

Structure Study of Polycrystalline $\text{Na}_3\text{YSi}_3\text{O}_9$ and Its Substitutes Related to $\text{Na}_4\text{CaSi}_3\text{O}_9$, $\text{Ca}_3\text{Al}_2\text{O}_6$ Structure

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The study of the $\text{Na}_3\text{YSi}_3\text{O}_9$ structure, by x-ray diffraction and infrared spectrum, showed that $\text{Na}_3\text{YSi}_3\text{O}_9$ is similar to $\text{Na}_4\text{CaSi}_3\text{O}_9$, except for its being pseudo-cubic instead of cubic. The peaks in the x-ray diffraction pattern of $\text{Na}_3\text{YSi}_3\text{O}_9$ could therefore be indexed on the basis of the $\text{Na}_4\text{CaSi}_3\text{O}_9$ cell. Also, modified $\text{Na}_3\text{MSi}_3\text{O}_9$ ($M = \text{Lu}, \text{Yb}, \text{Tm}, \text{Er}, \text{Y}, \text{Ho}, \text{Dy}, \text{Gd}, \text{Eu}, \text{and Sm}$) type compounds were synthesized by introducing excess sodium, decreasing $M(\text{III})$ concentration, and substituting small amount of phosphorus for silicon. The unit cell parameters of the composition $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_2\text{P}_{0.1}\text{O}_8$ were estimated from x-ray powder diffraction patterns using the Cohen method.

Introduction

In 1970 Maki and Sugimura¹ showed that $\text{Na}_4\text{CaSi}_3\text{O}_9$ is very similar crystallographically to $\text{Ca}_3\text{Al}_2\text{O}_6$. Both belong to space group $\text{Pa}\bar{3}$ and have similar unit cell dimensions. The unit cell of $\text{Ca}_3\text{Al}_2\text{O}_6$ consists of 72 Ca, 48 Al and 144 O. A unit cell of $\text{Na}_4\text{CaSi}_3\text{O}_9$ consists of 64 Na, 16 Ca, 48 Si, and 144 O. Thus there exist eight additional cations per unit cell in $\text{Na}_4\text{CaSi}_3\text{O}_9$. Mondal and Jeffery² refined the $\text{Ca}_3\text{Al}_2\text{O}_6$ structure with $R = 5.1\%$ and reported that "the structure consists of eight Al_6O_{18} rings in a unit cell, surrounding holes of radius 1.47 Å at $(1/8, 1/8, 1/8)$ and its symmetry-related positions, with calcium ions holding the rings together". According to their

study, "there are 80 possible holes between the eight Al_6O_{18} rings in the unit cell and 72 of them are filled up with calcium, leaving eight vacant. The unit cell of $\text{Ca}_3\text{Al}_2\text{O}_6$ consists of 64 pseudo-cells ($a' = a/4$). The calcium atoms occupy 56 body-centering positions of the pseudo-cells leaving eight of them vacant, namely $(1/8, 1/8, 1/8)$ and its symmetry-related positions. The 48 aluminum atoms and the remaining 16 calcium atoms occupy the corners of the pseudo-cells" (See Figure 1 and 2). They emphasized its isomorphic relationship with $\text{Na}_4\text{CaSi}_3\text{O}_9$ which has Si_6O_{18} rings. In addition, the replacement of CaO by Na_2O in $\text{Ca}_3\text{Al}_2\text{O}_6$ has been proved by Regourd et al.³ because the sizes of calcium ion and sodium ion are comparable and there are eight vacant holes available to replace one calcium ion by two sodium ions.

In 1980, Shannon et al.⁴ reported the unit cell of $\text{Na}_3\text{YSi}_3\text{O}_9$ is similar to those of $\text{Ca}_3\text{Al}_2\text{O}_6$ and $\text{Na}_4\text{CaSi}_3\text{O}_9$. However, no evidence was given for that assumption.

