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# Excitation spectra and luminescence decay analysis of $K^+$ compensated $Dy^{3+}$ doped $CaMoO_4$ phosphors

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A series of  $Dy^{3+}/K^+$  doped calcium molybdate phosphors were synthesized by a hydrothermal synthesis method and structural, photoluminescence and decay studies were carried out. The crystal structure and phase of the prepared phosphors were investigated using X-ray diffraction (XRD), Transmission electron microscopy (TEM) and Fourier transform infrared spectroscopy (FTIR). These studies show that the phosphors are of a tetragonal structure with a nanorod morphology. The photoluminescence results indicate that these phosphors could be efficiently excited by near-ultraviolet radiation which causes emission in the blue and yellow regions. A novel approach was used to calculate different spectral parameters of powder samples using excitation spectra instead of conventional absorption spectra. Quantitative calculation of spectral parameters, luminescence decay and quantum yield suggest the suitability of this phosphor as an efficient luminescent medium for light emitting devices.

## 1. Introduction

The study of optical spectra of rare-earth (RE) ion doped phosphors has been an active area of research due to their wide application in solid-state lasers, lighting and display devices.<sup>1,2</sup> As an effective laser/luminescent medium calcium molybdate,  $CaMoO_4$  is a promising host candidate for properties such as high melting point (1445–1480 °C), high refractive index (1.98), average decay time (14 ms), quantum yield (9%), absorption cross section ( $\sim 10^3 \text{ cm}^{-1}$ ).<sup>3</sup> Therefore, luminescence properties of different rare earth doped  $CaMoO_4$  phosphor have been studied previously to achieve a good luminescent media.<sup>4–7</sup>

The performance of luminescent materials can be assessed by the knowledge of Judd–Ofelt (JO) intensity parameters  $\Omega_t$  ( $t = 2, 4, 6$ ), spontaneous emission probabilities, oscillator strength and radiative branching ratios. The  $\Omega_2$  parameter is associated with the polarization and asymmetry of the RE ligands. The other two parameters  $\Omega_{4,6}$  depend on long range effects. However, it is very difficult to calculate the JO intensity parameters for powder materials since the quantitative absorption spectra of powder materials can hardly be measured especially for the case of low RE dopant concentration. Now a days, with the development of novel nanophosphors for various display and lighting applications, it is very much required to find more convenient methods for the determination of JO intensity parameters in case of powder materials, which are essential to predict RE spectral properties for a variety of material applications. An approach simply based on the measurement of the excitation spectra has been proposed by W.

Luo *et al.* to determine the JO parameters for  $RE^{3+}$  ions doped powders.<sup>8</sup> The approach has been successfully applied to three systems:  $NGW:Er$ ,  $YLF:Nd$  and  $Y_2O_3:Er^{3+}$  nanocrystals and the obtained JO parameters using this approach were in good agreement with that determined from the conventional method.

As per our literature survey till date no work has been reported on the estimation of JO parameters of doped/codoped  $CaMoO_4$  phosphors. The authors have already reported the luminescence properties of this  $K^+$  compensated  $Dy^{3+}$  doped  $CaMoO_4$  phosphors.<sup>9</sup> Keeping this in view, an attempt was made for the first time to estimate different spectral parameters, luminescence decay time and quantum yield of the optimized  $Dy^{3+}$  doped and  $K^+$  compensated codoped phosphor from the excitation spectra.

## 2. Experimental

### 2.1. Sample synthesis

Doped  $Ca_{1-x}MoO_4:Dy_x^{3+}$  ( $x = 0, 0.01, 0.015, 0.02, 0.03, 0.04, 0.05$ ) phosphors and codoped  $Ca_{1-x-y}MoO_4:Dy_x^{3+}, K_y^+$  ( $x = 0.02, y = 0.01, 0.02, 0.03, 0.04, 0.05$ ) phosphors were prepared by hydrothermal synthesis. The reactants  $CaCO_3$ ,  $(NH_4)_6Mo_7O_{24} \cdot 4H_2O$ ,  $Dy_2O_3$  and  $K_2CO_3$  were weighted in an appropriate stoichiometric ratio. All reagents were analytical grade and used without further purification. In a typical synthesis, solution A was prepared by dissolving  $CaCO_3$  and  $Dy_2O_3$  in diluted nitric acid. The solution was heated to drive away the unreacted nitric acid, and the residue was redissolved in 10 mL of deionized water and stirred for about 1 h at room temperature.  $(NH_4)_6Mo_7O_{24} \cdot 4H_2O$  was dissolved in 50 mL of deionized water named solution B. After stirring for about 15

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minutes, solution B was added dropwise into the solution A under vigorous stirring. The pH of the solution was adjusted in between 8–9 using NaOH solution (1 N). The resulting precursor solution was further stirred for about half an hour. After that, the solution was poured into 80 mL capacity Teflon-lined stainless steel autoclave and further heated to 180 °C for 12 hours. After cooling down to room temperature naturally, the nanophosphors were directly collected at the bottom of the vessel. The phosphors were filtered, washed several times with deionized water and absolute ethanol, and dried in oven at 100 °C for 5 hours.<sup>10</sup> For the preparation of codoped phosphors, solution A was prepared by dissolving CaCO<sub>3</sub>, Dy<sub>2</sub>O<sub>3</sub> and K<sub>2</sub>CO<sub>3</sub> in diluted nitric acid and rest of the procedure was same.

## 2.2. Sample characterization

X-Ray diffractogram of the prepared phosphors were recorded in a wide range of Bragg angle  $2\theta$  ( $10 \leq 2\theta \leq 80^\circ$ ) using Bruker D8 X-ray diffractometer with CuK $\alpha$  radiation ( $\lambda = 0.154056$  nm). FTIR studies were carried out on Perkin Elmer make Spectrum RX1 Spectrometer. Morphology and crystallite size of the phosphors were determined by JEOL make JEM-2100 transmission electron Microscope. Photoluminescence studies were carried out on Hitachi make F-2500 Fluorescence Spectrophotometer in the wavelength range 220–700 nm. The decay kinetics was studied on Quanta Master 40 fluorometer. All the studies were carried out at room temperature.

