \leq x \leq L_x$, $0 \leq z \leq L_z$ are divided into 23×56 grid points. In order to allow adequate spatial resolution in the neutral sheet of magnetotail, the grid spacing in the z direction increases according to a geometric series and a uniform mesh is adopted in the x direction.

We assume that a dawn-dusk electric field E is imposed on the boundary of magnetotail. Along the top boundary the electric field E is uniform in the range of $100R_E \leq x \leq 110R_E$ and E decreases linearly to zero within $0 \leq x \leq 100R_E$. Thus, an inward plasma flow $v_z = -cEB_x/B^2$, $v_x = -cEB_z/B^2$ is formed along the top boundary under the interaction of the electric field E and magnetic field B . The driven plasma inflow leads to the intermittent occurrence of the multiple X-line reconnection. The numerical results of all the two cases illustrate the repeated formation and progressive emission of the plasmoids with high density and high temperature. This means that a large amount of energy stored in the magnetotail is gradually dissipated by ejecting multiple plasmoids in the course of strong substorms. These results are in line with the features of multiple-plasmoid-like structures observed on Jan. 15, 1994 with Geotail. In this observation, five plasmoids are associated with five quasi-periodic energetic ion bursts. The repeated feature reproduced in this work is similar to that in the simulations with two-dimensions and two-components, more details can be found in refs. [5] and [6]. In the present study, two types of equilibrium solutions are used as the initial state of the simulation. Taking the different time evolution of B_y component into account, two kinds of plasmoid-like structures will be discussed.

Type I. At $t = 0$, $A(x, z)$, $B_y(x, z)$ and $\rho(x, z)$ are expressed by eqs. (10), (12) and (13), respectively. We set the electric field $E = 0.08$ which is in unit of $E_0 = V_A B_\infty / c$. The time variations of the total magnetic field amplitude B and three components B_x , B_y and B_z at the point ($x = 70R_E$, $z = -0.3R_E$) are shown in fig. 1. The bipolar signatures in the B_z component appear when a plasmoid passes this point in the neutral sheet. As shown in fig. 1 at $t \approx 49\tau_A$, $65\tau_A$, $73\tau_A$, $79\tau_A$, $83\tau_A$, $92\tau_A$, $106\tau_A$ and $112\tau_A$, obvious (+ / -) bipolar signature in the B_z component can be observed. In coincidence with the inflection point of the B_z bipolar signatures, the B_y component shows a peak value, whereas the B_x component shows a depressed value and the field magnitude B is between a peak and a minimum value. The maximum B_y value in the plasmoid's center is about twice of the value outside the plasmoid region. Such an intense axial field at the structure's center represents an important feature of the plasmoid-like structure with a flux rope core. For the

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case of type I , the distributions of B_y component in the

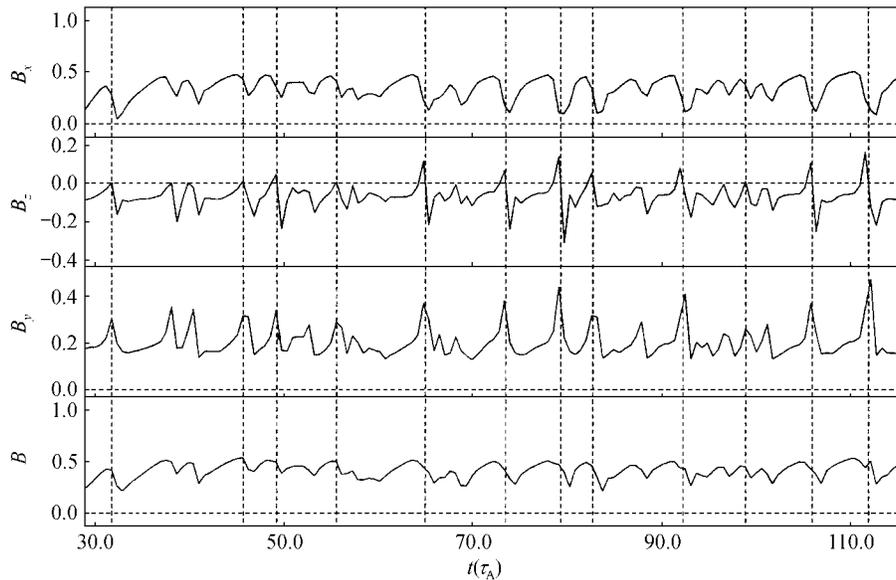


Fig. 1. Time history of magnetic field $B (B = \sqrt{B_x^2 + B_y^2 + B_z^2})$ and three components B_x , B_y , and B_z at a given point ($x=70R_E$, $z = -0.3 R_E$) in the neutral sheet for the case of type I .

