Anomalous Behavior of the Ethyl Group in the Aminolysis of S-Phenyl Acetate with Benzylamine in Acetonitrile

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The rates of the aminolysis of *S*-phenyl substituted-acetate series (RC(=O)SC₆H₄Z, with R=Me, Et, *i*-Pr, *t*-Bu and Bn) with benzylamines (XC₆H₄CH₂NH₂) are not correlated simply with the Taft's polar (σ^*) and/or steric effect constants (E_s) of the substituents due to abnormally enhanced rate of the substrate with R=Et. Furthermore, the cross-interaction constant, ρ_{X_Z} , is the largest with R=Et. These anomalous behaviors can only be explained by invoking the vicinal bond (σ)-antibond (σ^*) charge transfer interaction between C-C_{\alpha} and C-S bonds. In the tetrahedral zwitterionic intermediate, T[±], formed with R=Et the vicinal $\sigma_{\text{C-C}}$ - $\sigma^*_{\text{C-S}}$ delocalization is the strongest with an optimum antiperiplanar arrangement and a narrow energy gap, $\Delta \varepsilon = \varepsilon_{\sigma^*}$ - ε_{σ} . Due to this charge transfer interaction, the stability of the intermediate increases (with the concomitant increase in the equilibrium constant K (= k_a/k_{-a})) and also the leaving ability of the thiophenolate leaving group increases (and hence k_b increases) so that the overall rate, $k_N = Kk_b$, is strongly enhanced. Theoretical support is provided by the natural bond orbital (NBO) analyses at the B3LYP/6-31+G* level. The anomaly exhibited by R=Et attests to the stepwise reaction mechanism in which the leaving group departure is rate limiting.

Keywords: Aminolysis of *S*-phenyl substituted-acetate series, Anomalous behaviors of the ethyl group, Natural bond orbital (NBO) analysis, Cross-interaction constant.

Introduction

The nucleophilic substitution reactions of *S*-phenyl substituted-acetate (SPA) series, RC(=O)SAr where R=Me (CH₃), 1 Et(CH₃CH₂), 2 *i*-Pr((CH₃)₂CH), 3 *t*-Bu((CH₃)₃C) 3 and Bn(C₆H₅CH₂), 4 with a large excess amount of benzylamines in acetonitrile are found to proceed by a stepwise mechanism through a tetrahedral zwitterionic intermediate, T[±], with rate-limiting expulsion of the leaving group, thiophenolate anion (ArS⁻), k_b in eq. 1. Since the reactions occur in two steps, the overall rate constants, k_N , are complex, eq. 2.

$$RC(=O)SC_{6}H_{4}Z + 2XC_{6}H_{4}CH_{2}NH_{2} \xrightarrow{k_{a}} R_{-C}^{O}-SC_{6}H_{4}Z$$

$$SPA \qquad T^{\pm} \qquad (1)$$

$$k_{b} \qquad RC(=O)NHCH_{2}C_{6}H_{4}X + XC_{6}H_{4}CH_{2}NH_{3} + SC_{6}H_{4}Z$$

$$k_{N} = (k_{a}/k_{-a}) \cdot k_{b} = K \cdot k_{b}$$
(2)

The reactivity and selectivity parameters including the cross-interaction constants,⁵ ρ_{XZ} , in eqs. 3 where X and Z represent substituents in the nucleophile and leaving group,

$$\log(k_{\rm XZ}/k_{\rm HH}) = \rho_{\rm X}\sigma_{\rm X} + \rho_{\rm Z}\sigma_{\rm Z} + \rho_{\rm XZ}\sigma_{\rm X}\sigma_{\rm Z}$$
 (3a)

$$\rho_{XZ} = \partial \rho_Z / \partial \sigma_X = \partial \rho_X / \partial \sigma_Z \tag{3b}$$

respectively, are summarized in Table 1. One notes im-

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mediately from this Table anomalously high rate (k_N) and large magnitude of ρ_{XZ} for the α -methyl substituted acetate, i.e., R=Et. The purpose of this work is to examine factors that are responsible for such anomalous behaviors exhibited by the S-phenyl acetate homologue (SPA) with R=Et. Since the Taft's polar $(\sigma^*)^6$ as well as steric effect constant $(E_s)^6$ decreases, i.e., becomes more negative, by a successive α methylation from R=Me to R=t-Bu (Table 1), reactivity is expected to change (increase or decrease) successively along with the increase in the number of methyl group on the α carbon when the same mechanism applies to all the members in the series, as normally have been observed and reported.6 The unexpected anomaly observed with R=Et therefore suggests some important stereoelectronic factors operative in the transition state that are not reflected in the Taft's σ^* and E_s substituent constants.