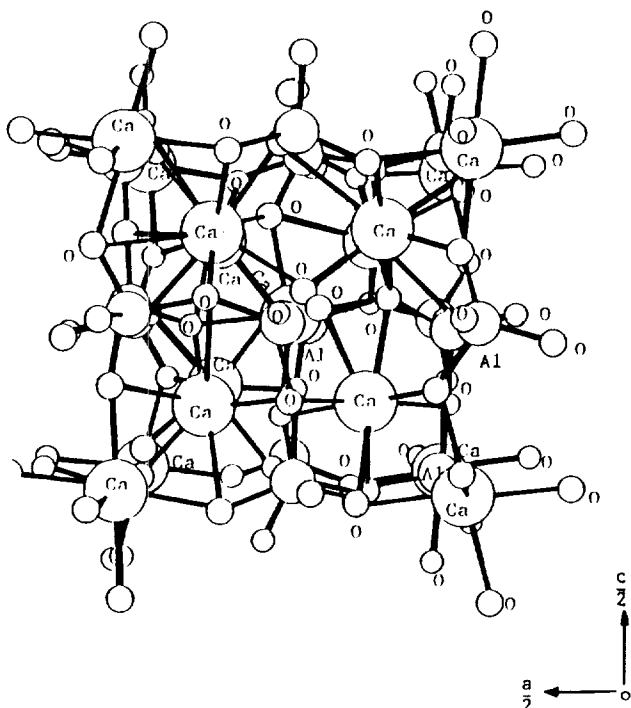
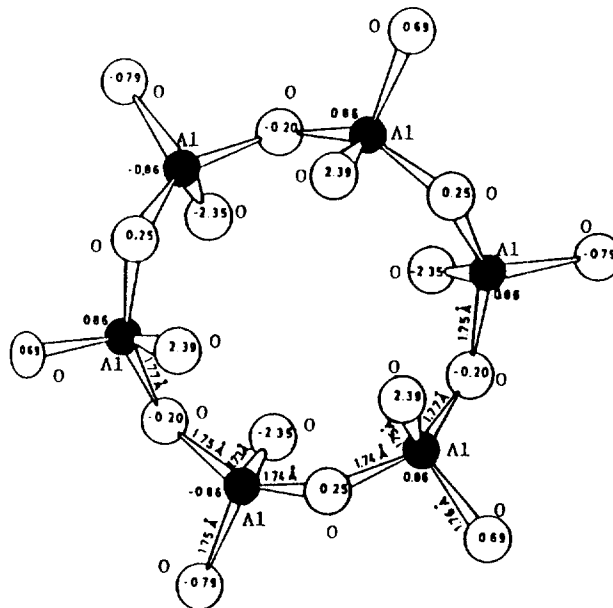


Figure 1. One eighth of the unit cell $\text{Ca}_3\text{Al}_2\text{O}_6$ viewed along $[0\bar{1}0]$. The origin is at rear, right-hand bottom corner.



The results of this work could give stronger confirmation about the $\text{Na}_3\text{YSi}_3\text{O}_9$ structure, which is very similar to $\text{Na}_4\text{CaSi}_3\text{O}_9$ and CaAl_2O_6 except that it is orthorhombic close to being pseudo-cubic instead of cubic. Also, samples of composition $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$ ($\text{M} = \text{Lu}, \text{Yb}, \text{Tm}, \text{Er}, \text{Y}, \text{Ho}, \text{Dy}, \text{Gd}, \text{Eu}, \text{and Sm}$) based on the $\text{Na}_3\text{YSi}_3\text{O}_9$ composition were synthesized. The unit cell parameters were estimated from x-ray powder diffraction patterns using the Cohen method⁵.

Experimental

For the synthesis of $\text{Na}_3\text{YSi}_3\text{O}_9$ starting materials Na_2CO_3 , Y_2O_3 , and SiO_2 were mixed in proper stoichiometric proportion and fired at 1180°C for 18 hours in a furnace. The fired sample was ground and reheated at the same temperature for 5–10 hours. X-ray patterns were obtained on a Philips powder diffractometer using $\text{Cu K}\alpha$ radiation. The indexing of each peak was attempted on the basis of lattice parameter $a = 15.215 \text{ \AA}$, $b = 15.126 \text{ \AA}$, and $c = 15.036 \text{ \AA}$. Also, the infrared spectrum of this specimen was recorded and compared with that of $\text{Na}_4\text{CaSi}_3\text{O}_9$. The infrared instrument used was the Perkin-Elmer Model No. 337.