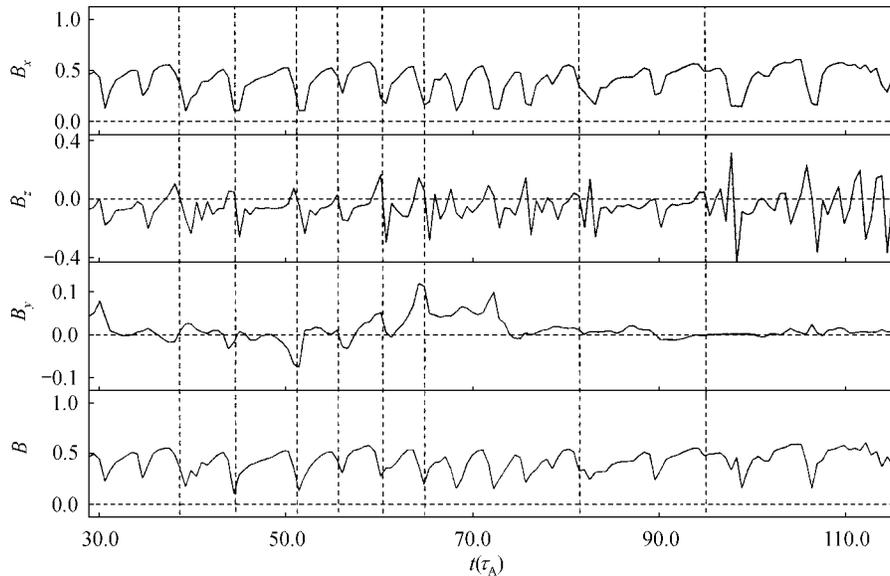


Fig. 2. Time history of the magnetic field $B (B = \sqrt{B_x^2 + B_y^2 + B_z^2})$ and three components B_x , B_y and B_z at a given point ($x=70R_E$, $z = -0.3R_E$) in the neutral sheet for the case of type II .

(x, z) plane are shown in fig. 2 at four different times. As shown in fig. 2, all B_y values are greater than zero and multiple B_y peak values exist in the plasma sheet. It can be found by comparing fig. 2 with the configuration of