Results and Discussion

The rate constants, $k_{\rm N}$ in Table 1, are correlated (excluding R=Et) with the Taft's polar substituent constants, σ^* , eq. 4,6 where k_0 is the $k_{\rm N}$ value with R=Me for which σ^* = 0.

$$\log(k_{\rm N}/k_0) = \rho^* \sigma^* \tag{4}$$

Figure 1 shows that the ρ^* value obtained for 4 R's except R=Et is ρ^* =2.97 ± 0.22 with correlation coefficient r = 0.994. The observed reactivity of R=Et is higher by ca. 16 times than that derived from eq. 4. In contrast to the good correlation of $\log k_N vs$. σ^* , inclusion of the steric effect (eq. 5a)⁶ gave unsatisfactory correlation, eq. 5b, with r = 0.779 for the 5 R's.

Table 1. Reactivity parameters for the reactions of RC(=O)SC₆H₄Z with XC₆H₄CH₂NH₂ in acetonitrile at 45 °C

R	$\sigma^{\!*}$	$E_{\rm s}$	$k_2 \times 10^{3a}$ (M ⁻¹ s ⁻¹)	$ ho_{\mathrm{X}}^{b}$ $(oldsymbol{eta}_{\mathrm{X}})$	$ ho_{ extsf{Z}}^{c}$ $(eta_{ extsf{Z}})$	$ ho_{ ext{XZ}}$	ΔH^{\ddagger} (kcal mol ⁻¹)	–Δ <i>S</i> [‡] (e.u.)	$k_{ m H}/k_{ m D}$	ref.
Me, CH ₃	0.00	0.00	1.65	-1.40 (1.36)	5.32 (-2.21)	0.90	5.2-6.2	46-56	1.25-1.39 (1.33) ^d	1
Et, C_2H_5	-0.10	-0.07	13.6	-2.09 (2.11)	2.74 (-1.18)	2.36	3.9-4.6	53-60	1.18-1.24 (1.23)	2
<i>i</i> -Pr, (CH ₃) ₂ CH	-0.19	-0.47	0.320	-1.33 (1.30)	4.35 (-1.82)	0.82	10.6-13.2	30-41	1.22-1.53 (1.22)	3
t-Bu, (CH ₃) ₃ C	-0.30	-1.54	0.221^{e}	-1.35 (1.30)	3.65 (-1.49)	1.05	9.9-11.5	39-46	1.23-1.51 (1.23)	3
Bn, C ₆ H ₅ CH ₂	0.22	-0.33	6.68	-1.50 (1.55)	1.61 (-1.66)	0.92	4.2-5.5	49-60	1.21-1.72 (1.36)	4

 $^{^{}a}X = p$ -MeO and Z = p-Me at 45 $^{\circ}$ C. $^{b}Z = H$. $^{c}X = H$. $^{d}X = p$ -MeO and Z = p-Me at 45 $^{\circ}$ C. $^{e}Extrapolated$ value from Arrhenius plot.

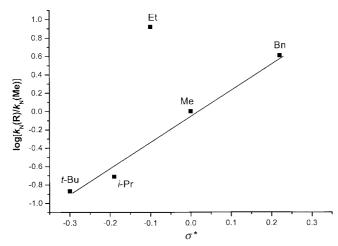


Figure 1. The plot log $[k_N(R)/k_N(Me)]$ *vs.* σ^* for the reactions of RC(=O)SC₆H₄-p-CH₃ with p-CH₃OC₆H₄CH₂NH₂ at 45 °C where R= Me, Et, i-Pr, t-Bu and Bn.