## 2.3. Theoretical background

**2.3.1. Judd–Ofelt theory.** The J–O theory<sup>11,12</sup> has been extensively used to analyze the radiative transitions of rare-earth ions in several host materials. The electric-dipole (ED) and magnetic-dipole (MD) transitions are mainly used to calculate the line strengths of optical spectra of RE<sup>3+</sup> ions in luminescent materials. For most of the transitions, the probability for magnetic dipole transitions is much smaller than those for the forced electric dipole transitions [ $A_{\text{md}}[J \rightarrow J'] < A_{\text{ed}}[J \rightarrow J']$ ]. However, in certain cases, they may significantly contribute to the total  $J \rightarrow J'$  radiative transition probability.

The excitation line strength for an ED transition can be expressed in terms of J–O intensity parameters  $\Omega_{2,4,6}$  by

$$S_{\text{calc}}^{\text{ed}}(J \rightarrow J') = \sum_{t=2,4,6} \Omega_t |\langle \varphi J \| U^t \| \varphi' J' \rangle|^2 \quad (1)$$

where the matrix elements  $\langle \langle U^t \rangle \rangle$  are doubly reduced unit tensor operator<sup>13</sup> of rank  $t$  calculated in the intermediate coupling approximation and are independent of the crystal host. The parameters  $\Omega_2$ ,  $\Omega_4$ , and  $\Omega_6$  exhibit the influence of the host on the transition probabilities since they contain the crystal-field parameters, inter configurational radial integrals, and the interaction between the central ion and intermediate environment. The reduced matrix elements of the unit tensor  $|\langle \varphi J \| U^t \| \varphi' J' \rangle|^2$  were taken from ref. 14.

The measured line strengths ( $S_{\text{meas}}^{\text{ed}}$ ) were calculated from the excitation spectrum by:

$$S_{\text{meas}}^{\text{ed}}(J \rightarrow J') = \frac{3ch(2J+1)}{8\pi^3 \bar{\lambda} e^2 N_0} \frac{9n}{(n^2+2)^2} \Gamma_{\text{exc}} \quad (2)$$

where  $J$  ( $J'$ ) is the angular momentum quantum number of the initial (final) state of rare earth ion,  $n$  is the refractive index of the sample,  $\bar{\lambda}$  is the mean wavelength of the excitation band,  $N_0$  is rare earth ion concentration and  $\Gamma_{\text{exc}}$  is the integrated excitation intensity for each band from the initial state to the final state which is similar to the integrated absorbance for the absorption spectrum.<sup>8</sup> The factor  $[9n/n^2 + 2]^2$  in eqn (2) is the local field correction for the ion in the dielectric host medium. The measured line strengths were then used to obtain the J–O parameters  $\Omega_2$ ,  $\Omega_4$ , and  $\Omega_6$  by solving a set of  $n$  number of equations for the corresponding transitions between  $J$  and  $J'$ . A least squares fit method was used for eqn (1) and (2) to get a good fit between the calculated and measured line strengths as well as to obtain J–O intensity parameters ( $\Omega_i$ ).

The magnetic-dipole transitions are parity allowed between states of the  $4f^N$  configuration and are subject to the selection rules,  $\Delta l = 0$ ,  $\Delta S = 0$ ,  $\Delta L = 0$ ,  $|\Delta J| \leq 1$ , (but not  $0 \leftrightarrow 0$ ) in the Russel–Saunders limit.<sup>15</sup> The line strengths due to the magnetic dipole contribution were determined using the following expression:

$$S_{\text{calc}}^{\text{md}}(J \rightarrow J') = \left( \frac{eh}{4\pi mc} \right)^2 | \langle (SLJ) \| L + 2S \| (S'L'J') \rangle |^2 \quad (3)$$

The line strengths of the bands due to magnetic dipole transition are determined from the corresponding values of oscillator strengths,  $f_{\text{calc}}^{\text{md}}$  using the following expression:

$$S_{\text{calc}}^{\text{md}}(J \rightarrow J') = \frac{3h(2J+1)n^2}{8\pi^2 mc \nu} f_{\text{calc}}^{\text{md}} \quad (4)$$

Values of  $f_{\text{calc}}^{\text{md}}$  were taken from Carnall *et al.*<sup>16</sup>

**2.3.2. Radiative properties.** The J–O parameters were used to predict the radiative properties of the excited states of Dy<sup>3+</sup> ion. The radiative transition probability ( $A_R$ ) for a transition  $J \rightarrow J'$  is calculated from the following equation:<sup>17</sup>

$$A_R(J \rightarrow J') = \frac{64\pi^4 \nu^3 e^2}{3h(2J+1)} \left[ \frac{n(n^2+2)^2}{9} S_{\text{ed}} + n^3 S_{\text{md}} \right] \quad (5)$$

where  $S_{\text{ed}}$  and  $S_{\text{md}}$  are the electric and magnetic-dipole line-strengths. The radiative lifetime ( $\tau_R$ ) of an excited state is given by

$$\tau_R(J) = \frac{1}{\sum_{J'} A_R(J \rightarrow J')} \quad (6)$$

The branching ratio ( $\beta_R$ ) corresponding to the emission from an excited level  $J$  to lower level  $J'$  is given by

$$\beta_R(J, J') = \frac{A_R(J \rightarrow J')}{\sum_{J'} A_R(J \rightarrow J')} \quad (7)$$

The stimulated emission cross-section ( $\sigma(\lambda_p)$ ) can be expressed as:

$$\sigma(\lambda_p)(J \rightarrow J') = \frac{\lambda_p^4}{8\pi c n^2 \Delta\lambda_{\text{eff}}} A_R(J \rightarrow J') \quad (8)$$

where  $\lambda_p$  is the peak wavelength and  $\Delta\lambda_{\text{eff}}$  is its effective line-width found by dividing the area of the emission band by its maximum height.