For the preparation of $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$, the starting materials Na_2CO_3 , SiO_2 , $\text{NH}_4\text{H}_2\text{PO}_4$, and M_2O_3 were weighed and ground in a proper stoichiometric proportion. They were fired for overnight at 890°C – 1020°C (1015°C for $\text{M} = \text{Y}$; 980°C for $\text{M} = \text{Dy}, \text{Yb}$; 945°C for $\text{M} = \text{Ho}, \text{Gd}, \text{Er}$; 930°C for $\text{M} = \text{Eu}, \text{Lu}, \text{Tm}$; and 895°C for $\text{M} = \text{Sm}$) in covered platinum crucibles. Samples were quenched, reground, reheated at the same temperature for 6–12 hours and quenched in air again. X-ray patterns of products obtained by quenching and by cooling at the natural cooling rate of the furnace were essentially the same.

To estimate the lattice parameters of each sample pure Si powder as an internal standard, was mixed with all samples and peaks of the samples between the Si peaks were corrected using the interpolation method. Sample peaks used were in the 2θ range of 60 – 70° since it is practical to deduce accurate values of the lattice constants in the range $\theta = 30$ to 90° ; peaks with indices (844), (484), (448), (880), (808), and (088) were

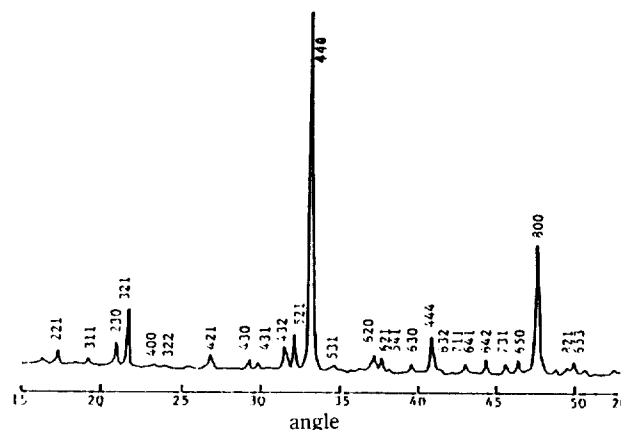


Figure 3. Powder x-ray diffraction pattern of $\text{Ca}_3\text{Al}_2\text{O}_6$.

chosen because they were clearer than the others. In this work the Cohen's least-square method⁵ was employed with angle error term⁶

$$\Delta \sin^2\theta = D \sin^2\theta (1/\sin\theta + 1/\theta).$$

Peak positions were read within about $\pm 0.04^\circ(2\theta)$ after 3–5 trials. The normal equations established were solved by using the matrix function of a programmable Texas Instrument TI-58C calculator.

Results and Discussion

Figures 3 and 4 show the x-ray powder diffraction patterns of $\text{Ca}_3\text{Al}_2\text{O}_6$ and $\text{Na}_4\text{CaSi}_3\text{O}_9$. The diffraction characteristics of these two compounds have been regarded to be essentially similar to each other¹. Figure 5 shows the x-ray powder diffraction pattern of $\text{Na}_3\text{YSi}_3\text{O}_9$. The peaks in the $\text{Na}_3\text{YSi}_3\text{O}_9$ pattern could be indexed on the basis of the $\text{Na}_4\text{CaSi}_3\text{O}_9$ cell. However, the shape of the peaks in $\text{Na}_3\text{YSi}_3\text{O}_9$ pattern is less sharp than those of $\text{Na}_4\text{CaSi}_3\text{O}_9$ due to the pseudo-cubic nature of the cell. In other words, the a , b , and c values are not exactly equal as in a cubic structure, but they are very similar. The X-ray peaks are thus broader due to all possible permutations of (hkl) reflections in the equation $d^{-2} = h^2a^{*2} + k^2b^{*2} + l^2c^{*2}$