$$\log(k_{\rm N}/k_0) = \rho^* \sigma^* + SE_{\rm s} \tag{5a}$$

$$\log(k_{\rm N}/k_0) = 1.74 \pm 2.19\,\sigma^* + 0.55 \pm 0.70E_{\rm s} \tag{5b}$$

For the three points (R=Me, i-Pr, t-Bu) correlation of log $(k_{\rm N}/k_0)$ with the steric effect constants, $(E_{\rm s})$, gave $S=0.30\pm$ 0.05 (r = 0.987); the two, R=Et and Bn, deviated wildly from the linearity. Comparison of the ρ^* and S values suggests that the steric effect (E_s) contributes much less (ca. one tenth) than the polar effect (σ^*) to the overall rates. One reason for this could be that the steric effect is compensated by its opposite influence on the rate. In the addition step, k_a , the bulkier the substituent R, the rate becomes more retarded by steric hindrance, whereas the rate is enhanced by steric relieving effect in the rate-limiting expulsion of the leaving group (k_b) from the intermediate, T^{\pm} . The negligible steric effect has led, of course, to the satisfactory correlation with polar effect alone (eq. 4). The $\rho^* \sigma^*$ correlation (eq. 4) is expected to apply for the reaction where steric and conjugative effects do not play any role.^{6,7} For example the S_N1 and S_N2 reactivities of alkyl derivatives are normally well correlated with eq. 4.7

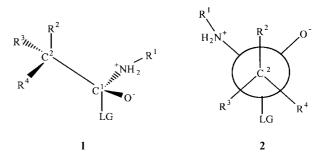
The anomalous reactivity found with R=Et cannot be due

to the steric effect since there is no reason to believe the ethyl group has an anomalously rate enhancing streic effect. We therefore think that it is caused by a rather strong conjugative effect within the TS. Since the rate constant k_N is composed of two constants, $k_N = K \cdot k_b$, the rate enhancing effect can be on either K or k_b , or on both.

In the molecular orbital theory, the proximate (geminal and/or vicinal) bond-antibond $(\sigma - \sigma^*)$ charge transfer delocalization stabilizations are well established effects. The charge transfer takes place from a bonding orbital (which can be π , σ or lone pair, n) to an unoccupied antibonding orbital (which can be π^* or σ^*), represented in general as $\sigma - \sigma^*$, and the stabilization energy is given by a second-order perturbation energy, $\Delta E^{(2)}_{\sigma - \sigma^*}$, in eq. 6 where $\Delta \varepsilon$ is the energy gap between the two, bonding (π, n) or σ type) and

$$\Delta E^{(2)}_{\sigma - \sigma^*} = -2F^2_{\sigma \sigma^*} / (\varepsilon_{\sigma^*} - \varepsilon_{\sigma}) \cong -2(kS_{\sigma \sigma^*})^2 / \Delta \varepsilon \tag{6}$$

antibonding, orbital levels (π^* or σ^* type) and $F_{\sigma\sigma^*}$ is the Fock matrix element which is proportional (with a constant k) to the overlap ($S_{\sigma\sigma^*}$) between the two orbitals. Now if we look at the T[±] intermediate structures, **1** and **2** in Scheme 1, for the case of (**b**) the C²-R² σ bond is located antiperiplanar to the vicinal C¹-LG antibonding σ^* orbital, as can be readily seen in structure **2**. The vicinal σ - σ^* charge transfer interaction is stronger when they are antiperiplanar than they are synperiplanar to each other. We therefore expect that in



Scheme 1. R^1 = $C_6H_5CH_2$ and LG= SC_6H_4Z , (a) $Me: R^2$ = R^3 = R^4 =H, (b) $Et: R^2$ = CH_3, R^3 = R^4 =H, (c) i- $Pr: R^2$ = R^3 = CH_3, R^4 =H, (d) t- $Bu: R^2$ = R^3 = R^4 = CH_3 .