### 3. Results and discussions

#### 3.1. Structural analysis

**3.1.1. XRD studies.** Fig. 1 shows the XRD spectra of undoped  $\text{CaMoO}_4$ , 2 mol%  $\text{Dy}^{3+}$  doped  $\text{CaMoO}_4$  and 2 mol%  $\text{K}^+$  codoped  $\text{CaMoO}_4$  phosphors. A single tetragonal phase was observed and diffraction peaks match with JCPDS card no. 77-2244 with space group  $I4_1/a$  (88). The substitution of  $\text{Dy}^{3+}$  and  $\text{K}^+$  for  $\text{Ca}^{2+}$  did not influence the phase and crystal structure of  $\text{CaMoO}_4$  suggesting that dopant and codopant might have occupied the cationic sites in the host lattice structure, following the charge balancing:  $2\text{Ca}^{2+} = \text{Dy}^{3+} + \text{K}^+$ . The enhancement of XRD peak intensities in codoped phosphor is due to the incorporation of  $\text{K}^+$  thus improving the crystallinity. The ( $hkl$ ) values of most prominent peaks are shown in the XRD pattern.

**3.1.2. Rietveld refinement.** A structural refinement by the Rietveld method<sup>19</sup> was performed using the Fullprof Program.<sup>20</sup> Fig. 2a shows the Rietveld plot for undoped  $\text{CaMoO}_4$ . The structural refinement results are presented in Table 1. Fig. 2b shows the schematic representation of the tetragonal  $\text{CaMoO}_4$  unit cell. The unit cell was modelled through a program called Visualization for Electronic and Structural Analysis (VESTA)<sup>21</sup> using Rietveld refinement data. The Ca and Mo sites have S4 point symmetry. Its crystal structure has two building blocks of  $\text{CaO}_8$  clusters with scalenohedral configuration and snub dipoide polyhedra (8 vertices, 12 faces, and 18 edges) and  $\text{MoO}_4$

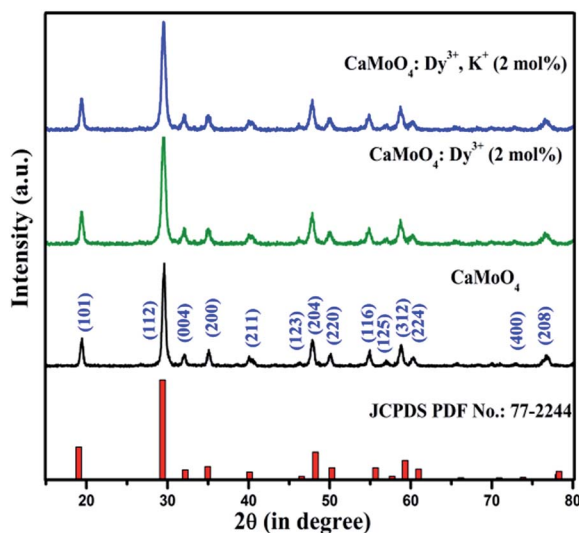


Fig. 1 XRD spectra of  $\text{CaMoO}_4$  phosphors.

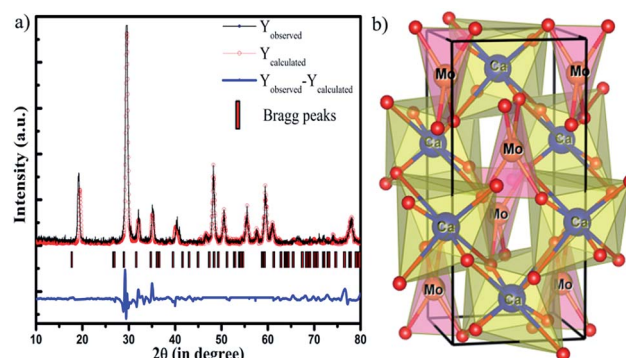


Fig. 2 Rietveld refinement pattern and  $\text{CaMoO}_4$  unit cell.

Table 1 Structural parameters of undoped  $\text{CaMoO}_4$  after Rietveld refinement

Atoms	Wyckoff	x	y	Z	Occupancy	Lattice constants
Ca	4b	0	0.25	0.625	0.250	$a = b = 5.12$
Mo	4a	0	0.25	0.125	0.250	$c = 11.11$
O	16a	0.090	0.398	0.306	1.000	

tetrahedra. Due to the O–Mo–O bond angles, the  $[\text{MoO}_4]$  clusters are slightly distorted into the matrix.<sup>22</sup> Each O atom links with two Ca atoms and one Mo atom. There are two different Ca–O bond lengths in  $\text{CaO}_8$  and one Mo–O bond length in  $\text{MoO}_4$ .

**3.1.3. TEM studies.** TEM images of undoped  $\text{CaMoO}_4$  phosphor is shown in Fig. 3a. Nanorod like structures of 20 nm diameter was observed. The high resolution TEM (HRTEM) image suggests that phosphor is crystalline (Fig. 3b). Its selected area electron diffraction (SAED) is shown in Fig. 3c. Based on a tetragonal phase, the rings are observed and ( $hkl$ ) planes are indexed. The SAED pattern show the (101), (112), (004), (200), (123), (211), (116) and (224) planes in good agreement with the XRD result. The lattice fringe was observed and  $d = 2.78 \text{ \AA}$ , which matches with  $hkl = 004$  plane of tetragonal phase.