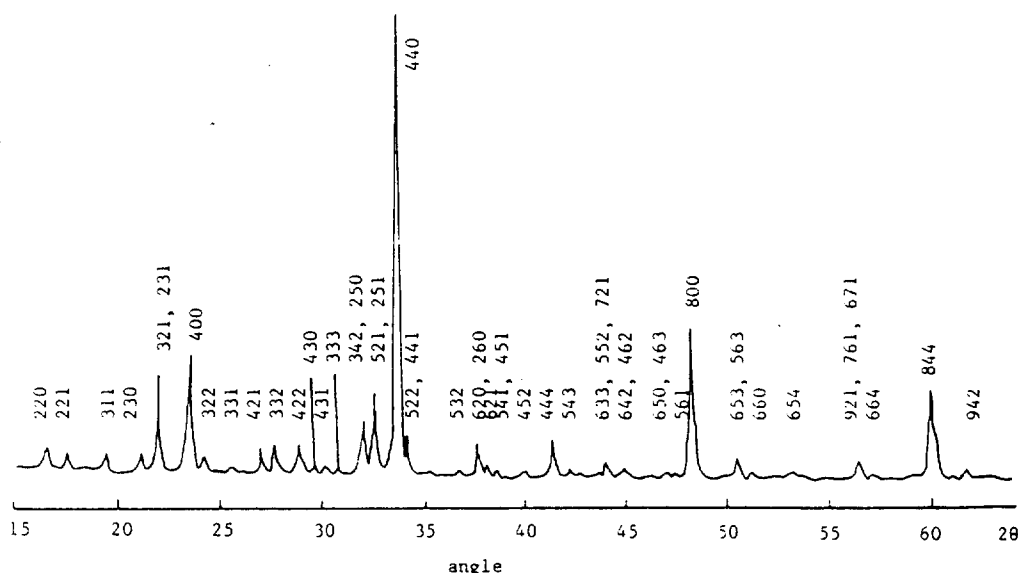
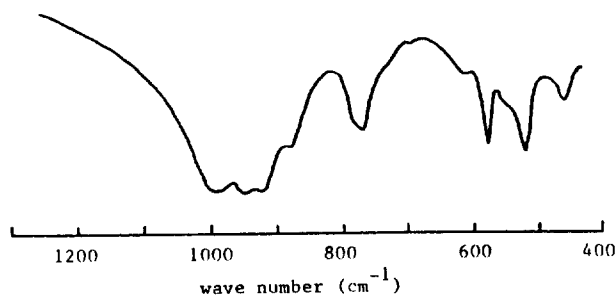


Figure 4. Powder x-ray diffraction pattern of $\text{Na}_4\text{CaSi}_3\text{O}_9$.

Figure 7. Infrared spectrum of $\text{Cu}_6\text{Si}_6\text{O}_{18} \cdot 6\text{H}_2\text{O}$.Table 2. $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$

Formula	Lattice Constants (Å)
$\text{Na}_{3.2}\text{Lu}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.160 \pm 0.006$ $b = 15.076 \pm 0.004$ $c = 14.989 \pm 0.005$
$\text{Na}_{3.2}\text{Yb}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.165 \pm 0.001$ $b = 15.103 \pm 0.001$ $c = 15.000 \pm 0.001$
$\text{Na}_{3.2}\text{Tm}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.192 \pm 0.006$ $b = 15.095 \pm 0.020$ $c = 15.011 \pm 0.015$
$\text{Na}_{3.2}\text{Er}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.193 \pm 0.008$ $b = 15.108 \pm 0.019$ $c = 15.011 \pm 0.016$
$\text{Na}_{3.2}\text{Y}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.211 \pm 0.002$ $b = 15.118 \pm 0.001$ $c = 15.017 \pm 0.001$
$\text{Na}_{3.2}\text{Ho}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.197 \pm 0.003$ $b = 15.124 \pm 0.001$ $c = 15.034 \pm 0.001$
$\text{Na}_{3.2}\text{Dy}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.218 \pm 0.002$ $b = 15.146 \pm 0.001$ $c = 15.040 \pm 0.002$
$\text{Na}_{3.2}\text{Gd}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.241 \pm 0.001$ $b = 15.175 \pm 0.002$ $c = 15.064 \pm 0.002$
$\text{Na}_{3.2}\text{Eu}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$	$a = 15.300 \pm 0.004$ $b = 15.201 \pm 0.005$ $c = 15.074 \pm 0.004$