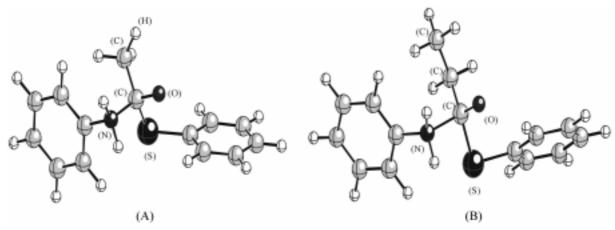


Figure 2. The structure of tetrahedral intermediate (T^{\pm}) bound with aniline and S-phenyl methyl (A) and ethyl (B) acetate at the RHF/3-21G*/RHF/3-21G* level.

the case of (**b**) with R=Et, there will be a strong charge transfer delocalization and the structure, *i.e.*, the T^{\pm} intermediate, is strongly stabilized (and hence K is large in eq. 2). The natural bond orbital (NBO) theory^{8b-c} predicts that the $\sigma_{AB} - \sigma^*_{CD}$ NBO delocalization leads to a decrease in A-B and C-D bond orders (and hence causes stretching of the bonds) and a simultaneous increase in B-C bond order (causes contraction of B-C bond). In other words the $\sigma_{C-C} - \sigma^*_{C-S}$ interaction in (**b**) leads to overall stabilization of the intermediate, T^{\pm} , (increase in K), but stretches the C-S bond somewhat, which facilitates, of course, the expulsion of the leaving group, $ZC_6H_4S^-$, in the rate-limiting step (increase in k_b). As a result, the rate is enhanced since both K and k_b in eq. 2 are increased. An antiperiplanar arrangement intermediate structure is presented in Figure 2.

What about in other compounds? Since the σ_{C-H} level is lower than the σ_{C-C} level, ^{8a} the $\sigma-\sigma^*$ interaction in (a) with R=Me will be smaller due to a larger energy gap, $\Delta \varepsilon$, in eq. 6. For R=i-Pr (c) and t-Bu (d) cases, the electron-donating ability increases with an increase in the number of Me group on the C^2 atom (as reflected in the almost 2 and 3 times more negative Taft polar effect (σ^*) constants⁶ in Table 1). As a result of this greater electron donation toward the C-S bond, the σ^*_{C-S} orbital level is raised⁹ and leads to a wider energy gap, $\Delta \varepsilon$, in eq. 6 and reduces the charge transfer stabilization energies, $\Delta E^{(2)}_{\sigma-\sigma^*}$. Furthermore as the α -carbon is successively methylated, steric inhibition increases in the intermediate, T[±], which will cause stretching of the C¹-C² bond^{8b,d} and in effect the overlap, $S_{\sigma\sigma^*}$, decreases. These two effects, (i) wider energy gap, ($\Delta \varepsilon = \text{large}$), and (ii) weaker overlap, $(S_{\sigma\sigma^*} = \text{small})$ cause weak and insignificant stabilization of the T[±] structure and the rate enhancing effect due to $\sigma_{C-C} - \sigma^*_{C-S}$ interaction becomes small (much smaller than that for R=Et case). For R=Bn, the phenyl group is a relatively strong electron-acceptor (σ^* =+0.22) so that the $\sigma_{\text{C-C}}$ level is depressed⁹ and hence $\Delta E^{(2)}_{\sigma-\sigma^*}$, decreases due to a wider energy gap, $\Delta \varepsilon$, in eq. 6.

We have performed natural bond orbital (NBO) analyses^{8b-e} to calculate charge transfer energies using a model system (3) with R^1 =H and LG=F in 1 and 2. For the

ethyl case, R=Et, the σ - σ^*_{C-F} vicinal charge transfer stabilization⁸ is the largest with $\Delta E^{(2)}_{\sigma-\sigma^*}$ = -4.9 kcal mol⁻¹ at

$$R \longrightarrow C \longrightarrow F$$
 NH_3
 $R = Me, Et, i-Pr and t-Bu$
3

the B3LYP/6-31+G* level of theory. For the R=Me, *i*-Pr and *t*-Bu, the corresponding stabilization energies are lower with -4.5, -2.9 and -3.2 kcal mol⁻¹ respectively. Albeit the differences in the charge transfer stabilization energies are small due to the adoption of a model calculation, the expected trend is borne out in the result of our density functional theory (DFT) calculation.¹⁰

In conclusion, the vicinal $\sigma_{\text{C-C}} - \sigma^*_{\text{C-S}}$ charge transfer delocalization is the strongest with R=Et due to the optimum, antiperiplanar, arrangement between σ and σ^* orbitals as well as the narrow energy gap, $\Delta \varepsilon$.