Fig. 4a and b show the HRTEM images of  $\text{Dy}^{3+}$  (2 mol%) doped and  $\text{Dy}^{3+}$ ,  $\text{K}^+$  (2 mol%) codoped phosphors. It clearly shows an improvement in crystallinity and  $d = 3.23 \text{ \AA}$  for doped and  $d = 3.13 \text{ \AA}$  for codoped phosphor, which matches with  $hkl = 112$  plane.

**3.1.4. FTIR studies.** FTIR spectra of the undoped,  $\text{Dy}^{3+}$  (2 mol%) doped,  $\text{K}^+$  (2 mol%) codoped phosphors in wave number range of  $4000\text{--}400 \text{ cm}^{-1}$  are shown in Fig. 5. It can be seen that all the phosphors show approximately similar vibrations. The strong absorption band occurring at  $805 \text{ cm}^{-1}$  is due to the asymmetric stretching vibrations in the  $[\text{MoO}_4]^{2-}$  clusters and a weak band at  $432 \text{ cm}^{-1}$  is due to the presence of asymmetric bending vibrations present in the O–Mo–O bonds.<sup>18</sup> The inset illustrates a characteristic  $[\text{MoO}_4]$  cluster with asymmetric stretching and asymmetric bending vibrations between the O–Mo–O bonds. The bands at  $1652$  and  $3419 \text{ cm}^{-1}$  correspond to H–O–H bending and O–H stretching vibrations of water molecules present on the surface of particles respectively. The



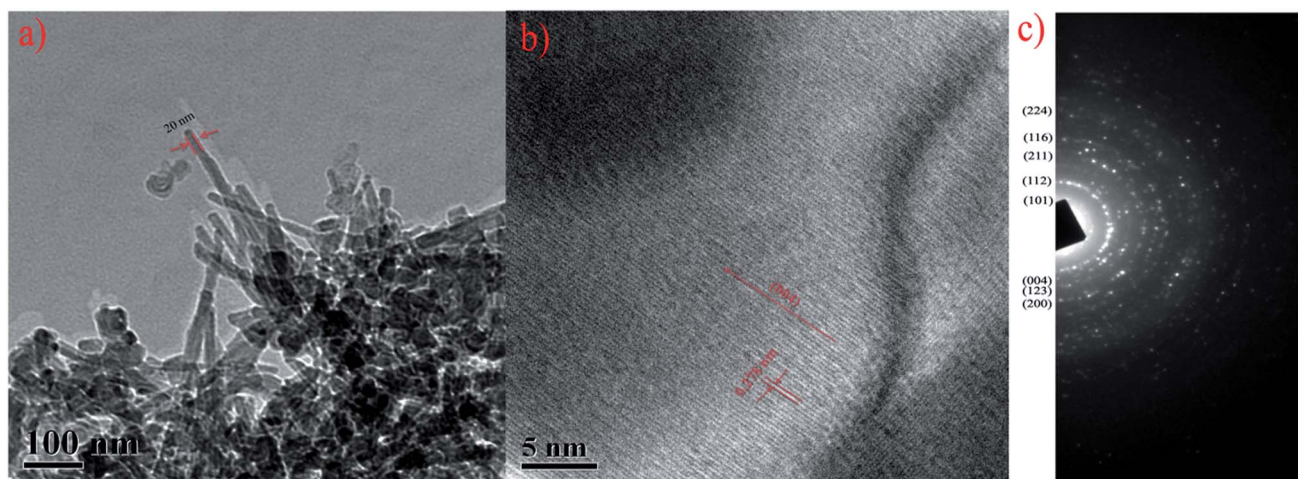


Fig. 3 TEM studies of  $\text{CaMoO}_4$  phosphor.

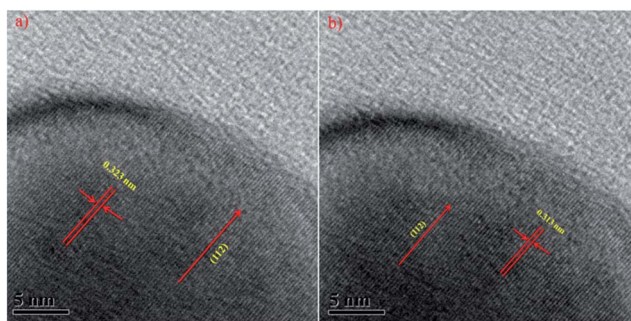


Fig. 4 HRTEM studies of (a) doped (b) codoped  $\text{CaMoO}_4$  phosphors.

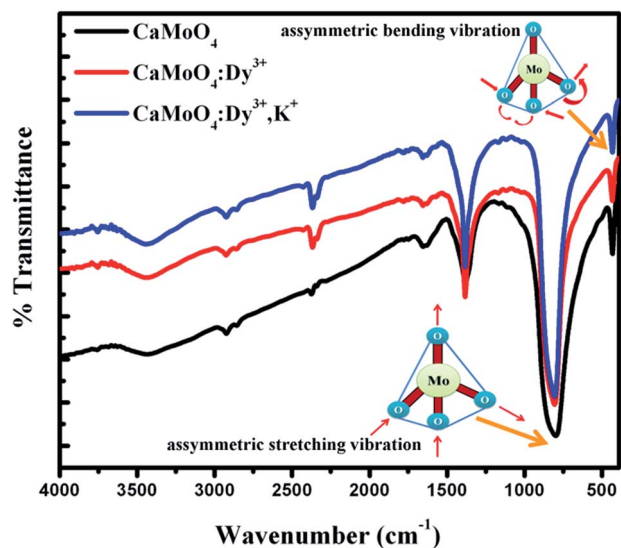


Fig. 5 FTIR of  $\text{CaMoO}_4$  phosphors.