occurs in spectra of Si_6O_{18} anions and it is probable that the assignment of a considerably higher frequency⁸ than that resulting from calculation is associated with the difficulty in clearly distinguishing the frequencies of the complex anion. It is supposed⁹ that the appearance of a high frequency band is due largely to special features in the dynamics of the anion. The infrared spectrum of diopside ($\text{Cu}_6\text{Si}_6\text{O}_{18} \cdot 6\text{H}_2\text{O}$), in which the Si_6O_{18} ring is a nonplanar structure, has been studied^{9,10}. Figure 7 shows the frequencies of the asymmetric Si-O-Si stretching at about 1000 cm^{-1} and those of symmetric Si-O-Si stretching at about 770 cm^{-1} . In a planar ring the Si-O-Si angle increases. This makes asymmetric stretching energetically favorable and the asymmetric Si-O-Si vibration increases. It was therefore expected that a planar ring might have higher asymmetric Si-O-Si vibrational frequency and lower symmetric Si-O-Si vibrational frequency⁸. As can be

seen in Figure 2, the six bridging oxygen atoms are almost coplanar thus the absorption bands in the $900\text{--}1080\text{ cm}^{-1}$ and 750 cm^{-1} region for $\text{Na}_3\text{YSi}_3\text{O}_9$ may be expected to be due to the Si-O-Si vibration in Si_6O_{18} anion structure.

Even though the synthesis of the $\text{Na}_3\text{YSi}_3\text{O}_9$ single crystal by solid solution method was not successful, the similarities in powder x-ray diffraction pattern and infrared spectra as mentioned above give the idea that $\text{Na}_3\text{YSi}_3\text{O}_9$ and $\text{Na}_3\text{CaSi}_3\text{O}_9$ are nearly isostructural. The unit cell contents of $\text{Na}_3\text{YSi}_3\text{O}_9$ are: 48 Na, 16 Y, 48 Si, and 144 O. The 48 Na and 16 Y would occupy 64 sites holding eight Si_6O_{18} rings coordinated by six SiO_4 tetrahedra, leaving 16 vacant holes.

The x-ray patterns of $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$ ($\text{M} = \text{Lu}, \text{Yb}, \text{Tm}, \text{Er}, \text{Y}, \text{Ho}, \text{Dy}, \text{Gd}, \text{Eu}, \text{and Sm}$) showed that they are isostructural with $\text{Na}_3\text{YSi}_3\text{O}_9$. Only some shifts in the position of the peaks depending on the size of M(III) ion were observed. For estimation of the orthorhombic $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$ lattice constants the following equation was employed:

$$\alpha A + \beta B + \gamma C + \delta D = \sin^2\theta$$

where $\alpha = h^2$, $\beta = k^2$, $\gamma = l^2$, $\delta = \sin^2 2\theta (1/\sin\theta + 1/\theta)$, $A = \lambda^2/4a^2$, $B = \lambda^2/4b^2$, $C = \lambda^2/4c^2$, and $\lambda_{\text{Cu K}\alpha} = 1.5405\text{ Å}$. The combination of the various observational equations led to a set of four normal equations:

$$A\sum\alpha^2 + B\sum\alpha\beta + C\sum\alpha\gamma + D\sum\alpha\delta = \sum\alpha \sin^2\theta$$

$$A\sum\alpha\beta + B\sum\beta^2 + C\sum\beta\gamma + D\sum\beta\delta = \sum\beta \sin^2\theta$$

$$A\sum\alpha\gamma + B\sum\beta\gamma + C\sum\gamma^2 + D\sum\gamma\delta = \sum\gamma \sin^2\theta$$

$$A\sum\alpha\delta + B\sum\beta\delta + C\sum\gamma\delta + D\sum\delta^2 = \sum\delta \sin^2\theta$$

ΔA , ΔB , and ΔC were then calculated with the same method suggested by Cohen. Table 1 shows the procedure estimated for $\text{Na}_{3.2}\text{Yb}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$. Table 2 is the result for $\text{Na}_{3.2}\text{M}_{0.7}\text{Si}_{2.9}\text{P}_{0.1}\text{O}_{8.7}$ using the same procedure described above.

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