The most stable intermediate, T^{\pm} , with R=Et should provide the strongest C-N bond and hence the largest magnitude of ρ_X and β_X value is observed experimentally (Table 1). The strongest σ - σ^* interaction should lead to a facile C-S bond cleavage in the rate-determining step, k_b , and the TS is reached at an early stage with lower degree of bond cleavage. The lower degree of bond cleavage is reflected in the smaller magnitude of β_Z (or ρ_Z) value, and also in the low activation enthalpy, ΔH^{\ddagger} , in Table 1. It is well known that the main component of the deformation energy, ΔE_{def} , which is required to transform the reactant to the TS structure, is the stretching of the cleaving bond. Thus a tightest TS is realized with R=Et as evidenced by the largest positive cross-interaction constant, ρ_{XZ} , in Table 1.

The kinetic isotope effects $k_{\rm H}/k_{\rm D}$, involving deuterated benzylamine (XC₆H₄CH₂ND₂) nucleophiles are all greater than unity¹² and the magnitude is similar so that the $k_{\rm H}/k_{\rm D}$ values do not provide a very sensitive measure of the TS structure.

The anomalous reactivity and large magnitude of ρ_{XZ} found with R=Et in the S-phenyl series are also found in the dithio series, RC(=S)SC₆H₄Z. The rate is the fastest and the ρ_{XZ} value is the largest with R=Et in the dithio series studied so far (R=Me, 13 Et14 and Bn15). If our interpretation is correct, the same anomaly will be found with R=Et in the phenolate series, RC(=O)OC₆H₄Z, as well as in the thiono series, RC(=S)OC₆H₄Z . Substitution of O by S, or of S by O, does not change the strongest vicinal $\sigma_{CC} - \sigma^*_{C-LG}$ charge transfer interaction expected with R=Et, as can be seen in Scheme 1. The same argument presented above for the Sphenyl series should apply to the other series, provided the same stepwise mechanism applies to all the members in the respective series. We stress that the anomaly observed with R=Et is a manifestation of the stepwise mechanism through a tetrahedral zwitterionic intermediate with rate-limiting expulsion of the leaving group on the grounds that : (i) If the bond formation step, in which polar effect alone is important, were rate-limiting, the rate order should have been in the order of the Taft's σ^* constant; R = t-Bu < i-Pr <Et < Me < Bn. (ii) If the reaction rates were affected exclusively by steric effects of the type present in reactions used to define E_s , the rate (log k_N) should have been well correlated with the steric effect constant, E_s , alone with the susceptibility constant S. (iii) If the reactions proceeded by a simple concerted (S_N2) process, the Taft equation (5a) should have been valid. (iv) If the bond cleavage were solely responsible in determining the rate, the rate order should have been in the reverse order of the Taft's σ^* constants since electron donating R group facilitates leaving group expulsion¹⁶; R=Bn < Me < Et < i-Pr < t-Bu.

We conclude that the anomaly observed with R=Et provides evidence for a stepwise mechanism in which the rate constant (k_N) is composed of two factors as expressed by eqn. (2). Thus the observed rate is determined by both the stability (K) of the intermediate, T^{\pm} , and nucleofugality of the leaving group (k_b) . Both of these factors are outstandingly favorable for the reactions with R=Et due to the strong vicinal σ_{C-C} - σ^*_{C-S} charge transfer interaction in the intermediate, T^{\pm} . Further experimental as well as theoretical works are in progress to support our arguments presented in this work.

Calculations. *Ab initio* MO calculations were performed with Gaussian 98 system of programs.¹⁷ Geometries were optimized at the B3LYP/6-31+G* level of theory. The natural bond orbital (NBO) analyses were carried out to obtain proximate bond - antibond $(\sigma - \sigma^*)$ orbital interaction energies $(\Delta E^{(2)}\sigma - \sigma^*)$ at the NBO-B3LYP/6-31+G* level.

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