$1383\text{ cm}^{-1}$  vibration is due to the N–O band of  $\text{HNO}_3$  used during the preparation of sample. The peaks observed at  $2382$  and  $2925\text{ cm}^{-1}$  in the as-prepared sample indicates C–H stretching vibration.<sup>23</sup>

### 3.2. Luminescence analysis

**3.2.1. Excitation spectra.** The excitation spectra of  $\text{Dy}^{3+}$  doped  $\text{CaMoO}_4$  with different  $\text{Dy}^{3+}$  ion concentrations (1, 1.5, 2, 3, 4 and 5 mol%) and  $\text{K}^+$  codoped  $\text{CaMoO}_4:\text{Dy}$  with varying concentration of  $\text{K}^+$  (1, 2, 3, 4, 5 mol%) and optimum  $\text{Dy}^{3+}$  concentration at 2 mol% are shown in Fig. 6a. The spectra exhibit a broad band from 220 nm to 330 nm with a maximum centred at 275 nm. This is due to charge transfer from oxygen ( $\text{O}^{2-}$ ) to metal ( $\text{Mo}^{6+}$ ) ion.<sup>24</sup> The other peaks<sup>25</sup> at 351 nm ( $^6\text{H}_{15/2} \rightarrow ^6\text{P}_{7/2}$ ), 366 nm ( $^6\text{H}_{15/2} \rightarrow ^4\text{M}_{19/2} + ^4\text{D}_{3/2} + ^6\text{P}_{5/2}$ ), 387 nm ( $^6\text{H}_{15/2} \rightarrow ^4\text{M}_{21/2} + ^4\text{K}_{17/2} + ^4\text{F}_{7/2} + ^4\text{I}_{13/2}$ ), 427 nm ( $^6\text{H}_{15/2} \rightarrow ^4\text{G}_{11/2}$ ), 452 nm ( $^6\text{H}_{15/2} \rightarrow ^4\text{I}_{15/2}$ ) and 475 nm ( $^6\text{H}_{15/2} \rightarrow ^4\text{F}_{9/2}$ ) are due to f–f transition of  $\text{Dy}^{3+}$ . These transitions are magnified in Fig. 6b.

**3.2.2. J–O parameters.** From the excitation spectra the measured line strengths ( $S_{\text{meas}}$ ) were determined by using eqn (1). The Judd–Ofelt parameters  $\Omega_2$ ,  $\Omega_4$ ,  $\Omega_6$  were obtained using least-squares fitting approach between the  $S_{\text{meas}}$  and the  $S_{\text{cal}}$ . The J–O parameters, for various  $\text{Dy}^{3+}$  concentrations and for 2 mol%  $\text{K}^+$  codoped  $\text{CaMoO}_4$  phosphors are tabulated in Table 2 along with the previously reported value for  $\text{CaMoO}_4:\text{Dy}$ .<sup>26</sup>

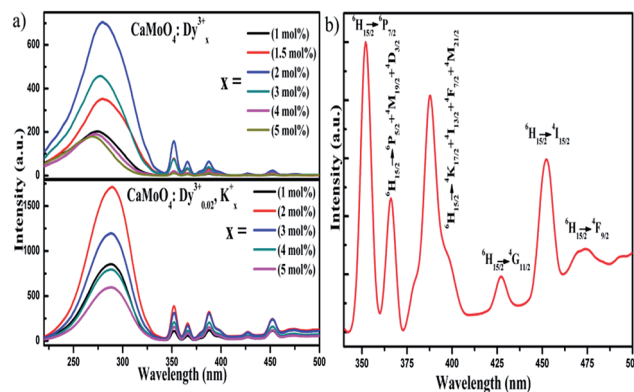


Fig. 6 Excitation spectra of  $\text{CaMoO}_4$  phosphors.

Table 2 Judd–Ofelt intensity parameters

Phosphor	Mol%	$\Omega_2 \times 10^{-20} \text{ (cm}^2\text{)}$	$\Omega_4 \times 10^{-20} \text{ (cm}^2\text{)}$	$\Omega_6 \times 10^{-20} \text{ (cm}^2\text{)}$	$\text{rms}\Delta S \times 10^{-20} \text{ (cm}^2\text{)}$
$\text{CaMoO}_4:\text{Dy}^{3+}$	$x = 1$	50.34	2.71	9.78	0.577
	$x = 1.5$	9.58	1.89	4.78	0.033
	$x = 2$	7.21	1.41	3.59	0.052
	$x = 3$	7.88	0.96	2.92	0.024
	$x = 4$	21.30	0.89	3.33	0.036
	$x = 5$	17.41	0.58	2.89	0.024
$\text{CaMoO}_4:\text{Dy}^{3+}, \text{K}^+$	$x = 2, y = 2$	40.94	1.36	6.18	0.406
$\text{CaMoO}_4:\text{Dy}$ (from literature)	1 wt%	0.266	2.89	1.79	

There is not much variation of  $\Omega_4$  and  $\Omega_6$  with change in the  $\text{Dy}^{3+}$  concentration. But the experimental value of  $\Omega_2$  is most sensitive to the ligand environment which can be clearly observed by the change of its value with concentration of  $\text{Dy}^{3+}$  and also with incorporation of  $\text{K}^+$  ions. Higher value of  $\Omega_2$  indicates high degree of metal–ligand covalency bond and lower symmetry of the coordination structure surrounding the  $\text{Dy}^{3+}$  ions.<sup>27</sup> The high  $\Omega_2$  value indicates the possession of high charge density for  $\text{Dy}^{3+}$  ion which polarizes the  $\text{O}^{2-}$  anion to a much greater extent. This results in a larger extent of molecular orbital overlap between the f orbital of the  $\text{Dy}^{3+}$  and the p orbital of the  $\text{O}^{2-}$  ion, resulting in expansion of the electron cloud and the formation of a bond having less ionic and more covalent character. The decrease in  $\Omega_2$  value decreases orbital overlap between  $\text{Dy}^{3+}$  and  $\text{O}^{2-}$  and hence the covalent character.<sup>28</sup>