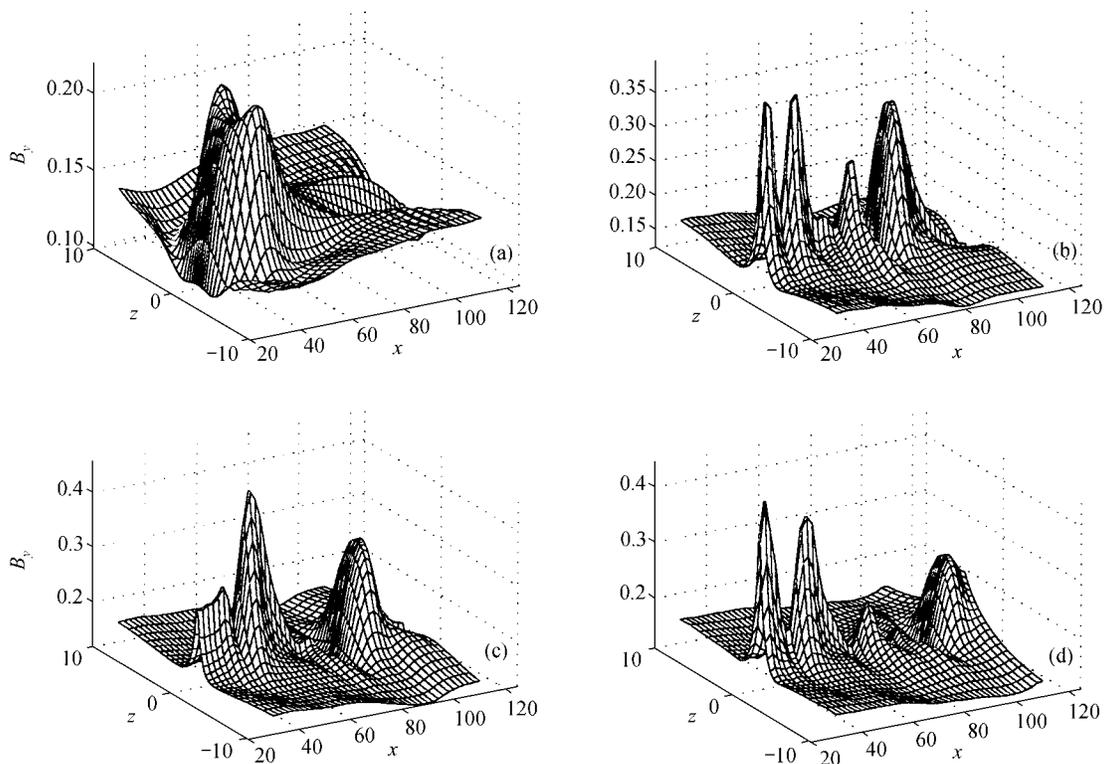
magnetic field lines (it is not displayed in this note) that the peak with the largest scale in the x - z direction always corresponds to the center of a pladmoid in the (x, z) plane. For example, at $t = 17.3 \tau_A$, $67.1 \tau_A$, $80.9 \tau_A$ and $94.8 \tau_A$, the B_y peak located at $x \sim 40 R_E$, $95 R_E$, $90 R_E$ and $100 R_E$ is

in line with the plasmoid locations at the same time, respectively. This also indicates that for the case of type I, the plasmoid structures always have a flux rope core configuration displayed in fig. 1. It can be found by comparing the Geotail observation in ref. [4] with that in fig. 1 that the numerical result of type I is similar to the main features of the P₃ plasmoid event in ref. [4]. In other words, the plasmoid-like structures with a flux rope core observed by Geotail can be reproduced by the case of type I.

Type II. At $t=0$, $A(x, z)$, $B_y(x, z)$ and $\rho(x, z)$ are expressed by eqs. (10), (14) and (15), respectively. We set $\alpha = 0.9$, $E = 0.12$. The time variations of the total magnetic field amplitude B and three components B_x , B_y , B_z at the point $(x = 70R_E, z = 0)$ are shown in fig. 3. The bipolar signatures in the B_z component are similar to those in fig. 1. This means that multiple plasmoids progressively pass through the neutral sheet of magnetotail. As shown in fig. 3, at the time when the bipolar signature passes through the inflection point, both B_x and the total field B show relative minimum. This is a common characteristic of a "classic" plasmoid. However, in fig. 3 the time variation of the B_z component shows a

complex pattern. Most of the inflection points of the B_z (at about $39\tau_A$, $44.5\tau_A$, $51.5\tau_A$, $55.5\tau_A$ and $60\tau_A$) are accompanied with a B_y bipolar signature. Also, there are components with rather large values (for example, at $t = 65\tau_A$ and $72\tau_A$). By comparing fig. 3 with ref. [4] for the case of type II, the kind of a plasmoid with bipolar signatures in the B_x and B_z components is similar to the features of P₂ plasmoid event.

The distributions of B_y component in the (x, z) plane are given in fig. 4. As shown in the figure, at $t = 40.5\tau_A$, the B_y component has generally negative values, but at $t = 66\tau_A$ and $75\tau_A$, the B_y component assumes positive values. However, later (e.g. $t = 107.5\tau_A$), the B_y component changes again into negative values in a quite large area. Thus it can be concluded that, as time elapses, the sign of B_y reverses if the reconnection process is still active. Furthermore, it can be found by comparing fig. 4 with the configuration of magnetic field lines (it is not displayed in this note) that the inflection regions of B_y component in fig. 4 appear to be near the plasmoid zones. Namely, for case of type II, both B_x and B_z components show bipolar



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Fig. 3. The surface plot of B_y component of the magnetic field at different time for the case of type I. (a) $t = 17.3 \tau_A$; (b) $t = 65.9 \tau_A$; (c) $t = 80.9 \tau_A$; (d) $t = 94.8 \tau_A$.