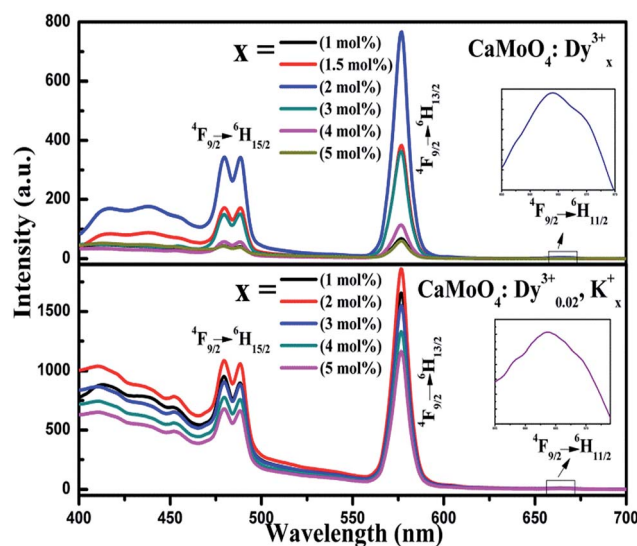
The root mean square (rms) deviation between the experimental and calculated line strengths is defined as:

$$\text{rms}\Delta S = \sqrt{\sum_{i=1}^N (S_{\text{meas}} - S_{\text{cal}})^2 / N - 3} \quad (9)$$

where  $N$  is the number of experimental bands involved in the above calculation. The value of the  $\text{rms}\Delta S$  reflects the goodness of the J–O parameters fitting.

**3.2.3. Emission spectra.** Fig. 7 represents the emission spectra of doped/codoped  $\text{CaMoO}_4$  phosphors as a function of  $\text{Dy}^{3+}$  and  $\text{K}^+$  concentration. Three peaks observed at 489, 576 and 663 nm are assigned to  $^4\text{F}_{9/2} \rightarrow ^6\text{H}_{15/2}$  (blue),  $^6\text{H}_{13/2}$  (yellow) and  $^6\text{H}_{11/2}$  (red) transitions, respectively. The transition  $^4\text{F}_{9/2} \rightarrow ^6\text{H}_{11/2}$  is of very low intensity which is magnified in the inset. The  $^4\text{F}_{9/2} \rightarrow ^6\text{H}_{13/2}$  transitions are hypersensitive electronic dipole transitions with  $\Delta J = 2$ , which are greatly affected by the coordination environment and are allowed only at low symmetries with no inversion centre. In this case, the dominance of this transition indicates that the location of  $\text{Dy}^{3+}$  deviates from the inversion symmetry, i.e., at low symmetry positions. This also corroborates the fact that  $\Omega_2$  has a high value which implies the asymmetric coordination surrounding  $\text{Dy}^{3+}$  ions.<sup>18,29</sup>

The luminescence intensity increases with increase of concentration of  $\text{Dy}^{3+}$  ions up to 2.0 mol% and then decreases. Quenching of luminescence with increasing  $\text{Dy}^{3+}$  ion concentration takes place as the distance between the neighboring

Fig. 7 Emission spectra of doped and codoped  $\text{CaMoO}_4$  phosphors.

$\text{Dy}^{3+}$  ions decreases with the increase of  $\text{Dy}^{3+}$  ions. This decrease in the distance between the ions reduces the radiative transitions, thereby increasing the non-radiative energy transfer through cross relaxation channels. Keeping the  $\text{Dy}^{3+}$  concentration at 2 mol%, the  $\text{K}^+$  mol concentration was varied from 1 to 5 mol% where the maximum intensity was recorded at 2 mol% of  $\text{K}^+$ . This was due to the charge compensation phenomena as  $2\text{Ca}^{2+} = \text{Dy}^{3+} + \text{K}^+$ . This  $\text{K}^+$  codoping increases the nonradiative decay paths for excited  $\text{Dy}^{3+}$  which increases the emission intensity. But further increase in  $\text{K}^+$  greater than 2 mol% increases the lattice distortion which reduces the emission intensity.<sup>9</sup>

From the calculated J–O intensity parameters, the spectral parameters such as radiative transition probability ( $A_R$ ), lifetime ( $\tau_R$ ) and branching ratio ( $\beta_R$ ) were calculated. The emission spectra were used to calculate the parameters like peak emission wavelength ( $\lambda_p$ ), effective line widths ( $\Delta\lambda_{\text{eff}}$ ) and the peak emission cross-section ( $\sigma(\lambda_p)$ ) using eqn (5)–(8). Experimental branching ratio ( $\beta_{\text{exp}}$ ) was obtained by using the relative intensities of individual peaks to that of the total intensity of emission peaks. All the spectral parameters including  $A_T$  and  $\tau_R$  for the excited  $^4\text{F}_{9/2}$  level are tabulated in Table 3.