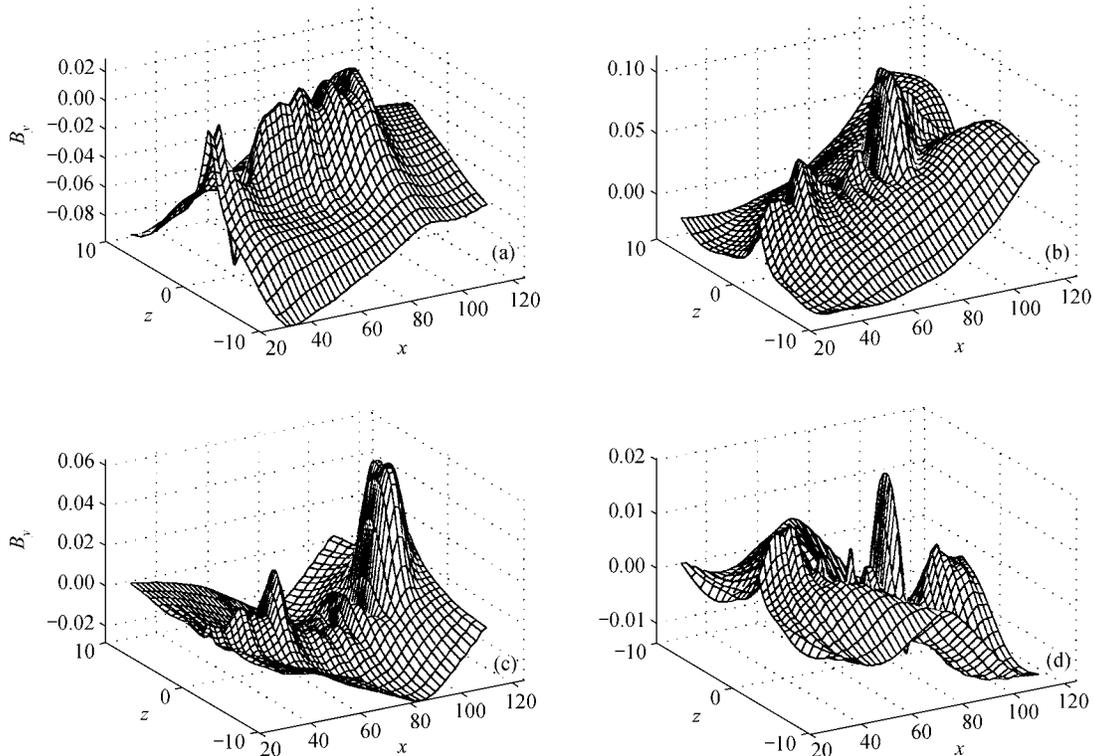


Fig. 4. The surface plot of B_y component of the magnetic field at different time for the case of type II. (a) $t = 40.5 \tau_A$; (b) $t = 65.9 \tau_A$; (c) $t = 74.6 \tau_A$; (d) $t = 107.5 \tau_A$.

signatures in some plasmoid regions. This is in agreement with the features displayed in $B_y \sim t$ and $B_z \sim t$ curves of fig. 3. Therefore, in ref. [4], the main features of P_2 event are reproduced by the simulation results of type II. Perhaps, the magnetic field of this configuration resembles a “close loop” plasmoid with a symmetry axis roughly in the (y, z) plane, which forms an angle of approximately 45° with respect to the z axis. The inflection points of B_y and B_z bipolar waveforms are not in coincidence. This phase relation can result from the fact that the center of the plasmoid-like structure does not pass through the selected point in the neutral sheet ($x = 70R_E, z = -0.3 R_E$).

In summary, a significant magnetic field B_y component in the magnetotail is closely correlated with the IMF and large B_y variations tend to be found during substorms^[2]. As shown in the simulation, two kinds of plasmoid-like structures are associated with two types of B_y initial distributions. Therefore, the occurrence of various magnetic structures in the magnetotail might be related to the non-stationary driven reconnection with different distributions of the B_y component as found here.

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