Table 3 Spectral parameters

Phosphor	Transition $^4F_{9/2} \rightarrow$	$\beta_{\text{exp}}$	$\beta_{\text{cal}}$	$A_R \times 10^3 \text{ (s}^{-1}\text{)}$	$\sigma(\lambda_p) \times 10^{-20} \text{ cm}^2$
CaMoO <sub>4</sub> :Dy <sub>0.02</sub> <sup>3+</sup>	$^6H_{15/2}$	0.306	0.111	0.619	0.100
	$^6H_{13/2}$	0.691	0.844	4.6996	1.52
	$^6H_{11/2}$	0.031	0.045	0.2525	0.103
	$A_T = 5.5711, \tau_R = 179.5 \text{ } \mu\text{s}$				
CaMoO <sub>4</sub> :Dy <sub>0.02</sub> <sup>3+</sup> , K <sub>0.02</sub> <sup>+</sup>	$^6H_{15/2}$	0.355	0.093	0.7865	0.079
	$^6H_{13/2}$	0.631	1.015	8.6093	2.56
	$^6H_{11/2}$	0.003	0.010	0.0869	0.029
	$A_T = 8.4827, \tau_R = 105.5 \text{ } \mu\text{s}$				

The radiative lifetimes of the  $^4F_{9/2}$  level decreases from 179.5  $\mu\text{s}$  to 105.5  $\mu\text{s}$  with the incorporation of K<sup>+</sup> ions. From the emission spectra as well as from the values of  $\beta_{\text{exp}}$ , it was found that the  $^4F_{9/2} \rightarrow ^6H_{13/2}$  transition sweeps most of the intensity emitted by the phosphor. The radiative transition probability and peak emission cross-section were also found to be higher for  $^4F_{9/2} \rightarrow ^6H_{13/2}$  transition compared to the other transitions. This high  $\sigma(\lambda_p)$  value suggests that the  $^4F_{9/2} \rightarrow ^6H_{13/2}$  transition has potential application for lasing action.

Further, in order to compare the luminescence intensity, the intensity area under the curve of magnetic and electric dipole transitions was determined by fitting with Gaussian distribution function

$$I = I_B + \sum_{i=1}^n \frac{A_i}{w_i \sqrt{\pi/2}} e^{-\frac{(\lambda - \lambda_{ci})^2}{w_i^2}} \quad (10)$$

where  $I$  is intensity,  $I_B$  is the background intensity,  $w_i$  is the width at half maximum intensity of the curve, and  $A_i$  is area under the curve.  $\lambda$  is wavelength and  $\lambda_{ci}$  is the mean wavelength value corresponding to the transition. All the fittings were carried out in the range of 450–510 and 535–615 nm for magnetic and electric dipole transitions, respectively. The relative intensity ratio  $^4F_{9/2} \rightarrow ^6H_{13/2}$  to  $^4F_{9/2} \rightarrow ^6H_{15/2}$  transitions can be used as sensitive parameter for understanding the symmetry around the Dy<sup>3+</sup> in the host material. This parameter is called asymmetric ratio ( $A_{12}$ )<sup>30</sup> and is defined as

$$A_{21} = \frac{\int_{535}^{615} I_2 d\lambda}{\int_{450}^{510} I_1 d\lambda} \quad (11)$$

where  $I_1$  and  $I_2$  represent the respective integrated intensities of  $^4F_{9/2} \rightarrow ^6H_{15/2}$  and  $^4F_{9/2} \rightarrow ^6H_{13/2}$  transitions of Dy<sup>3+</sup>, respectively. This ratio varies from 2.22 to 2.25 with the variation of Dy<sup>3+</sup> concentration. When K<sup>+</sup> is codoped the asymmetric ratio drastically decreases to 1.85. Higher value of  $A_{21}$  indicates more asymmetry around Dy<sup>3+</sup> ligand. This indicates that with K<sup>+</sup> codoping the symmetry nature of Dy<sup>3+</sup> ligand increases in the host matrix.

**3.2.4. Quantum yield.** External quantum efficiency (EQE) generally known as quantum yield ( $\eta$ ) is related to number of photons incident on the sample ( $\alpha$ ) and number of photons emitted ( $\varepsilon$ ) as<sup>30,31</sup>

$$\eta = \frac{\varepsilon}{\alpha} = \frac{\int I_{\text{emission}}}{\int I_{\text{solvent}} - I_{\text{sample}}} \quad (12)$$

where  $I_{\text{emission}}$  is luminescence emission spectrum of sample,  $I_{\text{solvent}}$  is the spectrum of light used to excite only solvent and  $I_{\text{sample}}$  is the spectrum of light used for exciting sample. Quantum yields for 2 mol% Dy<sup>3+</sup> doped and K<sup>+</sup> codoped phosphors found to be 5% and 8%, respectively.

**3.2.5. Decay curve analysis.** Theoretically, the measured lifetime ( $\tau_{\text{mes}}$ ) of the  $^4F_{9/2}$  fluorescent level can be expressed as:<sup>20</sup>

$$\frac{1}{\tau_{\text{mes}}} = \frac{1}{\tau_R} + W_{\text{NR}} \quad (13)$$

where  $\tau_{\text{mes}}$  and  $\tau_R$  are the measured and radiative lifetimes obtained from decay curves and J–O theory respectively.  $W_{\text{NR}}$  is the non-radiative relaxation rate which includes multi-phonon relaxation ( $W_{\text{MP}}$ ), energy transfer through cross-relaxation ( $W_{\text{CR}}$ ) and several other non radiative processes. The multi-phonon relaxation is inefficient owing to the significantly large energy gap between the  $^4F_{9/2}$  emitting level and the next-lower level (about 8000  $\text{cm}^{-1}$ ) as compared with the maximum phonon energy of the matrix lattice.<sup>27</sup> So only radiative transition and non-radiative energy transfer relaxation is responsible for the depopulation of the  $^4F_{9/2}$  multiplet. The internal quantum efficiency (IQE) of the excited  $^4F_{9/2}$  state ( $\eta$ ) is given by equation

$$\eta = \frac{\tau_{\text{mes}}}{\tau_R} \quad (14)$$

This IQE is completely different from the EQE calculated before as explained in ref. 32. Fig. 8 shows the decay curves of Dy<sup>3+</sup> ions at 576 nm emission of  $^4F_{9/2}$  excited level CaMoO<sub>4</sub> at 2 mol% concentration and 2 mol% K<sup>+</sup> codoped CaMoO<sub>4</sub>.

To understand behavior of luminescence decay, the decay data were fitted with different decay equations. It was found that curves follow two types of exponential decays for Dy<sup>3+</sup> doped and Dy<sup>3+</sup>/K<sup>+</sup> codoped phosphors respectively in the host viz., (i) bi-exponential decay

$$I(t) = I_1 e^{-\frac{t}{\tau_1}} + I_2 e^{-\frac{t}{\tau_2}} \quad (15)$$



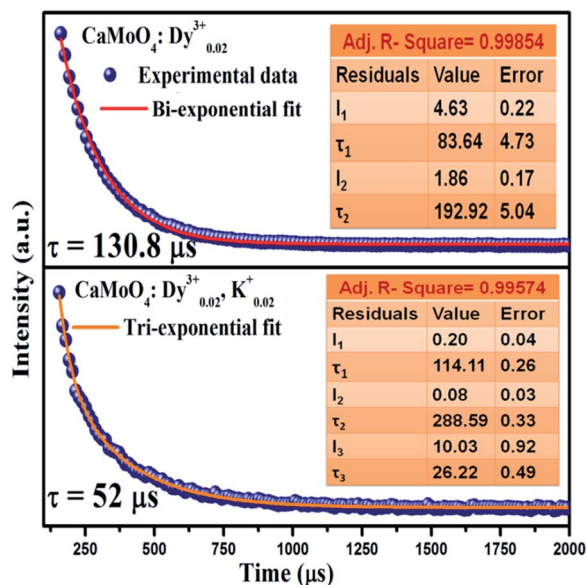


Fig. 8 Luminescence decay curve of CaMoO<sub>4</sub> phosphors.

where  $I_1$  and  $I_2$  are intensities at different times and their corresponding lifetimes  $\tau_1$  and  $\tau_2$ .

The average lifetime in case of a bi-exponential decay can be calculated using the equation

$$\tau_{\text{avg}} = \frac{I_1 \tau_1^2 + I_2 \tau_2^2}{I_1 \tau_1 + I_2 \tau_2} \quad (16)$$

and (ii) triexponential decay

$$I(t) = I_1 e^{-\frac{t}{\tau_1}} + I_2 e^{-\frac{t}{\tau_2}} + I_3 e^{-\frac{t}{\tau_3}} \quad (17)$$

where  $I_1$ ,  $I_2$  and  $I_3$  are intensities at different times and their corresponding lifetimes  $\tau_1$ ,  $\tau_2$  and  $\tau_3$ .

The average lifetime in case of a tri-exponential decay can be calculated using the equation

$$\tau_{\text{avg}} = \frac{I_1 \tau_1^2 + I_2 \tau_2^2 + I_3 \tau_3^2}{I_1 \tau_1 + I_2 \tau_2 + I_3 \tau_3} \quad (18)$$

The multiexponential decay may be explained as:<sup>29</sup>

(i) Difference in the nonradiative probability of decays for lanthanide ions at or near the surface and lanthanide ions in the core of the particles.

(ii) Inhomogeneous distribution of the doping ions in the host material leading to the variation in the local concentration.

(iii) The transfer of excitation energy from donor to lanthanide activators.

Moreover biexponential decay behavior has been reported for low concentration of lanthanide ions in different matrices which is also the case in the present paper.

The fluorescence lifetime  $\tau_{\text{meas}}$  ( $\tau_{\text{avg}}$ ) of the  $^4F_{9/2}$  multiplet was calculated to be 130.80  $\mu\text{s}$  for Dy<sup>3+</sup> doped CaMoO<sub>4</sub> and decreases to 52  $\mu\text{s}$  for K<sup>+</sup> codoped CaMoO<sub>4</sub>. The deviation between the  $\tau_{\text{meas}}$  and  $\tau_r$  (obtained from J–O theory) may be

because the Judd–Ofelt theory is prone to overestimate the value of the radiative lifetime due to its partial inadequacy to predict the radiative properties.<sup>27</sup> Moreover, structural defects and the presence of several Dy<sup>3+</sup> sites in the matrix may impact the  $^4F_{9/2}$  level emission, leading to  $\tau_{\text{meas}}$  lower than expected. It is clearly seen from the result that after K<sup>+</sup> codoping, the lifetime reduces. Codoping with K<sup>+</sup> ion increases the nonradiative decay paths for excited Dy<sup>3+</sup>. This increases the nonradiative transition probability which increases the radiative luminescence emission rate.<sup>33</sup> The increase in the total transition probability reduces the lifetime after K<sup>+</sup> codoping as the lifetime is inverse of the total transition probability.

The IQE for the 2 mol% doped Dy<sup>3+</sup> and 2 mol% K<sup>+</sup> compensated CaMoO<sub>4</sub> phosphors were found to be 72.42% and 49.52% respectively.

## 4. Conclusion

The Judd–Ofelt theory, extended for powder phosphors using excitation spectra instead of conventional absorption spectra, has been successfully applied to evaluate the intensity parameters, radiative transition rates, branching ratios and radiative lifetimes relevant to the  $^4F_{9/2}$  level of Dy<sup>3+</sup> ion in CaMoO<sub>4</sub> host. A strong yellow and blue emission bands were observed in the visible region upon efficient excitation by near UV light which was well matched with near UV LEDs. The phosphor was characterized by high values of emission cross-section and branching ratio for the  $^4F_{9/2} \rightarrow ^6H_{13/2}$  transition (yellow colour) which increases after K<sup>+</sup> codoping. As reported previously, the doped/codoped CaMoO<sub>4</sub> phosphors can be utilized in commercial white LEDs and other display devices owing to its colour tunable property. In this present study the fluorescence and radiative lifetimes of  $^4F_{9/2}$  level with suitable quantum efficiency also indicates that this doped/codoped phosphor may be efficiently used for solid-state yellow lasers pumped by commercially available blue laser diodes.

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